

Astronomy 730

Stellar
Populations



Outline

- ▶ **Stellar populations**
 - ▶ Big picture
 - ▶ Stellar classification and properties
 - ▶ Stellar evolution
- ▶ **Understanding stellar populations**
 - ▶ H-R diagrams
 - ▶ Reading: Noël et al. (2007, AJ, 133, 2037), Lewis et al. (2015, ApJ, 805, 183)
 - ▶ What is the data they use? Compare their CMDs.
 - ▶ Integrated light as a function of stellar luminosity: assignment
- ▶ **Stellar Population Synthesis**
 - ▶ Key ingredients
 - ▶ Fuel Consumption theorem
 - ▶ Differential Populations Synthesis
 - ▶ Simple Populations Synthesis and why it works
- ▶ **Nucleosynthesis**
 - ▶ Abundance patterns: definitions and observations
 - ▶ Chemical evolution



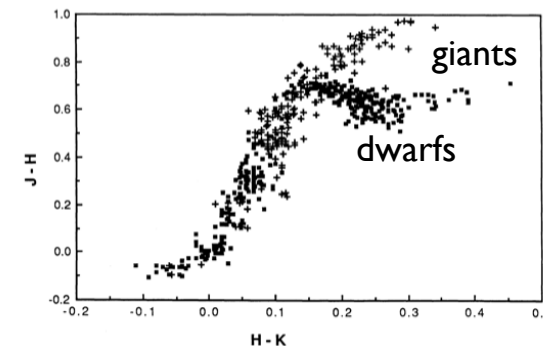
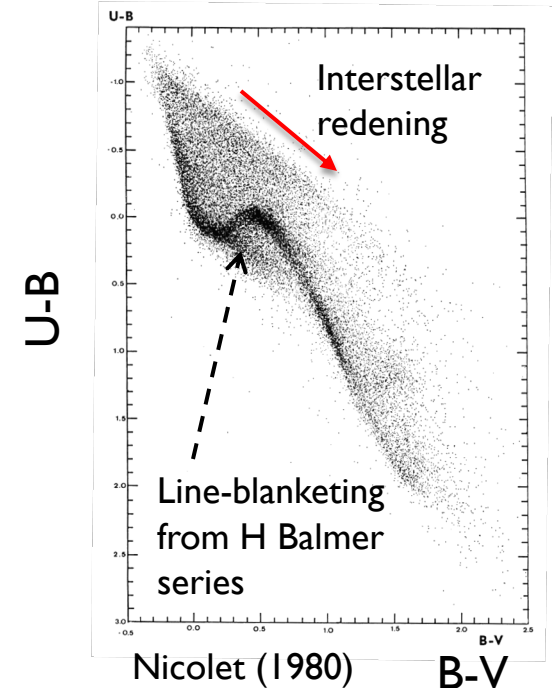
Role of Stars in Extragalactic Astronomy

- ▶ **Dynamics**
 - ▶ Stars are point masses –
 - ▶ collisionless tracers of the potential
 - ▶ Distinctions between stars irrelevant
 - ▶ But, which stars most accurately trace the “true” morphology and dynamics of a galaxy?
- ▶ **Chemical evolution**
 - ▶ Stars are responsible for producing and distributing the elements
- ▶ **Metric of evolution**
 - ▶ Star formation rate (SFR)
 - ▶ Star formation history (SFH)
 - ▶ H-R diagram are all diagnostics of evolution
- ▶ **Feedback**
 - ▶ evolution/organization of ISM in galaxies driven by gravity, hydrodynamics, and input of energy from stars



Stellar Classification

- ▶ **Photometry** : Based on optical and near-infrared (NIR) colors
 - ▶ First order: stars are blackbodies, so any two flux-points constrain temperature
 - ▶ Combination of two bands yield “color” = temperature
 - ▶ Second-order: stars have line-blanketing, so e.g., colors are degenerate for massive stars
 - ▶ Need observations in at least three bands.
 - ▶ NIR can break degeneracy between cool giants and dwarfs.
- ▶ **Spectroscopy** : individual line ratios very tightly constrain temperature, surface gravity, etc.
 - ▶ Yields the OBAFGKM classification
 - ▶ Further sub-classification is the luminosity class

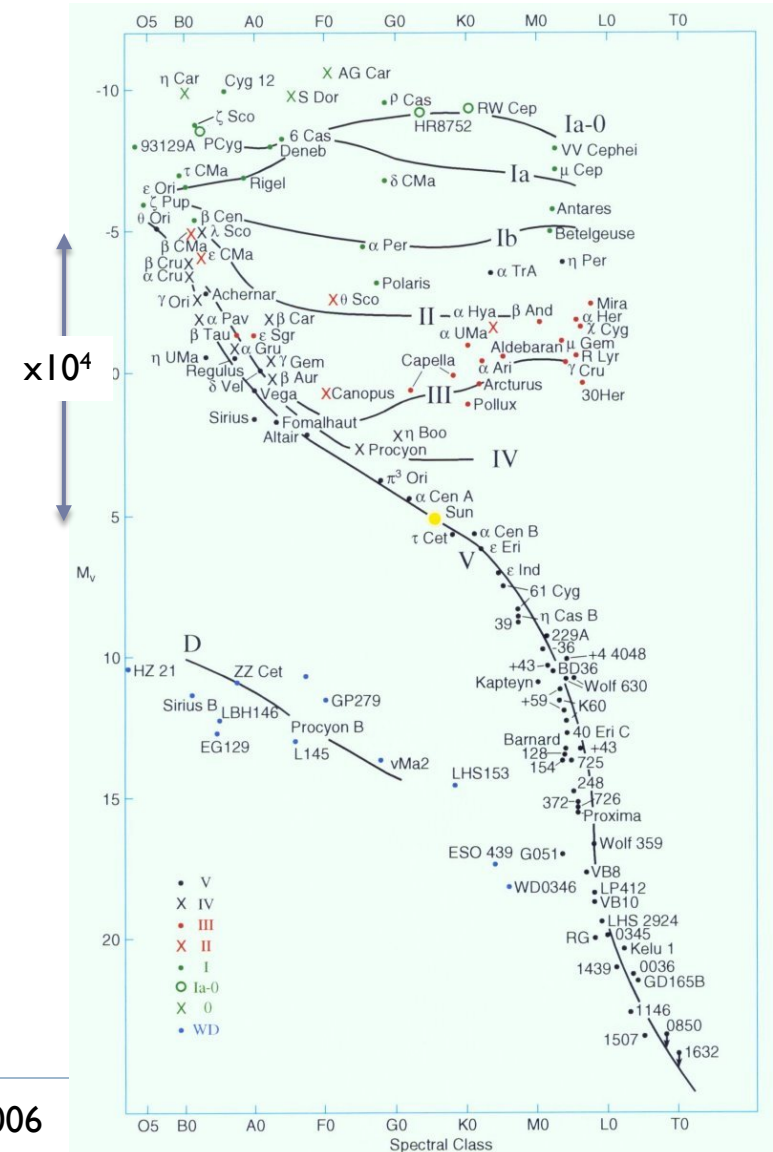


Bessell & Brett (1988)

Basic Properties of Stars

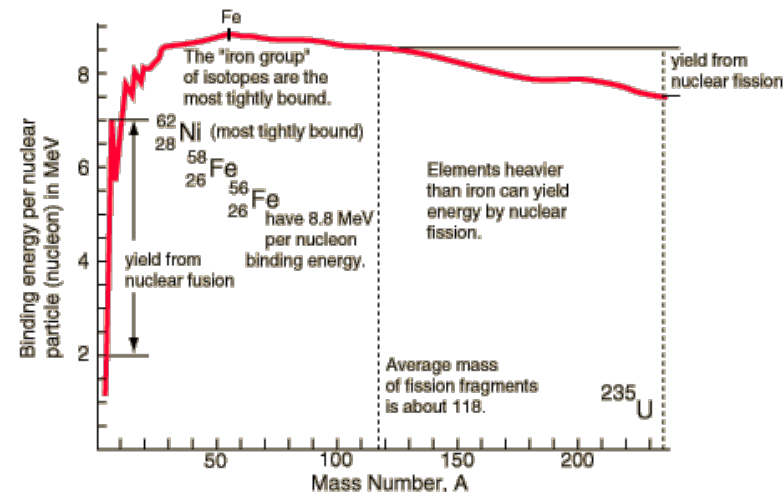
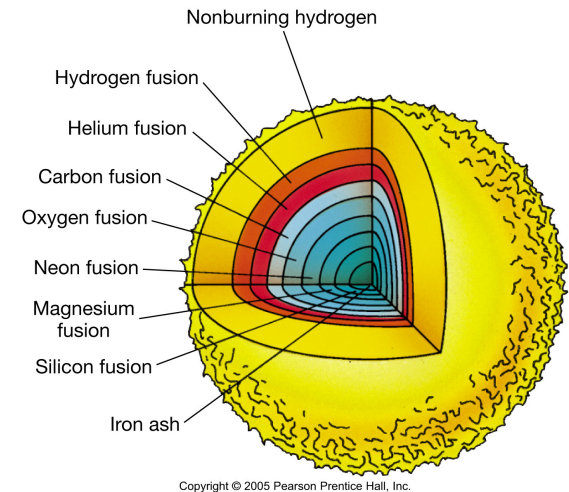
Spec. type	Absorption lines	T_{eff} (K)	M_v (V, I)	(B-V)
O	He II, C III	40-50,000	-6,-8	<-0.33
B	He I, S III, H	12-30,000	-1.5, -7	-0.2
A	H, Mg II	7-9,000	1.0, -7	0
F	Ca II	6-7,000	3.0,-7	0.4
G	Ca II, CH	5.5-6,000	5.0,-7	0.6
K	CH, CN	4-5,500	6.0,-7	1.2
M	TiO	2.5-4000	9.0,-7	1.6

- Luminosity class
- ▶ Ia – most extreme supergiants
 - ▶ Ia – moderate supergiants
 - ▶ Ib – less luminous supergiants
 - ▶ II – bright giants
 - ▶ III – normal giants
 - ▶ IV – subgiants
 - ▶ V - dwarfs



Fundamentals of Stellar Evolution

- ▶ History: BBNS cannot account for the abundances of all the elements; Burbidge, Burbidge, Fowler, & Hoyle laid out the model for stellar nucleosynthesis.
- ▶ Main sequence: H to He fusion via proton-proton chain & CNO bi-cycle
- ▶ Post-MS: H depletion in core, interior pressure decreases, collapse of core and interior, H shell burning ignites, envelope expands and star becomes a red giant.
- ▶ Later phases: repeat with heavier and heavier elements via α -processes, faster and faster rates (more energy production per unit time), more and more shells.
- ▶ Fusion ends depending on mass sufficient to overcome core degeneracy, or when core burns to Fe.



MS Stellar Lifetimes

- ▶ Because H burning lifetime depends on mass there is a nice correlation between turn-off mass and age
 - ▶ Spectral types are determined by surface-temperature (T_{eff})
 - ▶ T_{eff} set by mass *on the main sequence*:
 - ▶ more mass burns brighter and hotter
- ▶ $L_{\text{MS}}/L_{\odot} \sim (M/M_{\odot})^{2.14} \quad (M/M_{\odot} > 20)$
- ▶ $L_{\text{MS}}/L_{\odot} \sim (M/M_{\odot})^{3.5} \quad (2 < M/M_{\odot} < 20)$
- ▶ $L_{\text{MS}}/L_{\odot} \sim (M/M_{\odot})^{4.8} \quad (M/M_{\odot} < 2)$

$$\text{So: } \tau_{\text{MS}} = 10 (M/M_{\odot})(L/L_{\odot})^{-1} \text{ Gyr}$$



Stellar Lifetimes through core He-burning

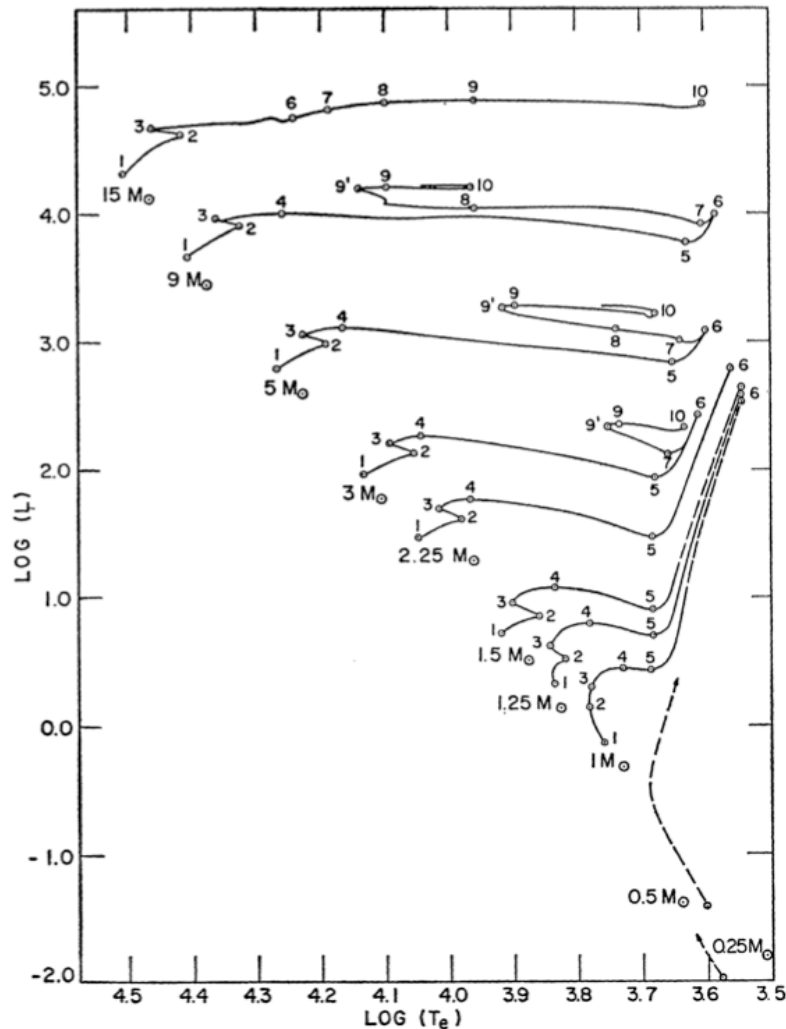


TABLE III
STELLAR LIFETIMES (yr)*

Interval (i-j)	(1-2)	(2-3)	(3-4)	(4-5)	(5-6)
Mass (M_{\odot})					
15	1.010 (7)	2.270 (5)		7.55 (4)	
9	2.144 (7)	6.053 (5)	9.113 (4)	1.477 (5)	6.552 (4)
5	6.547 (7)	2.173 (6)	1.372 (6)	7.532 (5)	4.857 (5)
3	2.212 (8)	1.042 (7)	1.033 (7)	4.505 (6)	4.238 (6)
2.25	4.802 (8)	1.647 (7)	3.696 (7)	1.310 (7)	3.829 (7)
1.5	1.553 (9)	8.10 (7)	3.490 (8)	1.049 (8)	≥ 2 (8)
1.25	2.803 (9)	1.824 (8)	1.045 (9)	1.463 (8)	≥ 4 (8)
1.0	7 (9)	2 (9)	1.20 (9)	1.57 (8)	≥ 1 (9)

* Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.

TABLE IV
STELLAR LIFETIMES (yr)*

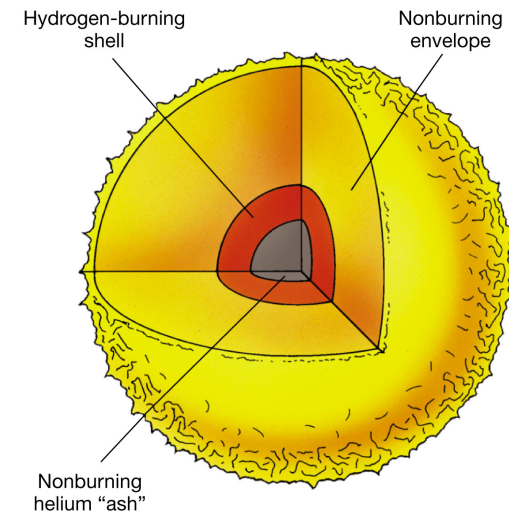
Interval (i-j)	(6-7)	(7-8)	(8-9)	(9-10)
Mass (M_{\odot})				
15	7.17 (5)	6.20 (5)	1.9 (5)	3.5 (4)
9	4.90 (5)	9.50 (4)	3.28 (6)	1.55 (5)
5	6.05 (6)	1.02 (6)	9.00 (6)	9.30 (5)
3	2.51 (7)		4.08 (7)	6.00 (6)

* Numbers in parentheses beside each entry give the power of ten to which that entry is to be raised.

- Note changing morphology with mass in
 - RGB
 - HB
- Wanted: phases later than 6 for $M < 3M_{\odot}$
- Wanted: phases later than 10 for higher mass
- Wanted: modern counterparts

Post-MS Stellar Evolution

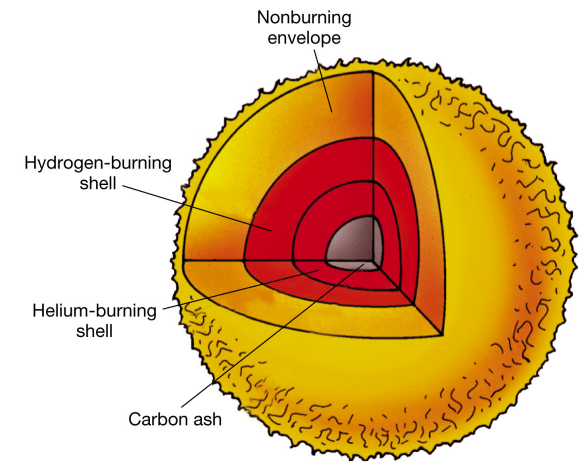
- ▶ RGB to Horizontal Branch (HB)
 - ▶ Core contraction/core mass increases
 - ▶ $T \sim 10^8$ K, $\rho \sim 10^4$ g cm⁻³ get He burning
 - ▶ $2\alpha \rightarrow {}^8\text{Be}, {}^8\text{Be} + \alpha \rightarrow {}^{12}\text{C}$
 - ▶ In stars w/ $M > 2M_{\odot}$, its not degenerate and we get core expansion
 - ▶ Essentially a He-burning main sequence
 - ▶ In more massive stars get ${}^{12}\text{C} + \alpha \rightarrow {}^{16}\text{O}$; for stars with M up to $8 M_{\odot}$ we're left with a degenerate CO core (white dwarf)
 - ▶ He-burning lifetime $\sim 10^8$ years
- ▶ Evolution to Asymptotic Giant Branch ($M > 0.8 M_{\odot}$) – *you are going to check this*
- ▶ Further Burning Stages...



Fundamentals of Stellar Evolution

► Evolution to AGB

- He-burning, growing CO core
 - Low mass stars can't lift degeneracy, end up as planetary nebula + white dwarf
- Eventually get He shell burning that drives expansion of envelope and luminosity increases (plus unburned H, H shell burning)
 - Occurs with a series of “dredge-ups” that produce chemically bizarre stars (convection)
 - Site of “s-process” nucleosynthesis

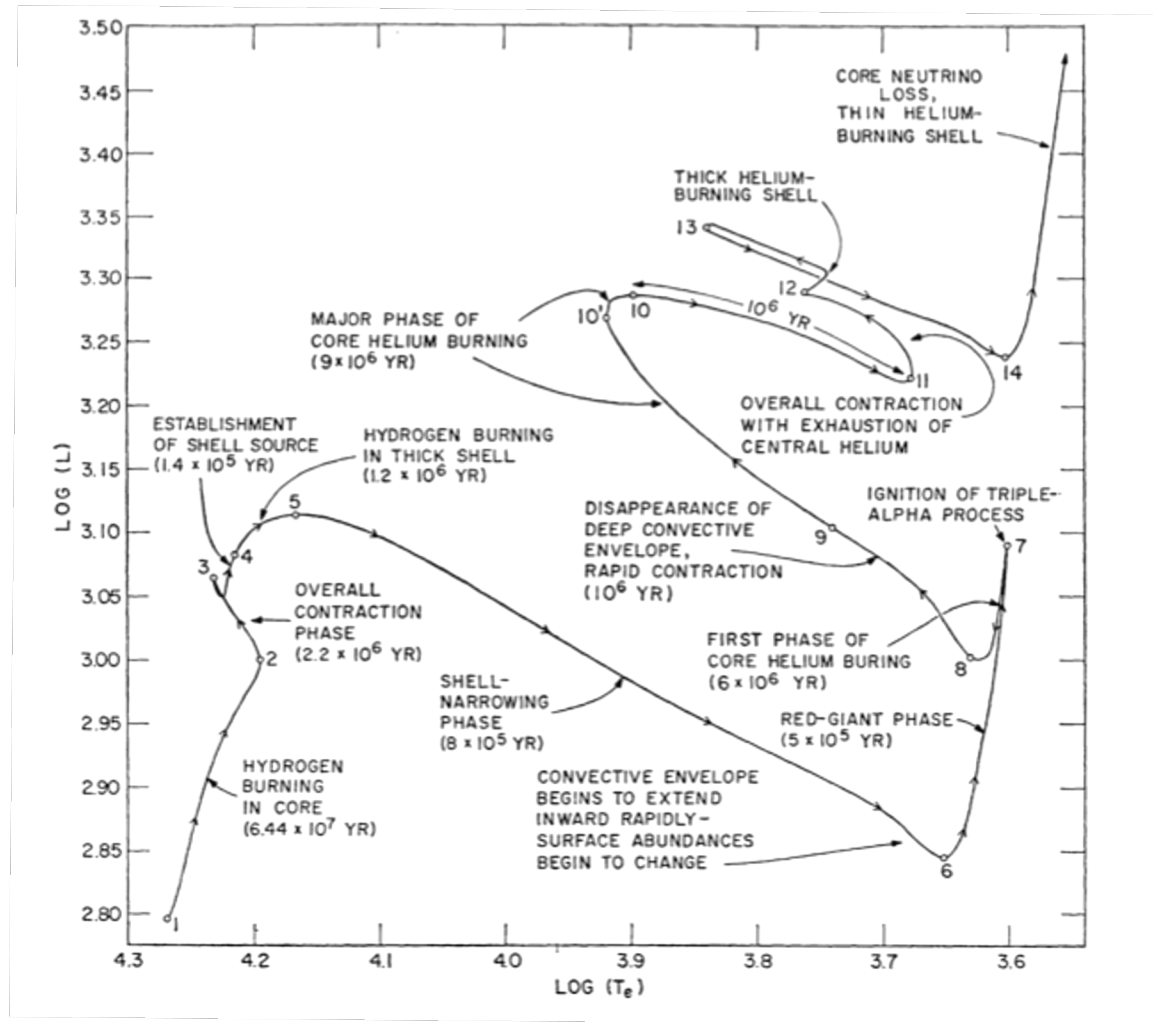


► Neutron capture processes

- S-process (“slow”) – yields elements like Ba and Tc largely in AGB stars (all those free n from previous burning processes)
- R-process (“rapid”) – yields very heavy elements like Ur, usually in SNe

Path of 5 M_⊙ metal-rich star

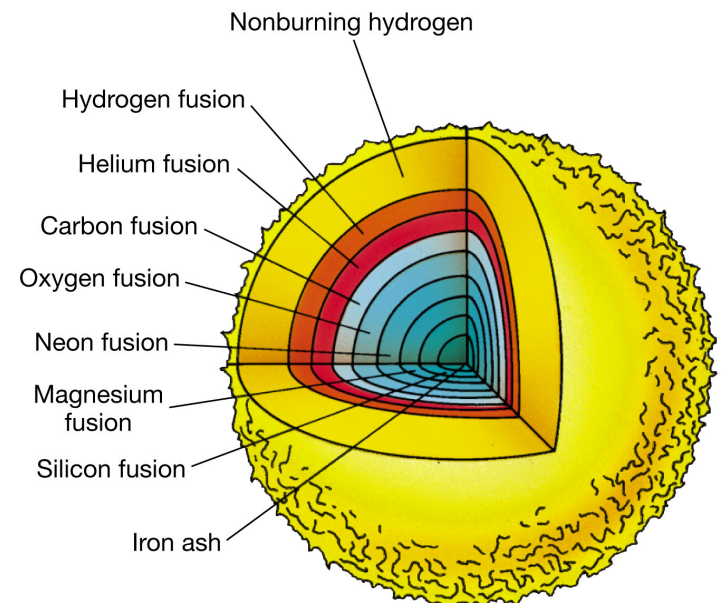
$$L_{\odot} = 3.86 \times 10^{33} \text{ erg/s}$$



Fundamentals of Stellar Evolution

► Further Burning Stages ($M > 8M_{\odot}$)

- $^{12}\text{C} + ^{12}\text{C} \rightarrow ^{20}\text{Ne} + \alpha$
- $^{16}\text{O} + ^{16}\text{O} \rightarrow ^{28}\text{Si} + \alpha$
- $^{20}\text{Ne} + ^4\text{He} \rightarrow ^{24}\text{Mg} + \gamma$
- Leads ultimately to the production of ^{56}Fe , core collapse, and supernova explosion (Type II SNe)
- Can also get n production via, e.g.,
 $^{12}\text{C} + ^{12}\text{C} \rightarrow ^{23}\text{Na} + \text{n}$



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Modern evolutionary tracks

- ▶ A few links:

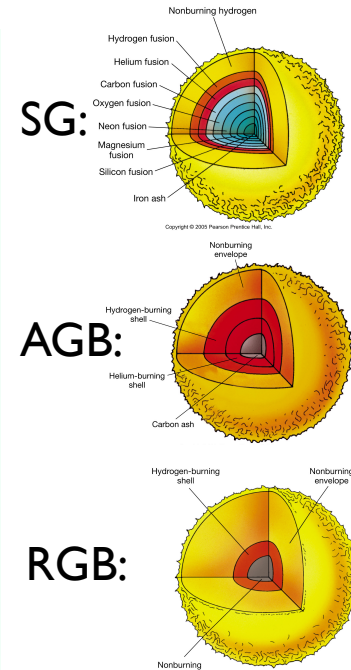
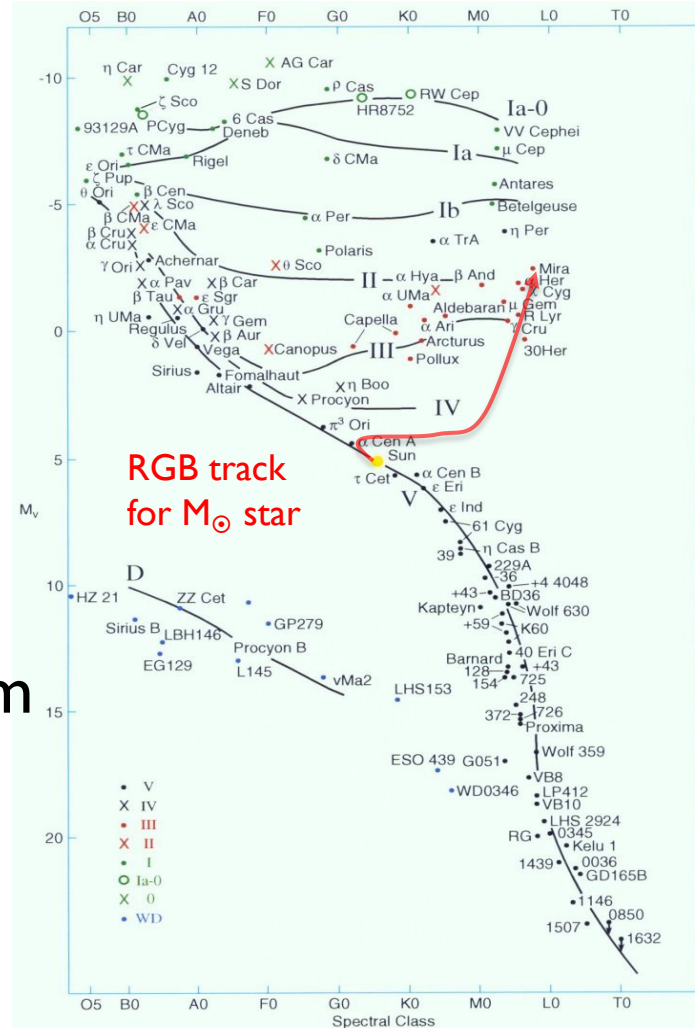
- ▶ Awesome web tool by our very own RICH TOWNSEND:
 - ▶ <http://www.astro.wisc.edu/~townsend/static.php?ref=ez-web-movie>
- ▶ Two other very nice tools for exploring evolution of individual stars:
 - ▶ <http://stellar.dartmouth.edu/models/>
 - ▶ <http://astro.u-strasbg.fr/~koppen/starpop/StellarEvolution.html>
- ▶ Watch a simple stellar population (SSP) evolve in the HR diagram:
 - ▶ <http://www.kitp.ucsb.edu/~paxton/extras/movie10K.mpg>
- ▶ Where to go to build your own stellar population synthesis (SPS) code:
 - ▶ <http://stev.oapd.inaf.it/cgi-bin/cmd>
 - ▶ <http://www.astro.yale.edu/demarque/yystar.html> -- for old populations
 - ▶ <http://iopscience.iop.org/article/10.3847/0004-637X/823/2/102/pdf>

- ▶ **Your assignment:**

- ▶ Explore the above.
- ▶ What is the lower mass-limit for core He burning?
 - ▶ what happens after Iben's #6 for $M < 3M_{\odot}$?
- ▶ What is the lower mass-limit for core-burning beyond He?
 - ▶ How long-lived and luminous are these phases?

Summary

- ▶ **Stellar types:**
 - ▶ Classification – photometry & spectroscopy
 - ▶ τ_{MS}
- ▶ **Stellar evolution:**
- ▶ **Burning phases**
- ▶ **Paths in the HR diagram (tracks)**
- ▶ **Elemental yields**
- ▶ **Metrics of evolution**



Understanding Stellar Populations

- ▶ Color – temperature – mass – lifetime relationships mean the observed “color-magnitude” diagram (CMD) can tell us something about the age/evolutionary status of a stellar population (especially if it’s a single age)
- ▶ CMD can also hint at the production of metals

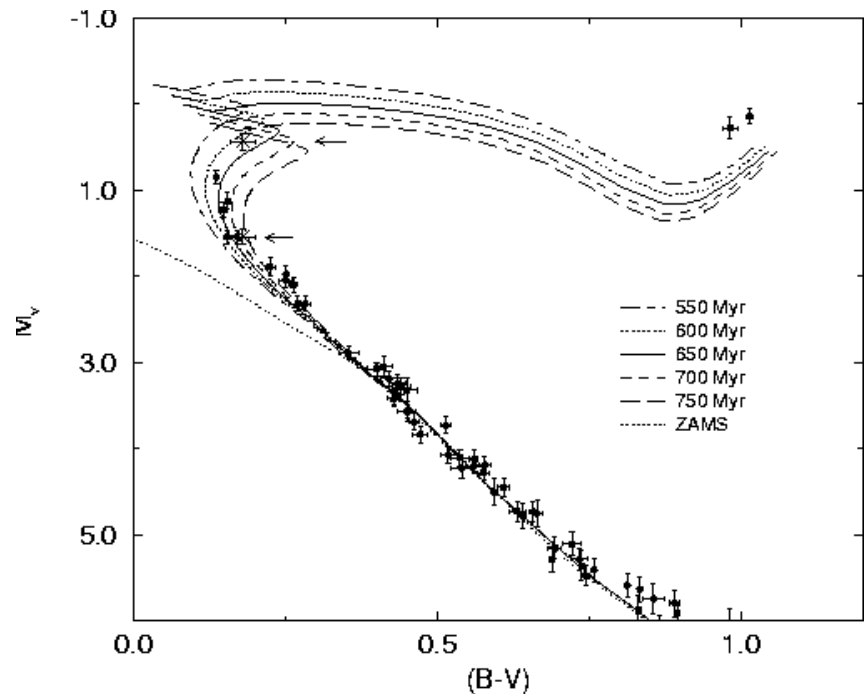


H-R Diagrams

- ▶ Stars spend most of their lives on the “main sequence”
- ▶ “turn-off” age is primary indicator of the age of a stellar population



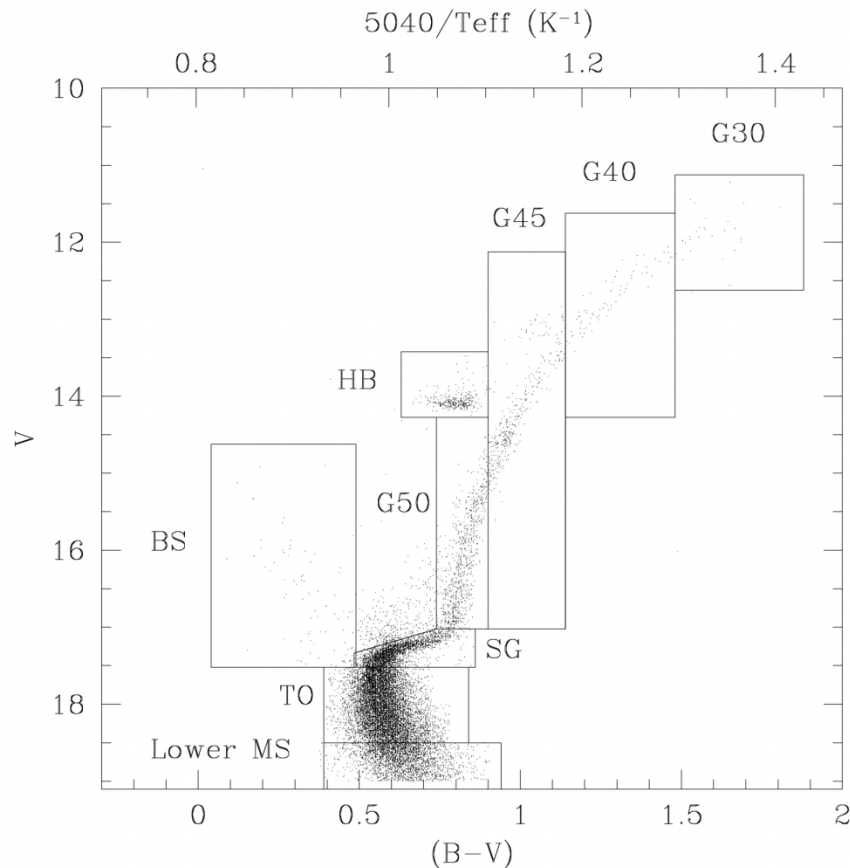
Aldebaran – not part of cluster



Hyades open cluster; Perryman et al. 1998

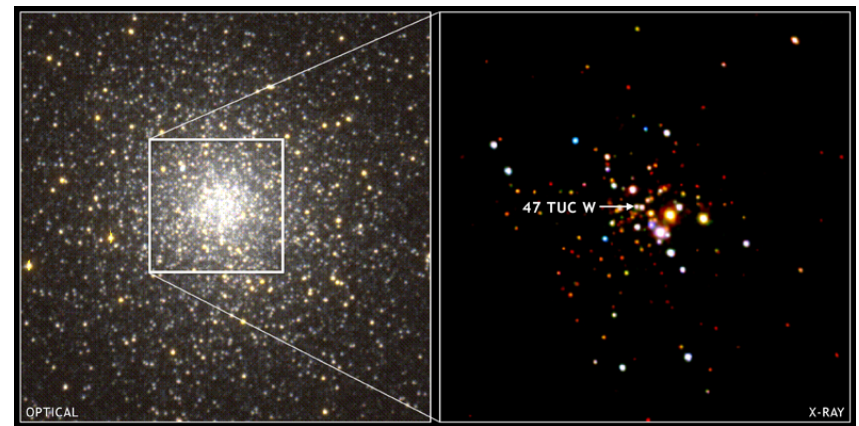
ZAMS = zero-age main sequence

H-R Diagrams *continued*

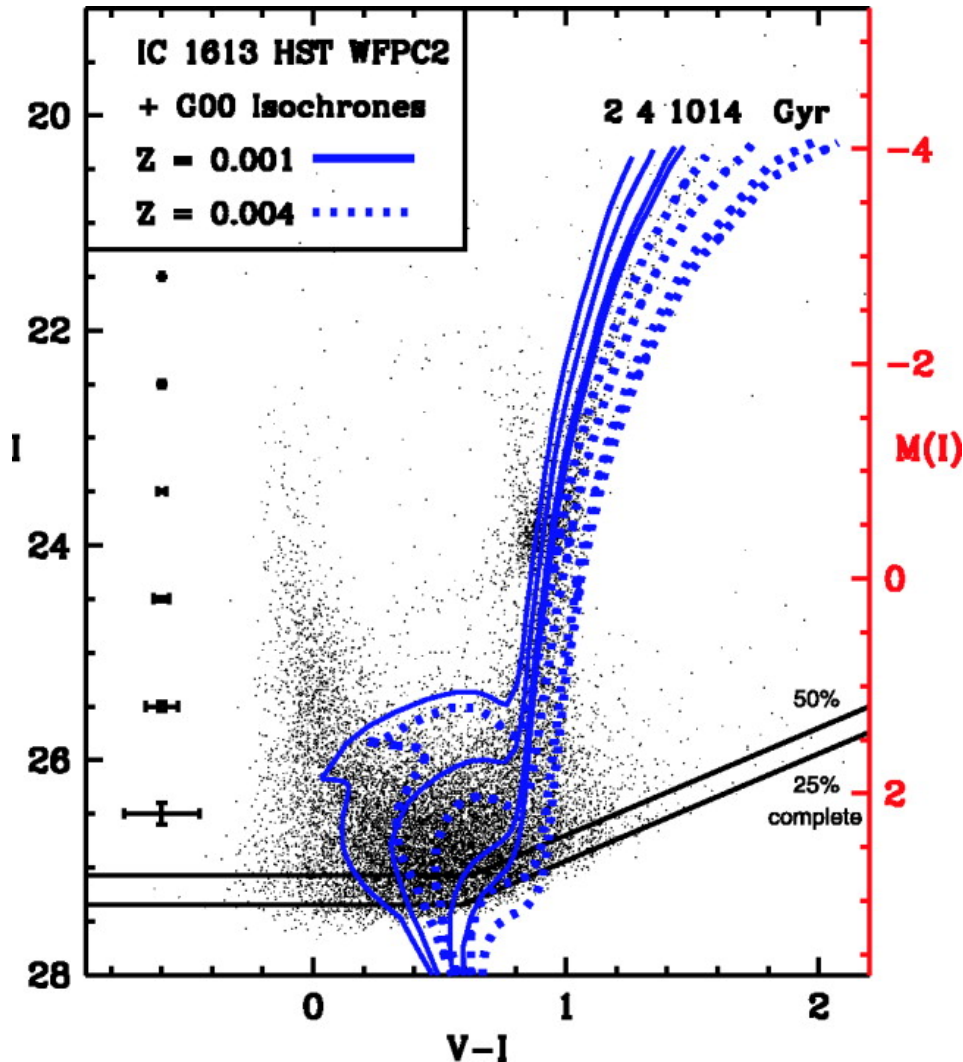


Globular cluster 47 Tuc
(Edmonds et al. 2002)

- ▶ Tracing evolution of a stellar population
- ▶ $(B-V) \rightarrow$ temperature
- ▶ $V \rightarrow$ luminosity



H-R Diagrams *continued*

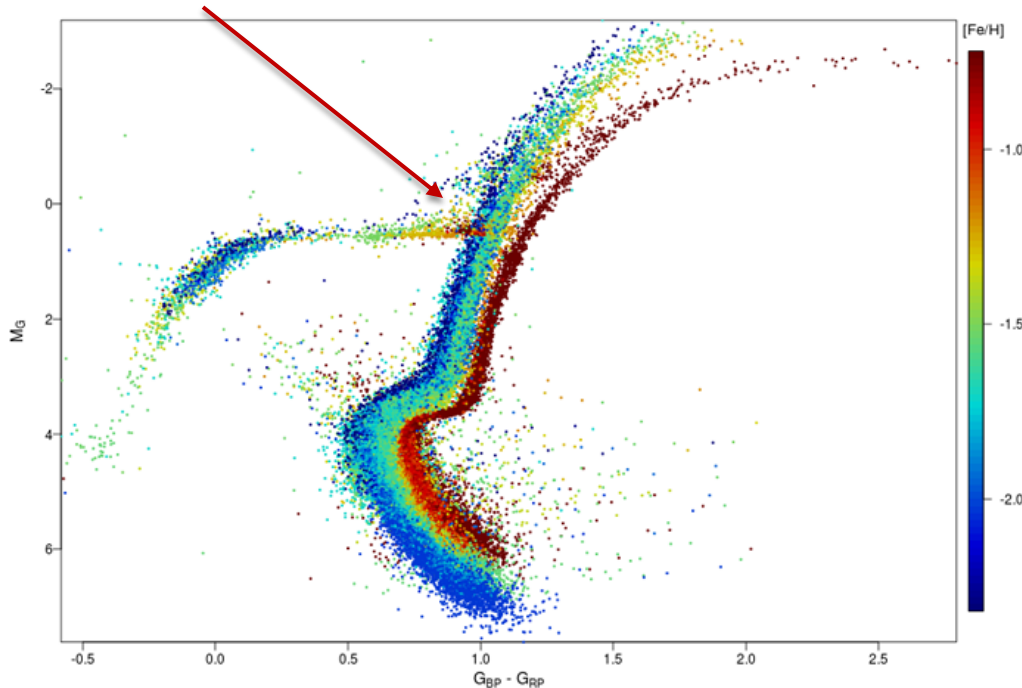


- ▶ Gets more complicated with a mixed-age stellar population
- ▶ Multiple turn-offs, multiple HBs
- ▶ Dwarf spheroidal galaxies are ideal labs for this

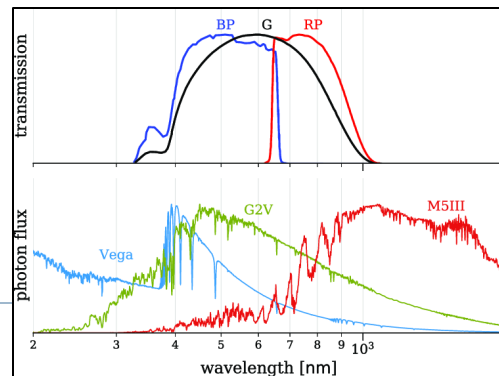
H-R Diagrams *continued*

Red clump appears above $[\text{Fe}/\text{H}] \sim -1.25$

Absolute Magnitude



Blue-Red color



- ▶ Metallicity drives shifts in giant branch and turn-off location in HRD due to changes in line-opacity
- ▶ It also changes the Horizontal Branch morphology
- ▶ Gaia DR2
- ▶ 14 globular clusters

Statistical Stellar Astrophysics

▶ Stellar initial mass function

- ▶ $dN = N_0 \xi(M) dM$
- ▶ $N_0 \int dM M \xi(M) = \text{total mass of burst/episode}$
- ▶ Observationally: $\xi(M)$ goes as $(M/M_\odot)^{-2.35}$
 - ▶ “Salpeter IMF”
 - ▶ Slight variation with mass (time? environment?), according to some
 - ▶ Upper mass limit in the 80-120 M_\odot
 - but note small-number statistics become important
 - ▶ Turn-over likely below 0.1 M_\odot
 - ▶ Other estimates of the IMF:
 - Miller-Scalo
 - Chabrier *
 - diet-Salpeter
 - Kroupa *
 - bimodal (e.g., Larson)

Stellar Populations

▶ Integrated Colors

- ▶ Population I – “Disk Population” – open clusters, circular orbits, confined to a disk, “blue”
- ▶ Population II – “Halo Population” – globular clusters, large random velocities, elliptical orbits, spherical distribution, “red”
- ▶ Population III – extremely metal poor, not yet detected
 - ▶ Cosmic Mystery #2: Where are the Pop-III stars?

▶ Correlations

- ▶ Color vs kinematics
 - ▶ Blue stars are disk-like
- ▶ Color vs metallicity
 - ▶ Red stellar populations tend to be metal poor, strong Galactic correlation between kinematics and metallicity

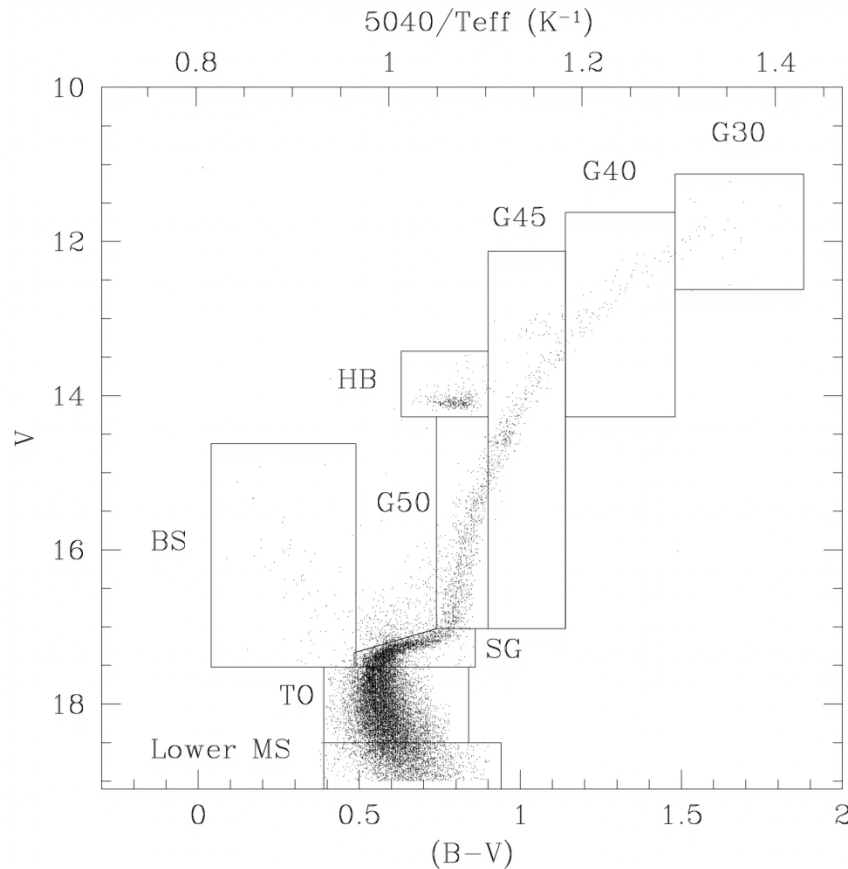


Interpreting CMDs

- ▶ Density of any locale on a CMD is a function of IMF, SFR, mass, and age
 - ▶ $C(M_V, V-I) = \iint \xi(\log m, t) \times \text{SFR}(t) dt d\log m$
 - ▶ Small mass bin (i.e. single mass)
 - ▶ Constant IMF (ξ)
 - ▶ Can recover star formation history from a complex CMD
- ▶ **Statistical Approach**
 - ▶ What is the probability that a certain distribution of points on the CMD came from one particular set of stellar evolution models (Tolstoy & Saha 1996)



HR Diagrams revisited

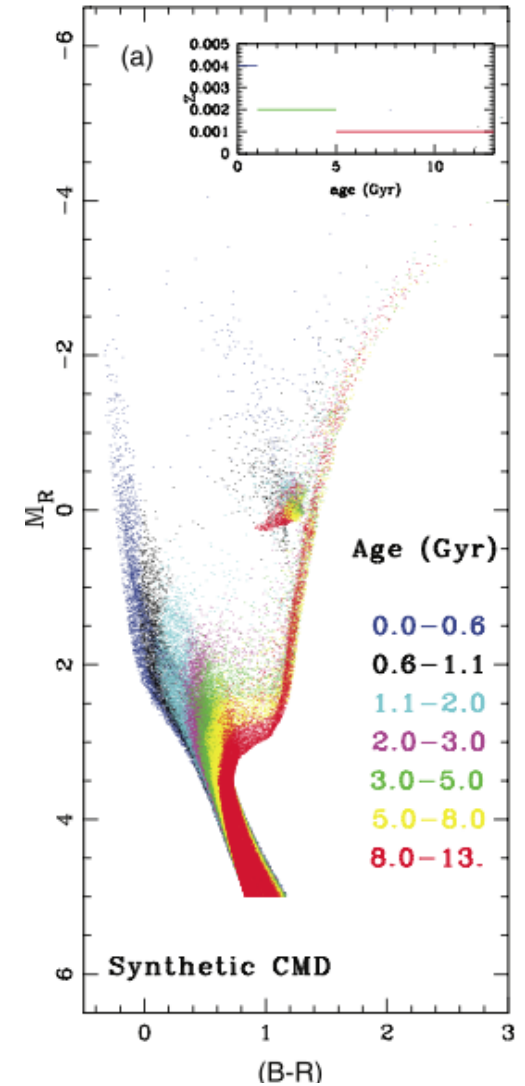
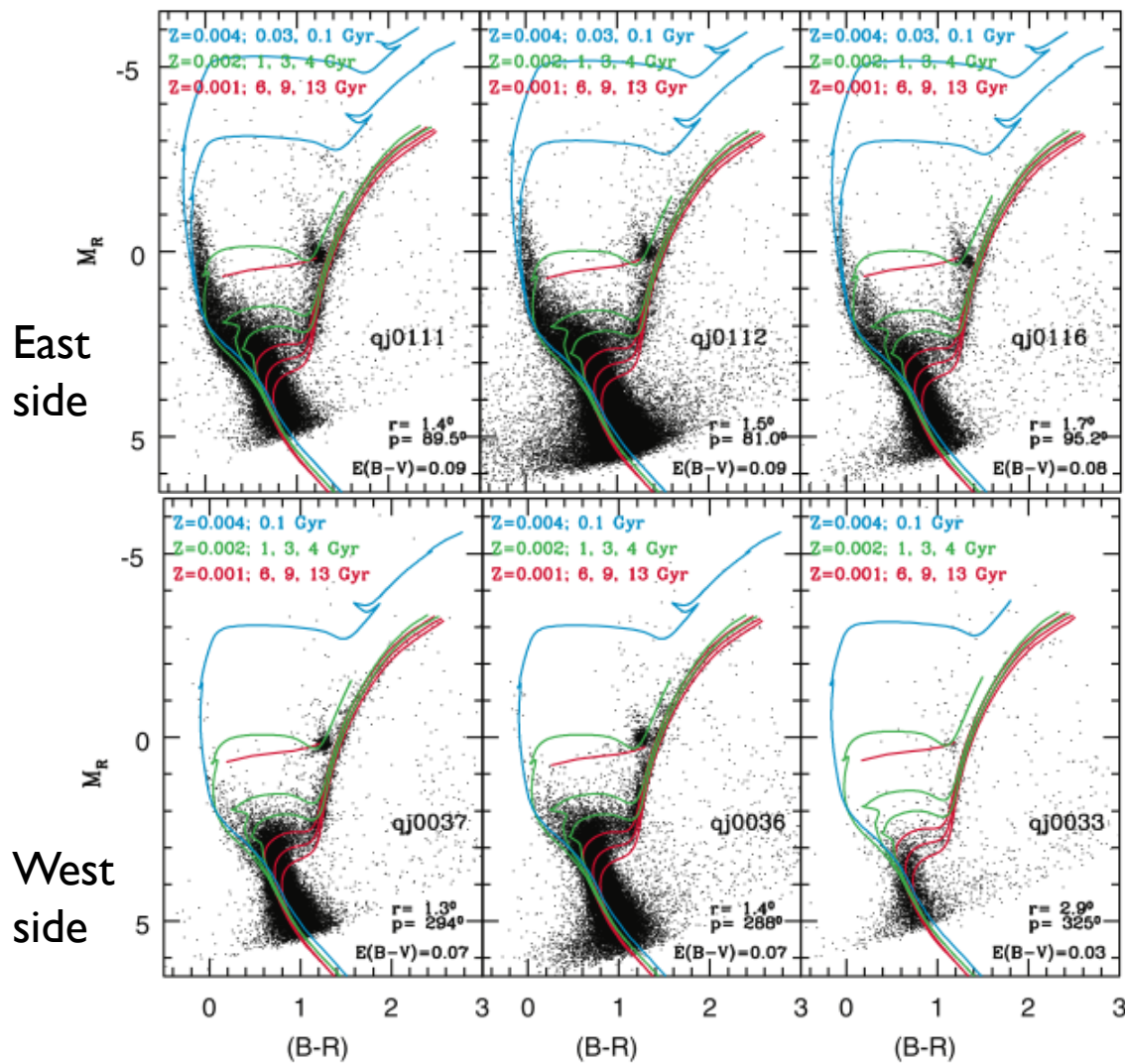


H-R diagram for 47 Tuc

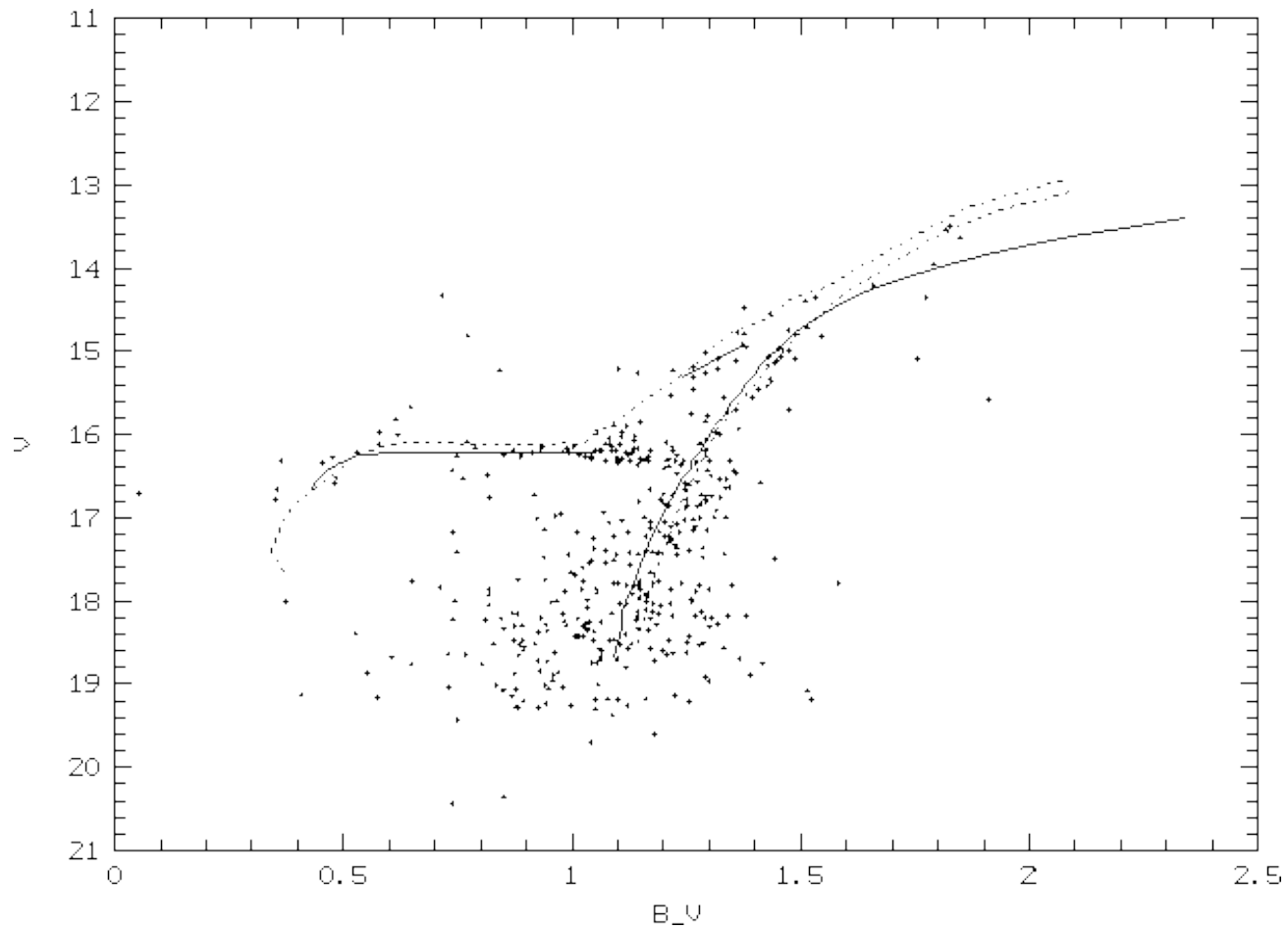
$[\text{Fe}/\text{H}] = -0.75$

- ▶ Evolution + nucleosynthesis – each box is a different burning stage
- ▶ Could you sketch the H-R diagram of this cluster and label all of the major burning stages?

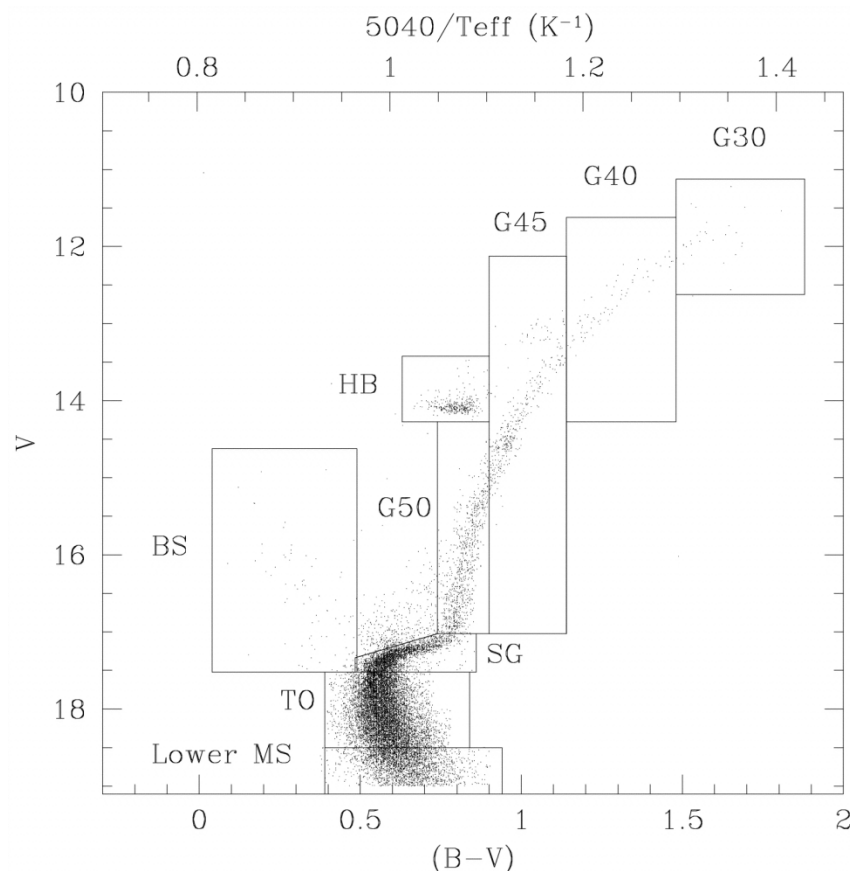
SMC: Noel et al. 2007



How old is this cluster? Why?



Summary: stellar populations



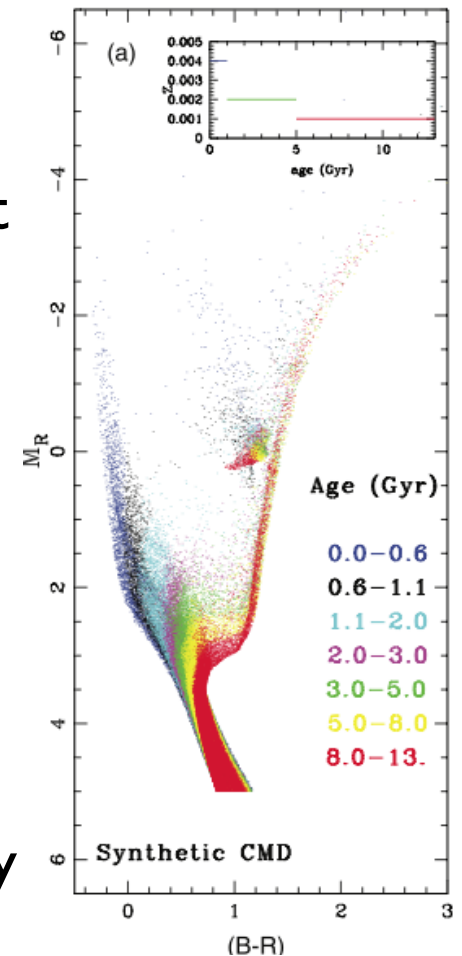
H-R diagram for 47 Tuc

[Fe/H] = -0.75

- ▶ Evolution + nucleosynthesis – each box is a different burning stage
- ▶ Density of any locale on a CMD is a function of IMF, SFR, mass, and age
 - ▶ $C(M_V, V-I) = \iint \xi(\log m, t) \times \text{SFR}(t) dt d\log m$
 - ▶ Constant IMF (ξ)
 - ▶ Can recover star formation history from a complex CMD
- ▶ Statistical Approach
 - ▶ Probability distribution of points on the CMD from one particular set of stellar evolution models (Tolstoy & Saha 1996)
- ▶ Stellar initial mass function
 - ▶ $dN = N_0 \xi(M) dM$
 - ▶ $N_0 \int dM M \xi(M) = \text{total mass}$
 - ▶ Observationally: $\xi(M)$ goes as $(M/M_\odot)^{-2.35}$
 - ▶ Upper mass limit in the 80-120 M_\odot
 - ▶ Turn-over likely below 0.1 M_\odot

Questions to answer:

- ▶ What is the fraction of the total integrated luminosity of a stellar population as a function of the limiting stellar absolute magnitude (i.e., the integral of all stars brighter than some limit compared to the total integral).
 - ▶ How does this depend on wavelength, population age (star-formation history) and metallicity?
 - ▶ How can you estimate this crudely but easily?
 - ▶ How can you estimate this more precisely?
 - ▶ Are there tools already available?
- ▶ What are the resolution limits in ground or space-based imaging in the MW, Local Group galaxies (e.g., LMC, SMC, M31, M33) and nearby galaxies outside the LG?



To get you started:

- ▶ Analytic solution:
 - ▶ IMF, MS lifetime, M-L relations
- ▶ Trilegal (Girard+2005,2016)
 - ▶ <http://stev.oapd.inaf.it/cgi-bin/cmd>
 - ▶ <http://stev.oapd.inaf.it/cgi-bin/trilegal>
- ▶ Dartmouth
 - ▶ <http://stellar.dartmouth.edu/models/>
- ▶ MATCH (Dolphin 2002; see also Beerman+2012, Weisz+2015, Lewis+2015)
- ▶ IAC-STAR (Aparacio & Gallart 2004; Gallart+2005, Pietrinferni+04)
- ▶ Noel+2007
- ▶ Dalcanton+ 2012a,b, Williams+2015



Stellar Population Synthesis (SPS)

▶ Key ingredients

▶ IMF(t, ρ, Z)

▶ SFR($t; R, \theta, \varphi$)

▶ Isochrones (theoretical HR diagram)

▶ Stellar library with parameters ($\log g, T_e, Z, A$) to map to HR

▶ Chemical evolution: $Z(t; R, \theta, \varphi), A(t; R, \theta, \varphi)$

▶ Density evolution: $\rho(t; R, \theta, \varphi)$

▶ or whatever else the IMF depends on, e.g., turbulence, magnetic fields

▶ Dynamical diffusion rate

▶ Resonant scattering (e.g., radial migration)

Z = metallicity, e.g., Fe/H

'Metals' are anything heavier than He

A = abundance, i.e., any metal relative to Fe
(R, θ, φ) = spatial cell in a galaxy

If you want to know what stars you should expect to find at some time in some cell of the galaxy (R, θ, φ) then you need the ingredients in red; these are beyond most SPS models, but are explored in various types of numerical models that explore galaxy formation and evolution.

SPS and the Fuel Consumption Theorem

► Fuel Consumption theorem (FCT)

- The relative *bolometric* contribution of stars (L_j) in any evolutionary phase (j) is equal to the relative amount of fuel (F_j) that each evolving star burns during that phase

$$L_j/L_T = \sim 9.75 \times 10^{10} B(t) F_j,$$

↑
Total (integrated) luminosity

Number of stars in any post-main sequence stage of duration t_j :

$$N_j = B(t) L_T t_j,$$

← Amount of fuel burned by stars of turn-off mass $M_{TO}(t)$:

$$F_j = \Delta M_j^H + 0.1 \Delta M_j^{He}$$

↑
He fusion liberates only 10% energy per unit mass compared to H

← Death-rate per unit luminosity, i.e., the specific evolutionary flux; $B(t)$ ranges from 0.5×10^{-11} to 2×10^{-11} stars per year per L as age increases from 10^7 to 10^{10} yr

Fuel-consumption *continued*

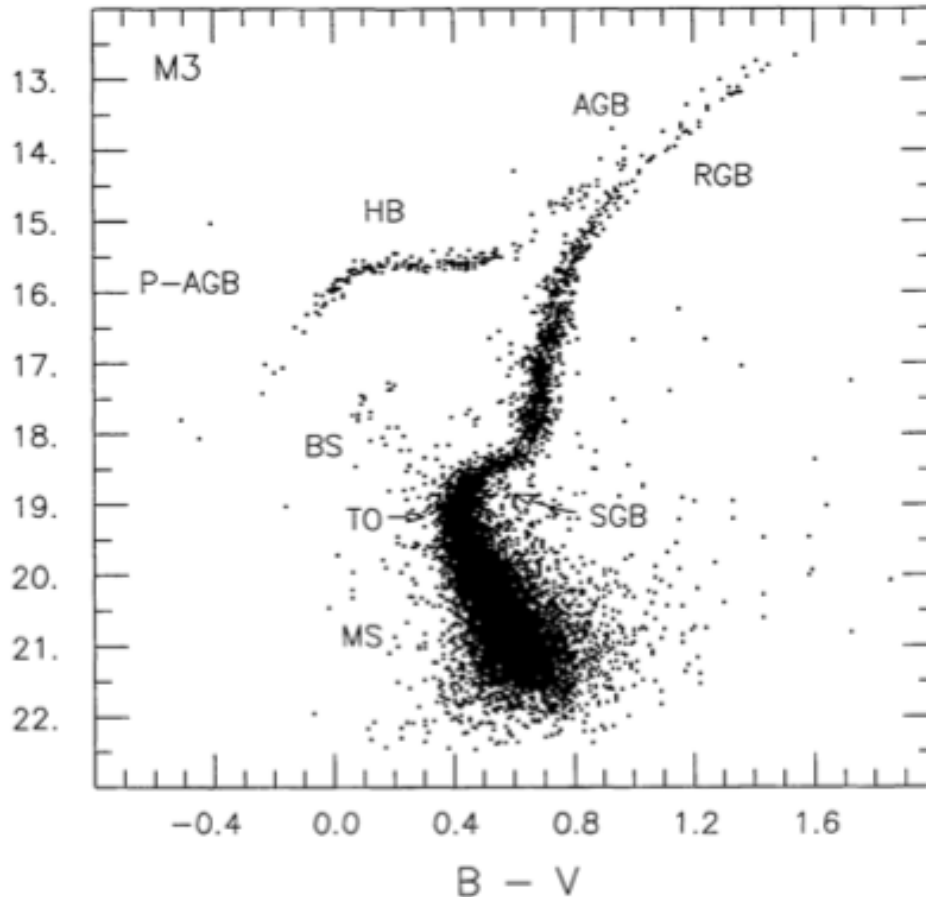
- ▶ FCT particularly useful for old stellar populations
 - ▶ For $t \geq 10^{10}$ yr, $B(t) \sim 2.2 \times 10^{-11}$ stars $L_{\odot}^{-1} \text{ yr}^{-1}$

$$\frac{L_j}{L_T} \simeq 2 \times F_j[M_{\text{TO}}(t)] .$$

- ▶ Accurate to about 10%
- ▶ When you don't trust the isochrones FCT is the best solution and always a good sanity check.



Examples: M3 and 47 Tuc



M3: $[\text{Fe}/\text{H}] = -1.34$ to -1.5

47 TUC: $[\text{Fe}/\text{H}] = -0.75$

Figure 1 The CMD of the cluster M3 (Buonanno et al. 1986a, 1987). In this diagram, 10,637 stars are plotted, 9879 from a sample that is complete down to $V = 21.5$ and totals $\sim 30,000 L_{\odot}$ of cluster light, while the remaining 758 stars are drawn from a sample that is complete down to $V = 18$ and totals $\sim 50,000 L_{\odot}$ of cluster light. The stars brighter than $V = 18$ therefore belong to a sample totaling $\sim 80,000 L_{\odot}$ of cluster light ($\sim 30\%$ of the total luminosity of M3). More information on this diagram can be found in Table 2. The following classification has been adopted for the various evolutionary stages: 1. main sequence (MS)—core hydrogen-burning phase; 2. blue stragglers (BS); 3. subgiant branch (SGB)—shell hydrogen-burning phase, from the MS turnoff (TO) to the Hayashi line; 4. red giant branch (RGB)—shell hydrogen-burning phase along the Hayashi line, until helium ignition in the core; 5. horizontal branch (HB)—core helium-burning phase; 6. asymptotic giant branch (AGB)—shell hydrogen- and helium-burning phase; 7. post-AGB (P-AGB)—final evolution from the AGB to the white dwarf (WD) stage.

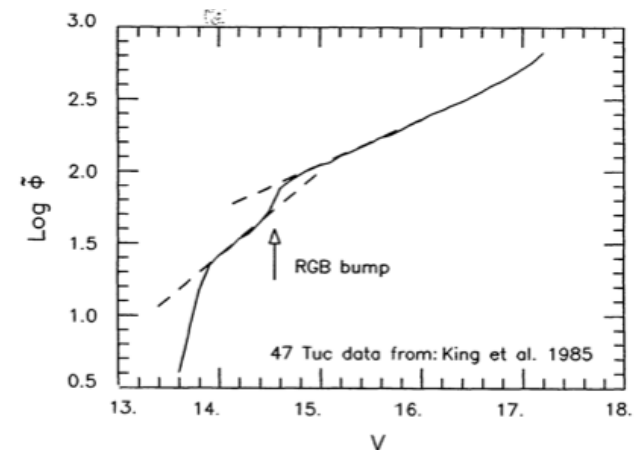
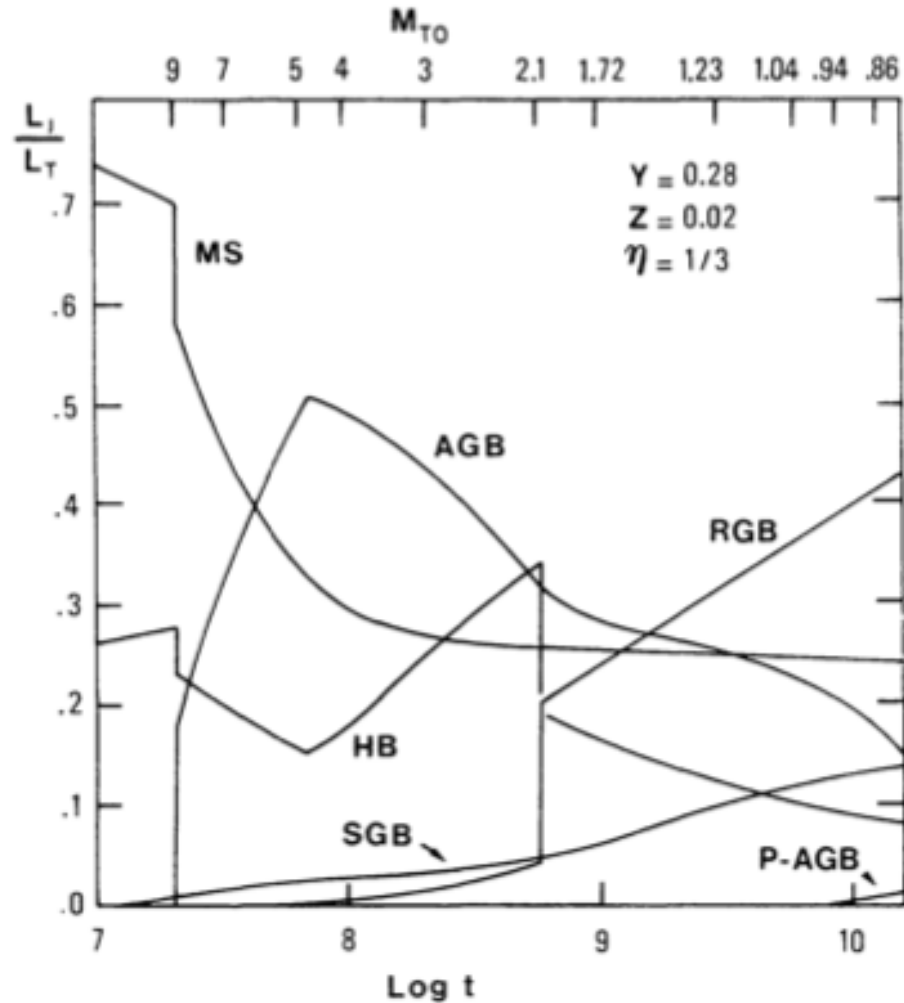


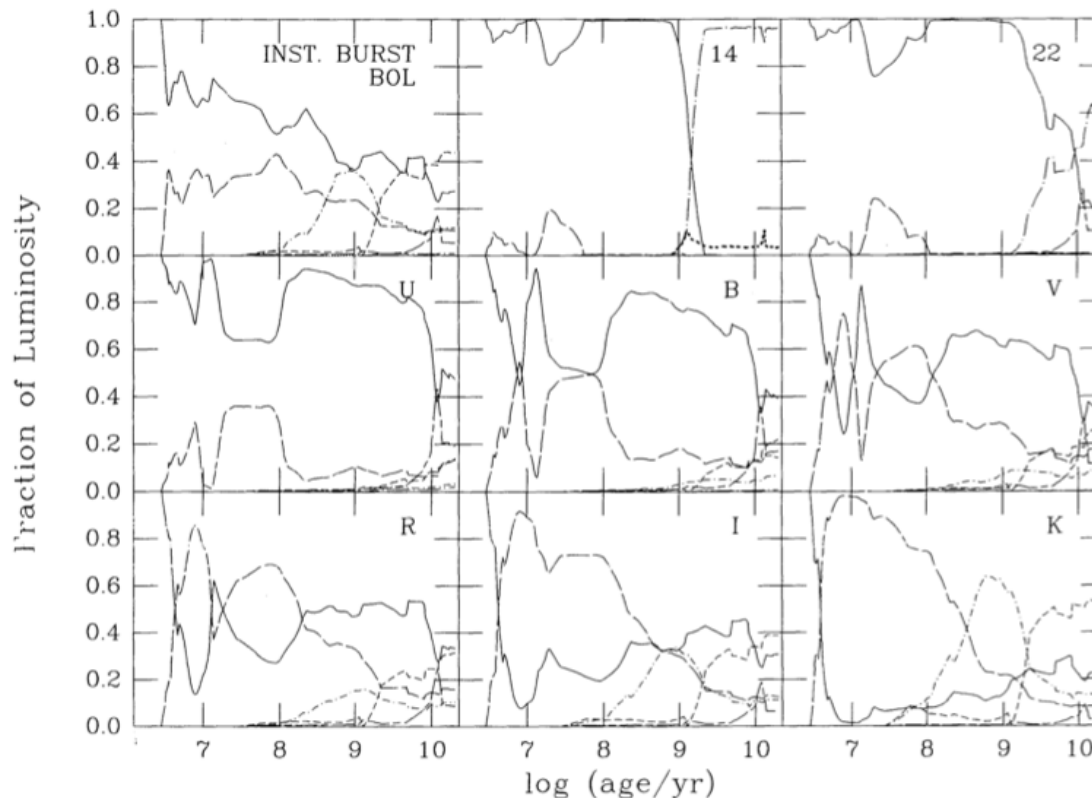
Figure 4 The cumulative luminosity function Φ for the RGB stars of the cluster 47 Tuc, obtained from Figure 4 of King et al. (1985). The RGB bump and the associated change in slope are clearly visible.

Bolometric contributions by time and phase



Contributions by time, phase, and λ

► Updated with modern stellar population synthesis (SPS)



Bruzual & Charlot (1993, *ApJ*, 405, 538)

Bruzual & Charlot (2003, *MNRAS*, 334, 1000)

<http://www.cida.ve/~bruzual/bc2003>

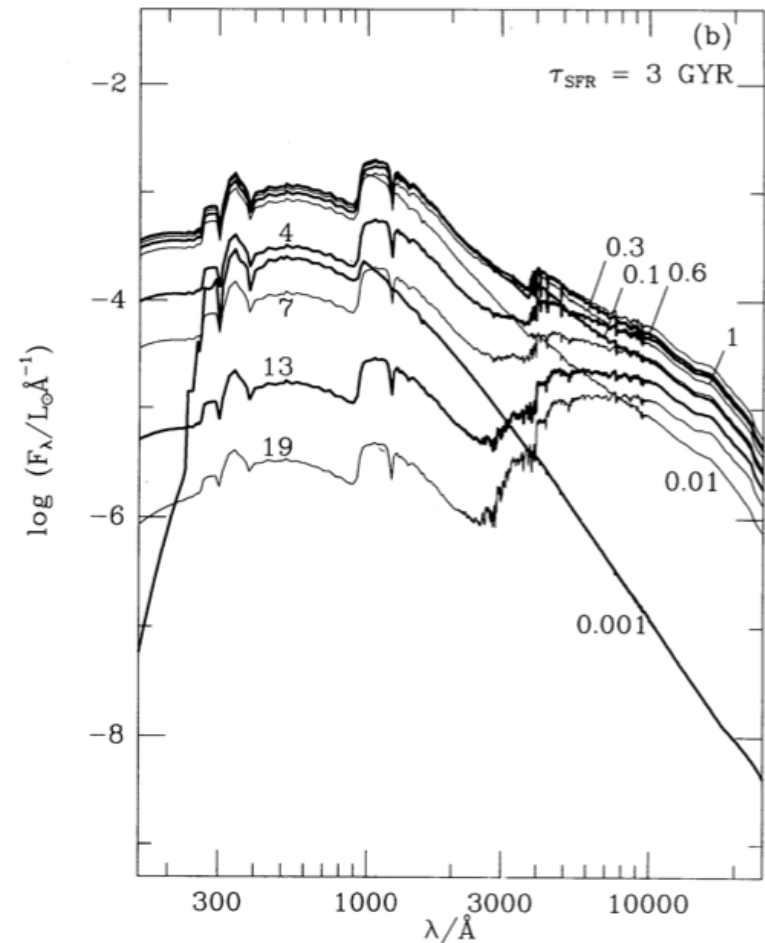
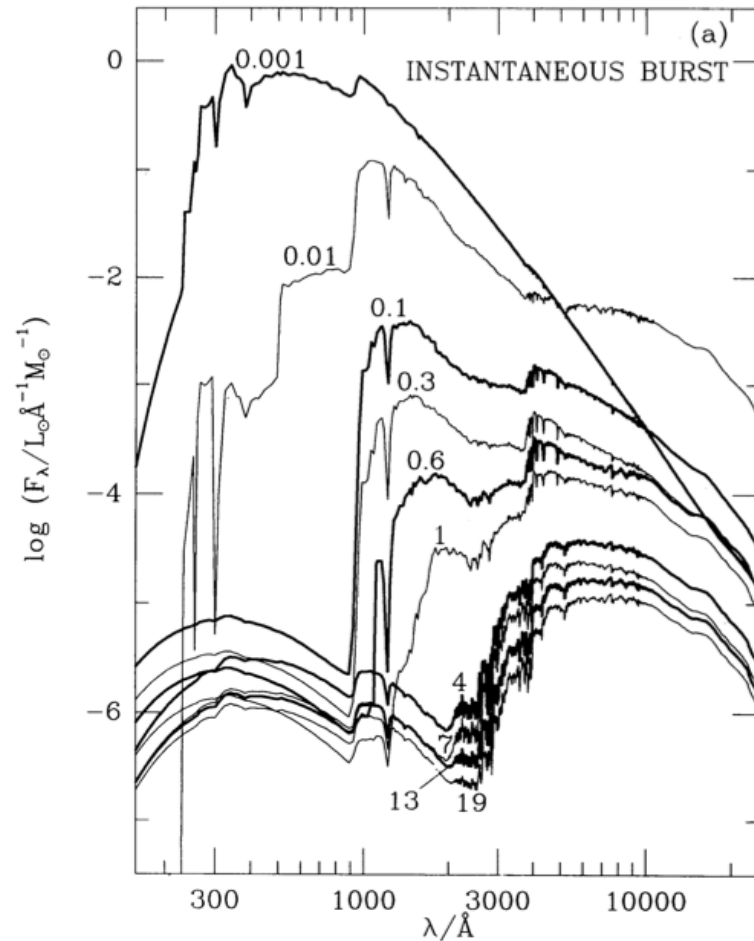
See also PEGASE and PEGASE-HR (Le Borgne et al. 2004,

<http://www2.iap.fr/pegase/>);
PEGASE-HR covers 400-680nm
at $R = 10,000$.

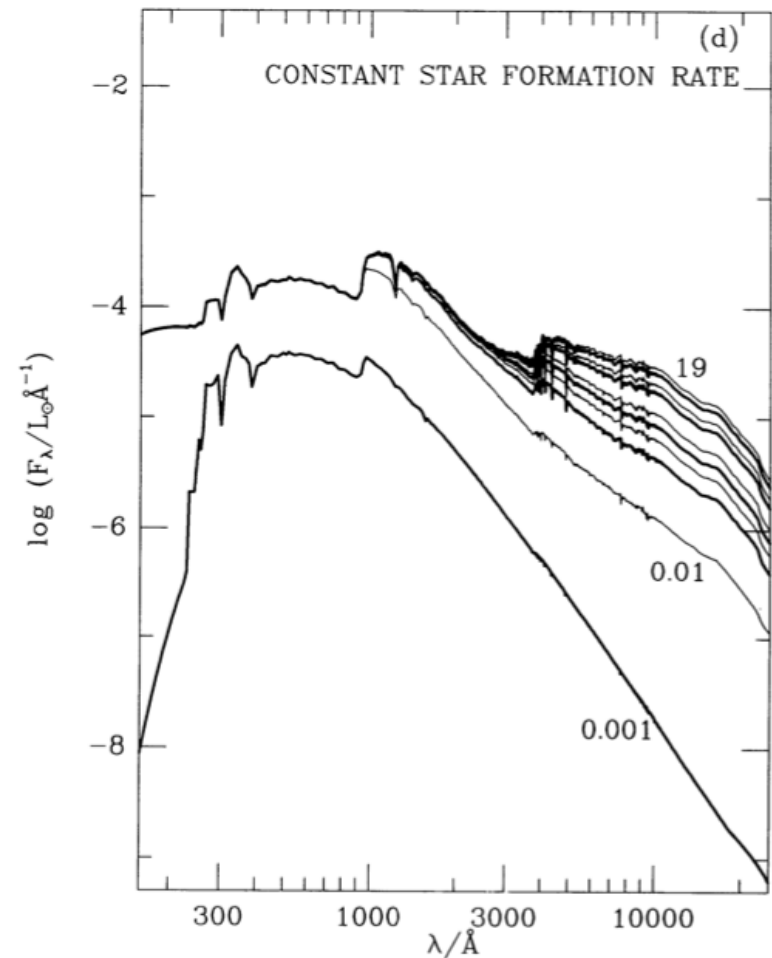
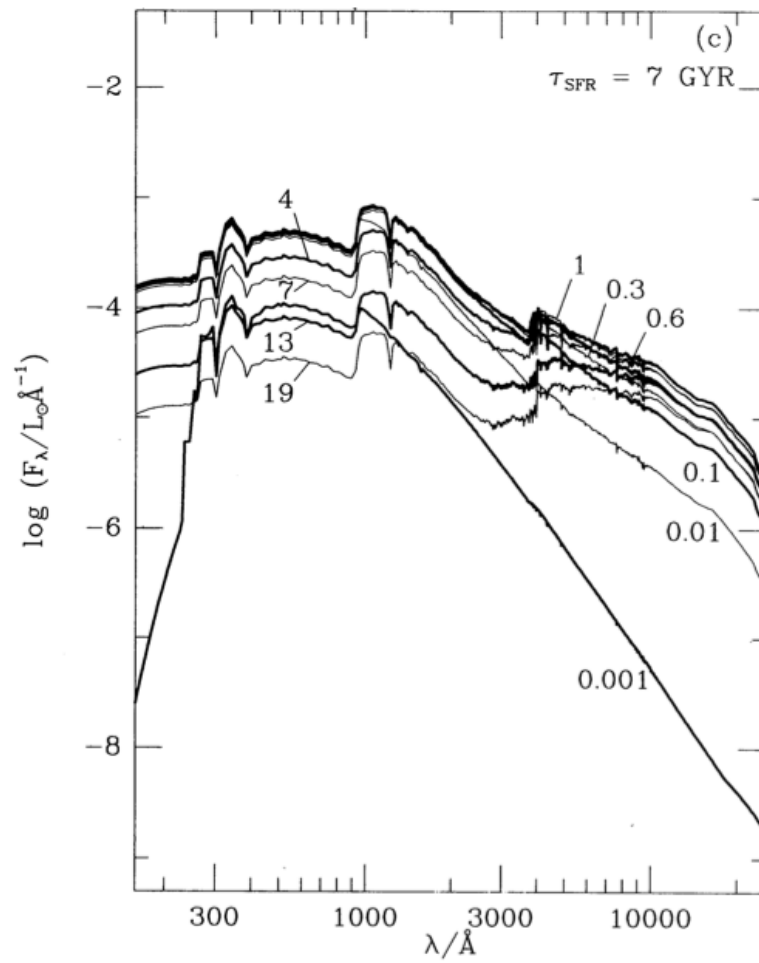
FIG. 2.—Fractional contribution to the integrated light of an instantaneous-burst population by the various stellar evolutionary stages, as predicted by the present model of spectral evolution (isochrone synthesis). The nine panels indicate the contributions to the bolometric light, to the fluxes at 1400 and 2200 Å, and to the broad-band *UBVRIC* fluxes. In each panel the different curves correspond to the following stellar evolutionary stages (acronyms defined in § 3.5): main sequence (solid line), SGB (short-dash-long-dash line), RGB (dashed line), CHeB (long-dashed line), AGB (dot-short dash line), PNN (dot-long dash line), and WD (short-dashed line).

► See also Portinari et al. 2004, Maraston et al., Conroy et al.: chem. evol., late phases.

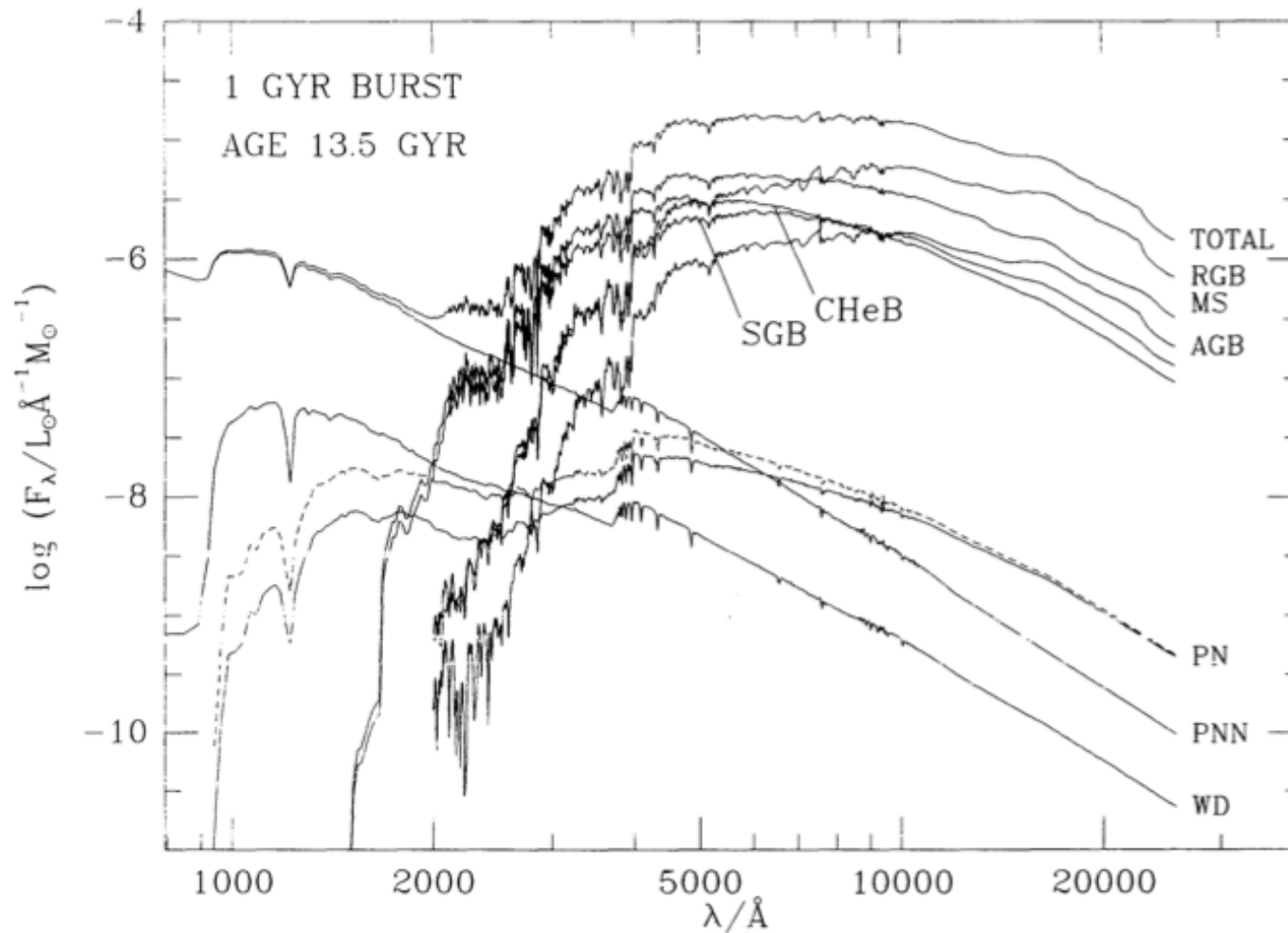
SPS Evolution: early star-formers



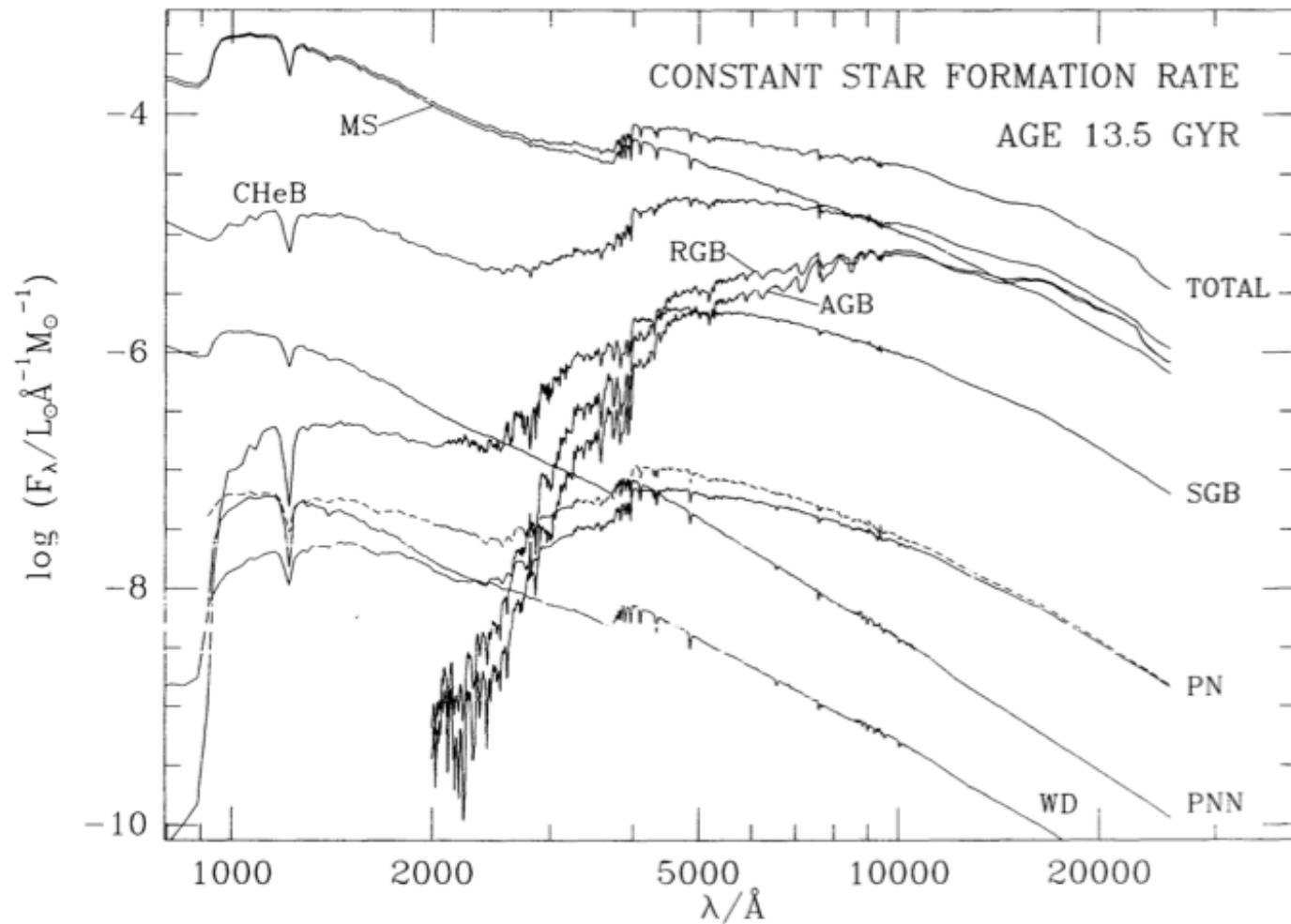
SPS Evolution: on-going star-formers



SPS Contributions today: early star-formers



SPS Contributions today: on-going star-formers



List of modern SPS

- ▶ Bruzual & Charlot (2003, ApJ)
- ▶ Conroy, Gunn & White (2009, ApJ, 699, 486)
- ▶ Maraston & Strömbäck (2011, MNRAS, 418, 2785)
- ▶ Vazdekis et al. (2015, MNRAS, 449, 1177)



Differential populations synthesis

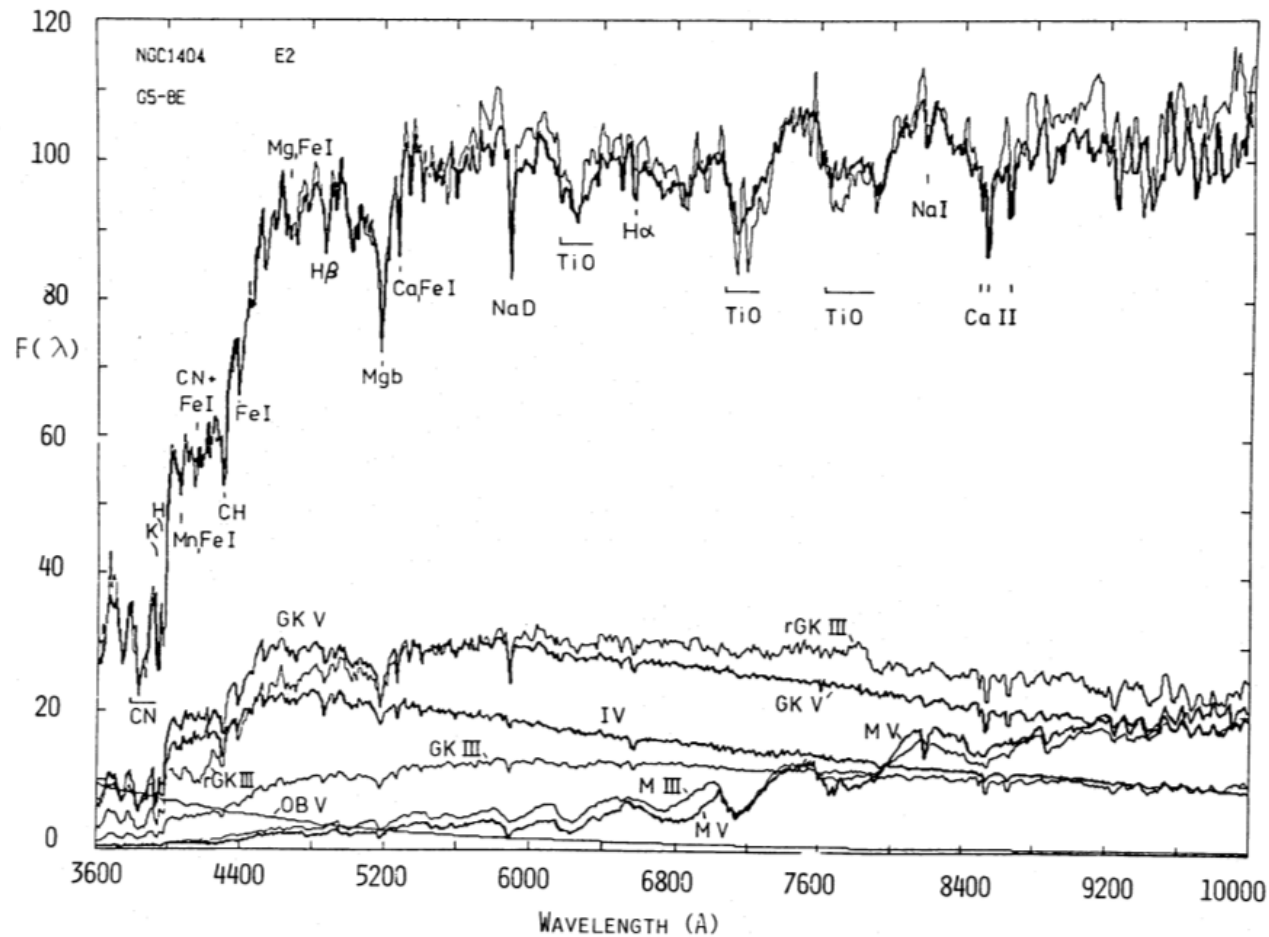
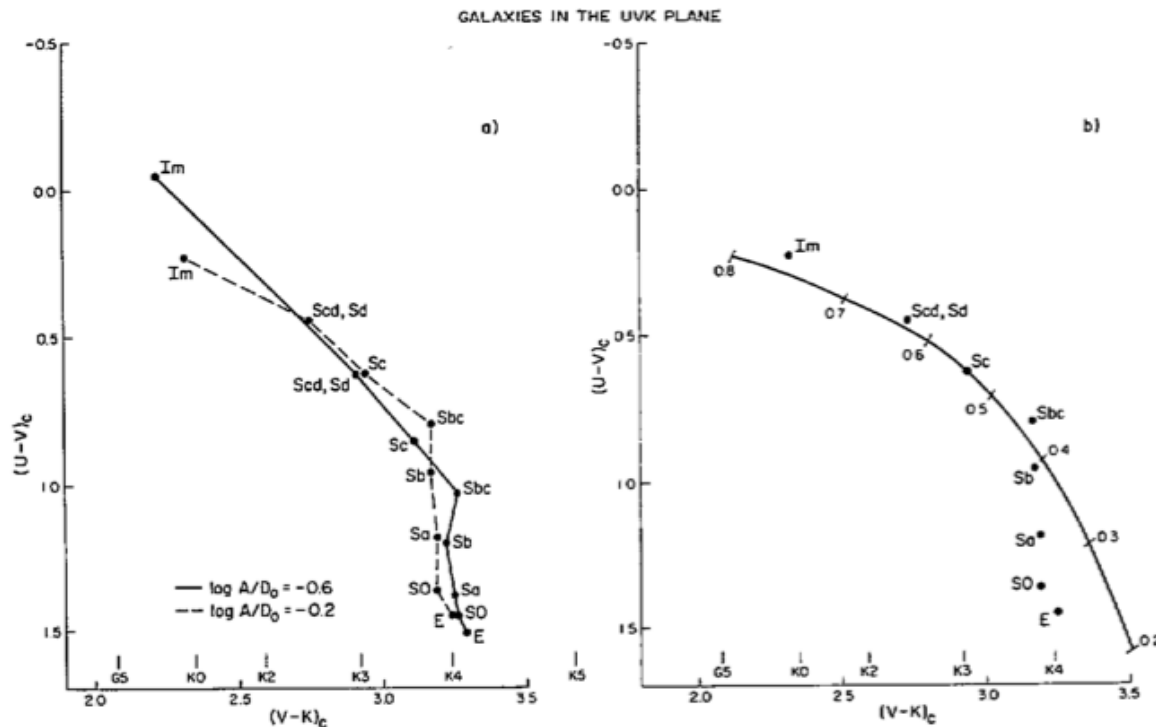


FIG. 2a

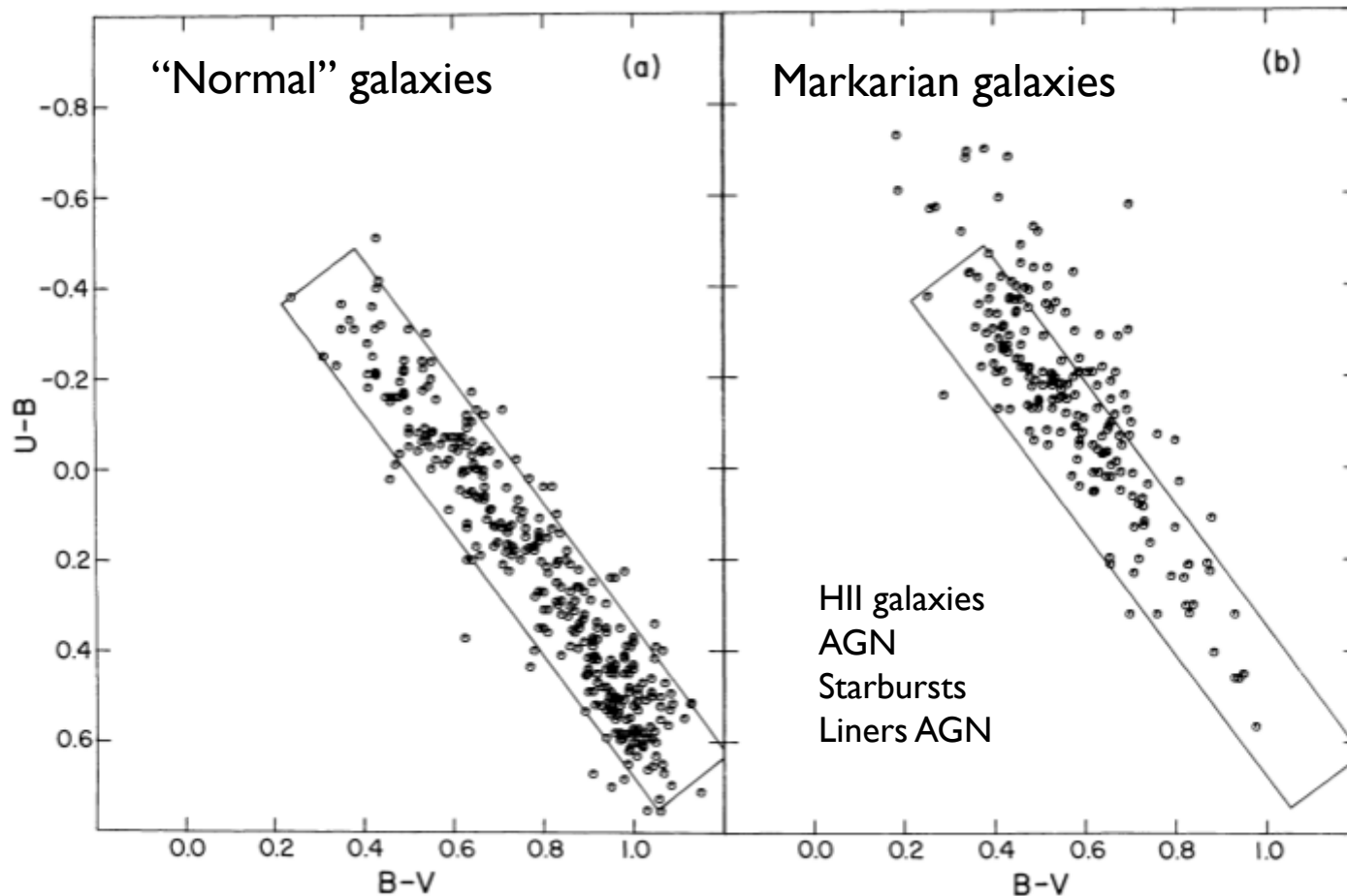
Simple population synthesis: the UVK plane



U: 370 nm
V: 550 nm
K: 2200 nm

Galaxies can be well-modeled by an admixture of A0V and M0III in U-V vs V-K

Galaxies in the UBV plane



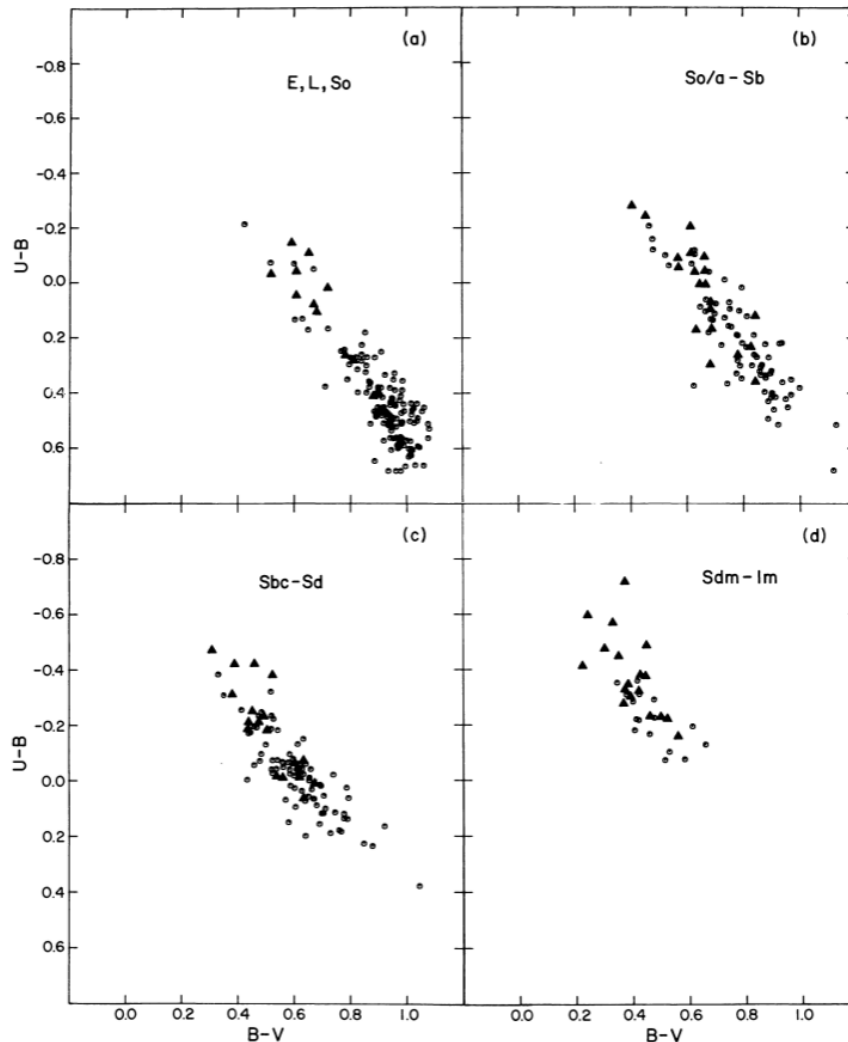
Markarian:
Russian astronomer

U: 370 nm
B: 440 nm
V: 550 nm

What's the
color of an
A0V?

What does this
tell us about
Aaronson's
simplification of
A0V+M0III for
the UVK plane?

Galaxies in the UBV plane by Type



U: 370 nm

B: 440 nm

V: 550 nm

What's the color of an A0V?

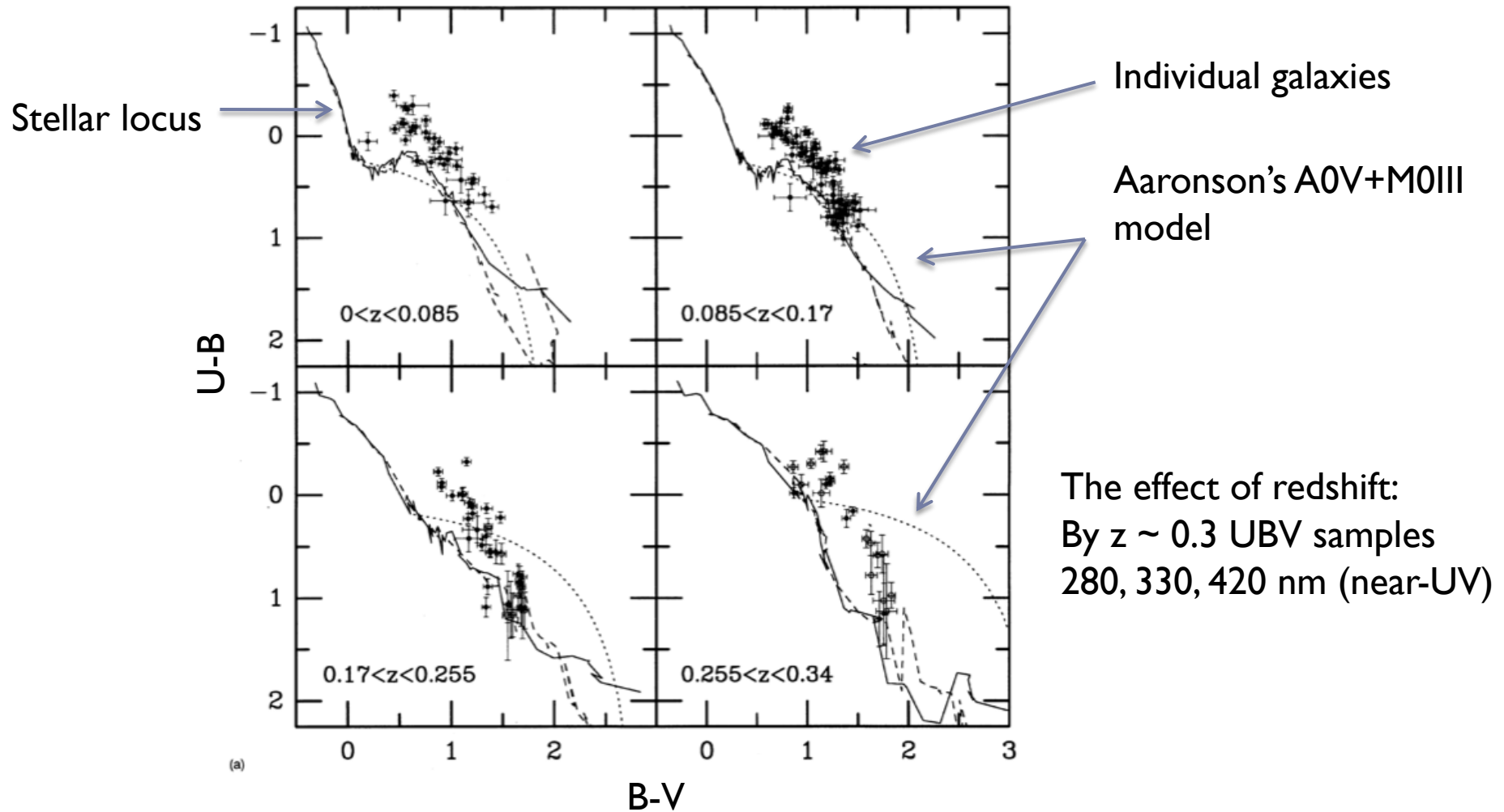
What does this tell us about Aaronson's simplification of A0V+M0III for the UVK plane?

Why is it more complicated when you look in more detail in the blue? ($U-V \rightarrow U-B, B-V$)

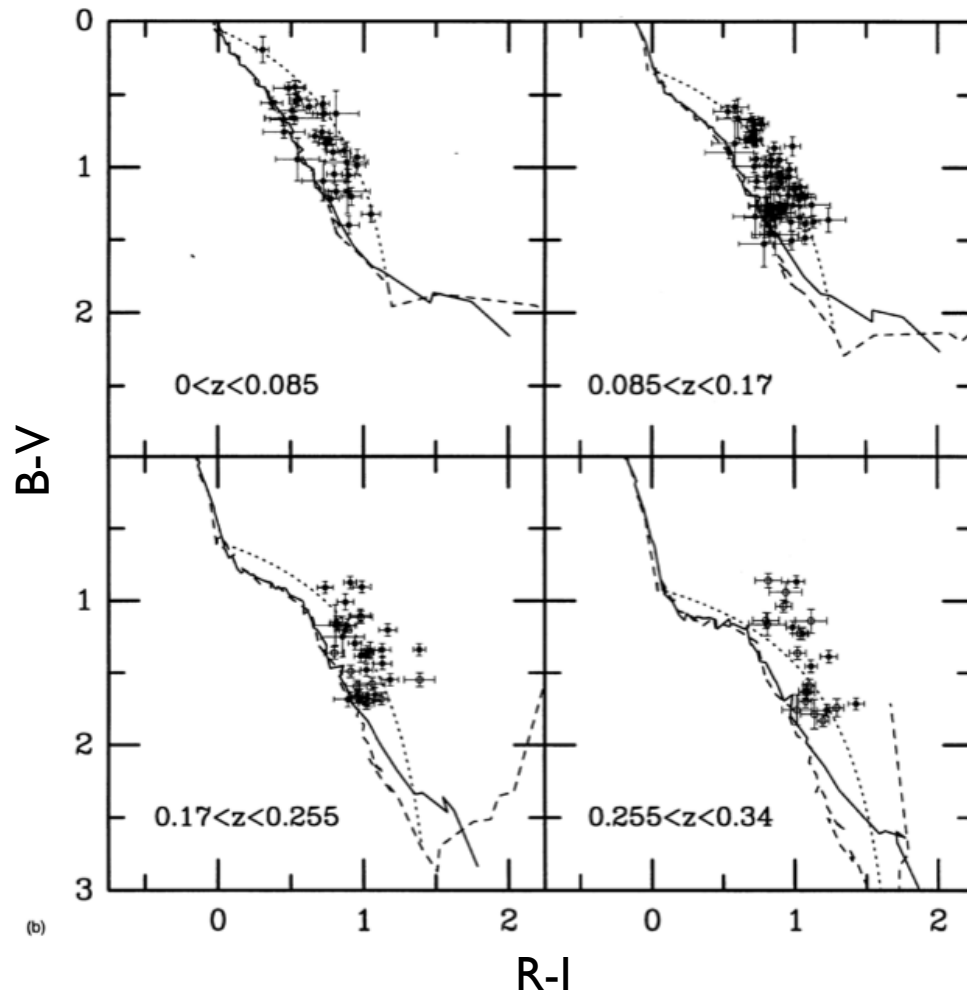
What are the implications for spectra?



Galaxies: UBVRIK multi-colors

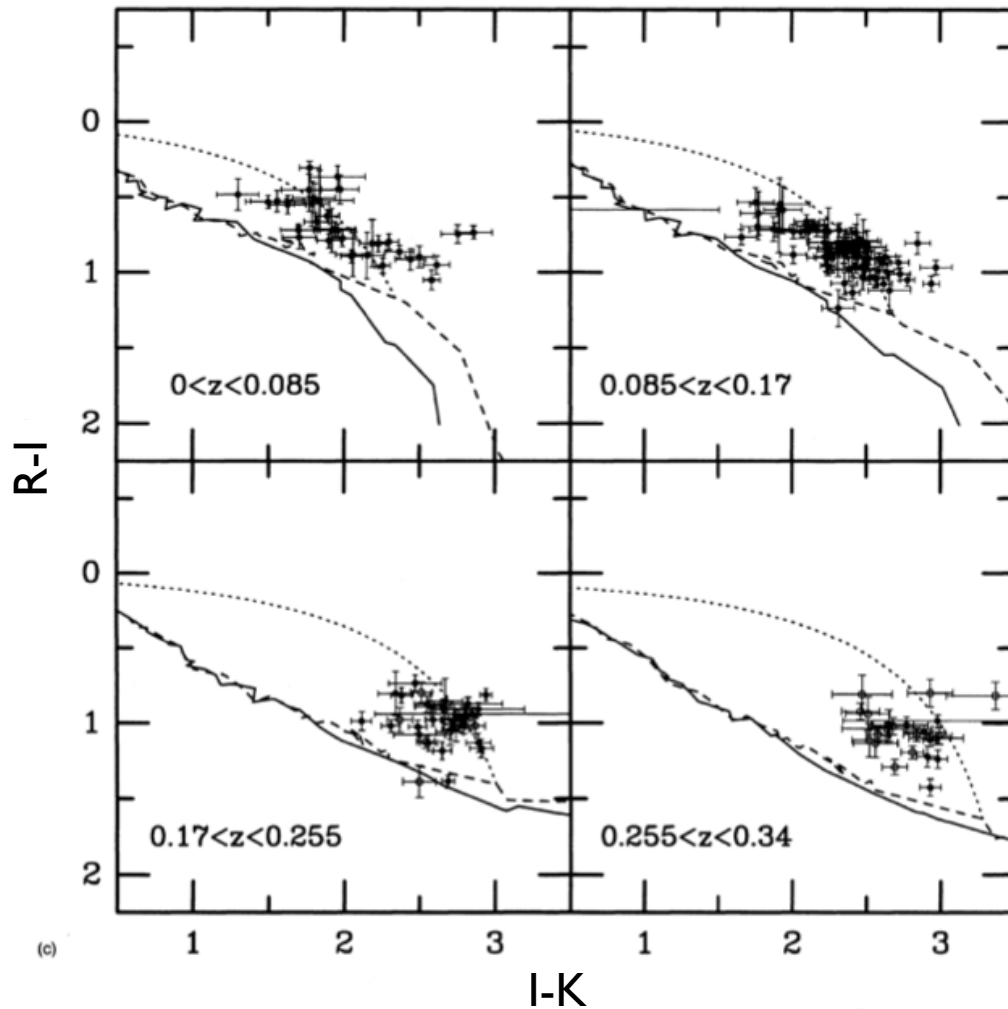


Galaxies: UBVRIK multi-colors



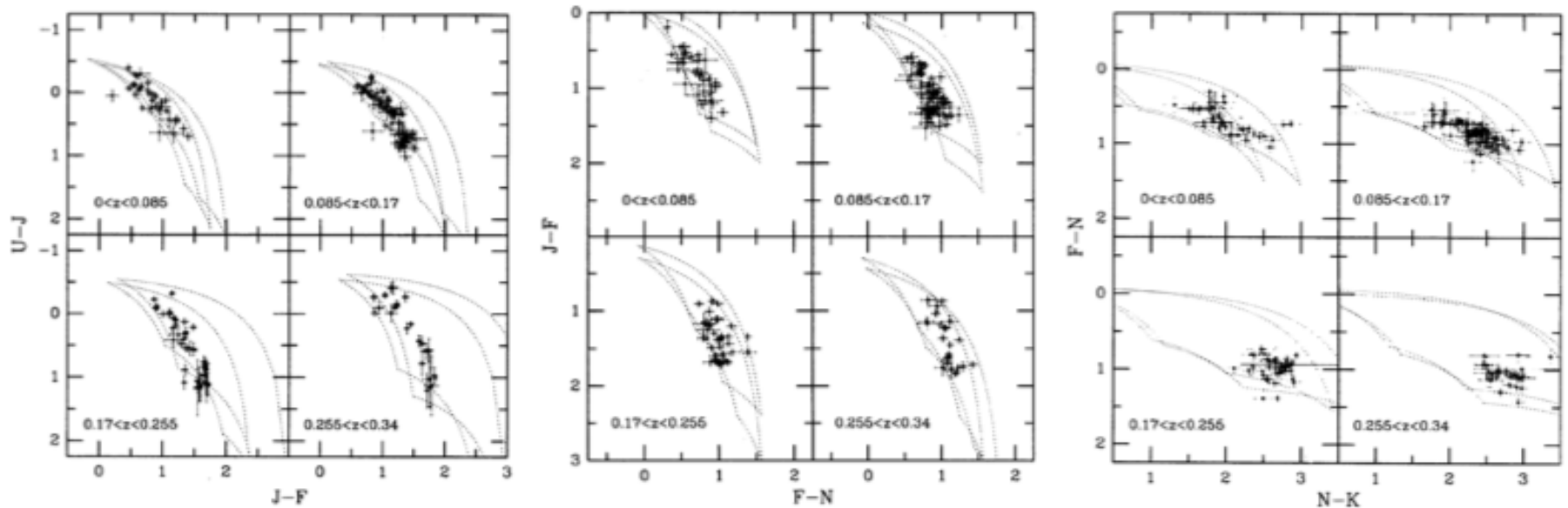
R: 650 nm
I: 800 nm

Galaxies: UBRIK multi-colors



Simple model: 4 stars in UBRIK

Linear combinations of B V, G V, K III, M III

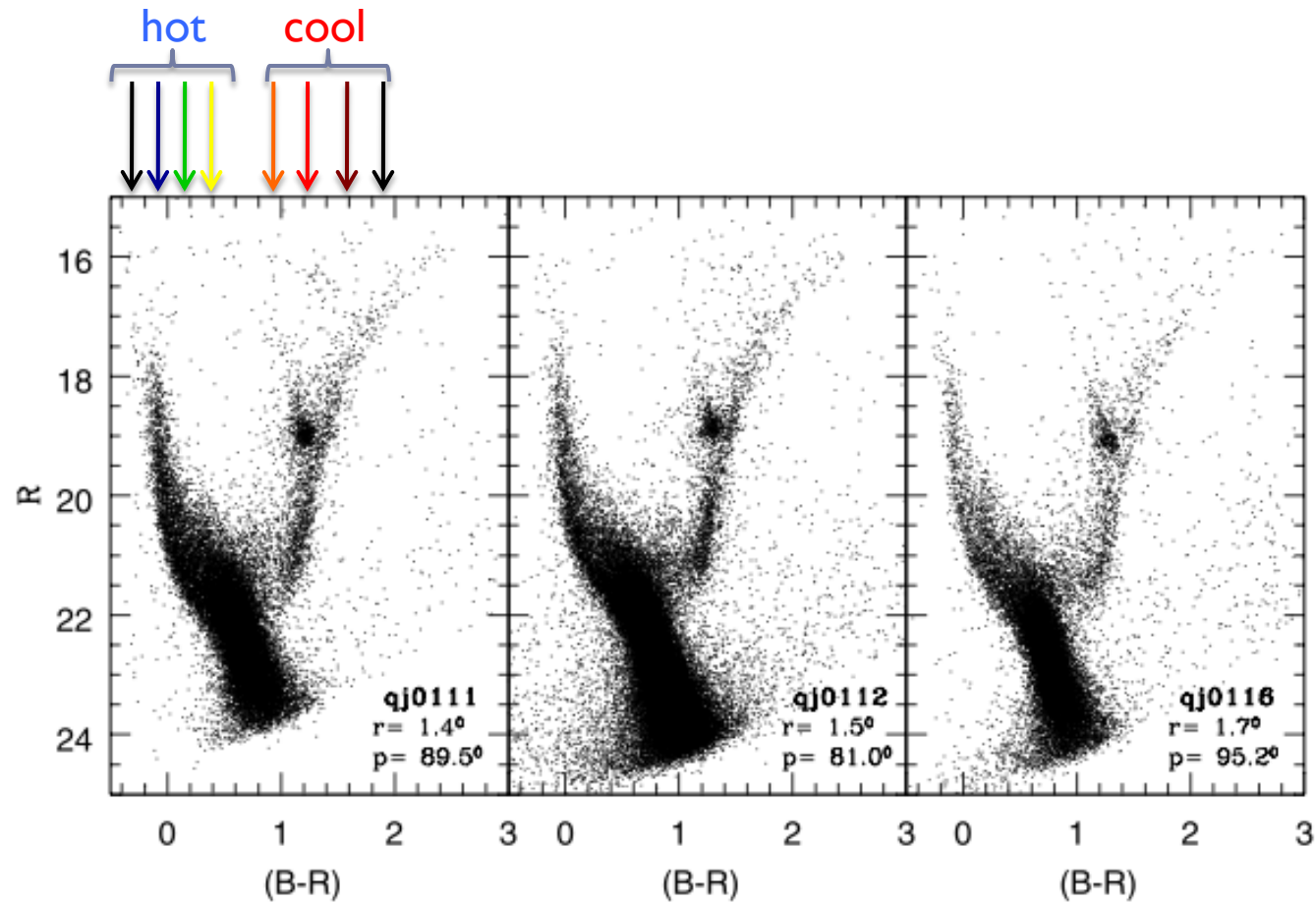


Alternatively, use linear combinations of 2 stars, but don't fix type:

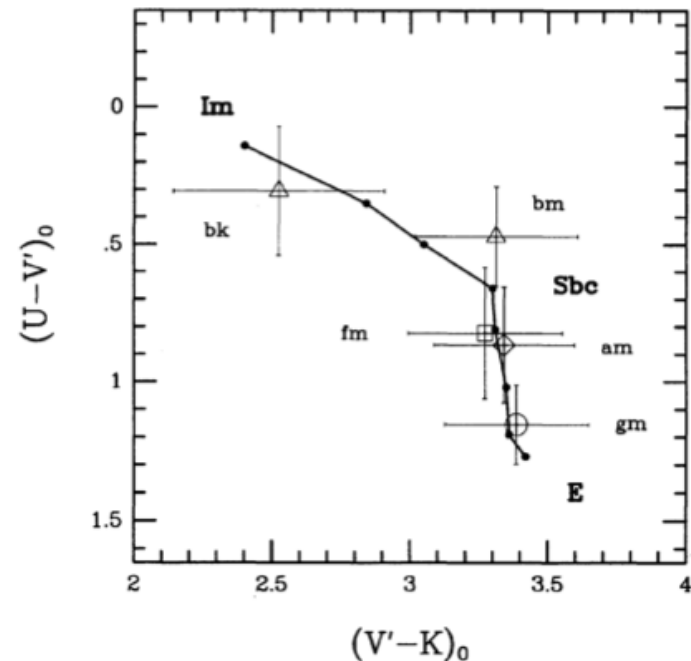
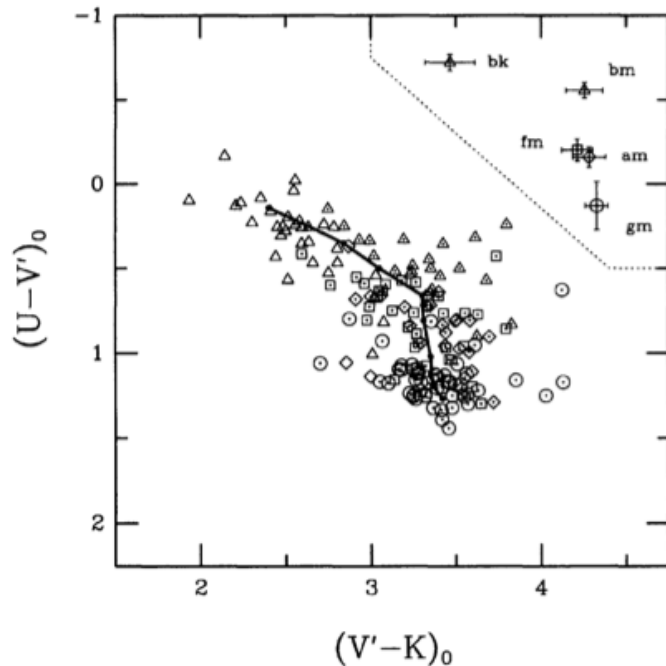
- One star is hot (ranging from B to G) – assume luminosity class V
- The second star is cool (ranging from G to M) – assume luminosity class III

Thinking in terms of CMDs, why does this make sense?

CMD for the SMC at 60 kpc OMG



UVK plane revisited

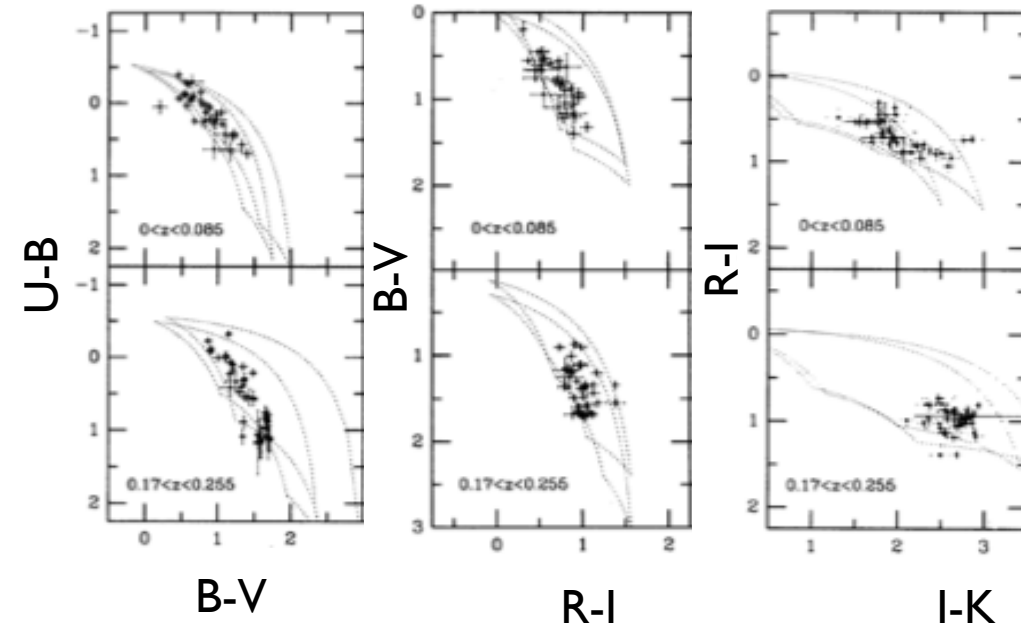


- Galaxies classified by two-star models required to fit UBVRIK multicolors
- Reminiscent of Morgan spectral-types, extended to red and NIR

Simple SPS: Linear combinations of 3-4 stars

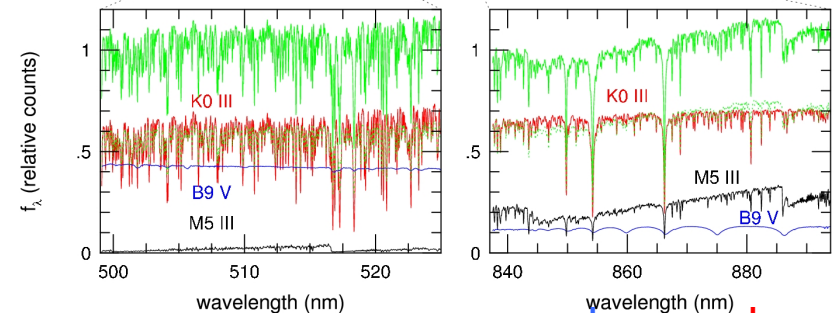
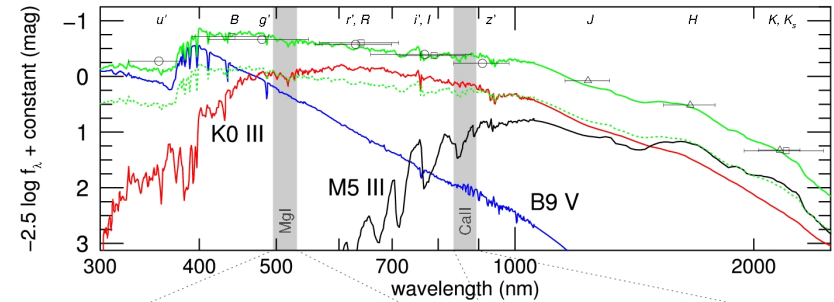
(e.g., B V, G V, K III, M III) works from 0.35-2.2 microns

Integrated colors of galaxies....to detailed SEDs:

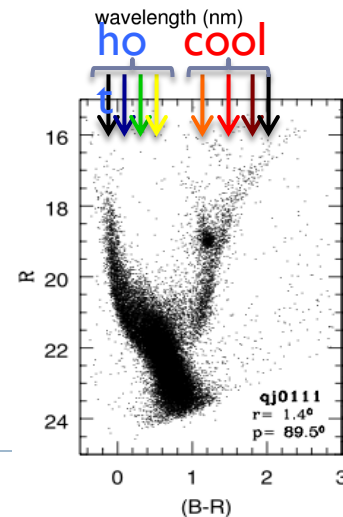


Why do it?

Whenever you know there are systematic uncertainties in complex models (e.g., SPS tracks, libraries) fall back to minimal empirical constraints. (a) This is what any complex model must reproduce. (b) You know which stars (what physics) are most important to get right in your complex models.



Why it works:
Think in terms of
CMDs:



Nucleosynthesis

▶ Hydrogen Burning (main sequence)

▶ P-P chain:

- ▶ $\text{H} + \text{H} \rightarrow {}^2\text{D} + \text{e}^+ + \nu + 0.42 \text{ MeV}$
- ▶ ${}^2\text{D} + \text{H} \rightarrow {}^3\text{He} + \gamma$
- ▶ ${}^3\text{He} + {}^3\text{He} \rightarrow {}^4\text{He} + 2\text{H} + 12.86 \text{ MeV}$
- ▶ Or step through ${}^8\text{Be}$ (only 14% of the time)

▶ CNO bi-cycle (if $T > 20$ million K)

- ▶ ${}^{12}\text{C} + \text{H} \rightarrow {}^{13}\text{N} + \gamma \dots$
- ▶ ${}^{14}\text{N} + \text{H} \rightarrow {}^{15}\text{O} \dots {}^{17}\text{O} + \text{H} \rightarrow {}^{14}\text{N} + {}^4\text{He}$
- ▶ N can be brought to surface via dredge-up; majority of ${}^{14}\text{N}$ is produced this way \rightarrow “secondary” product

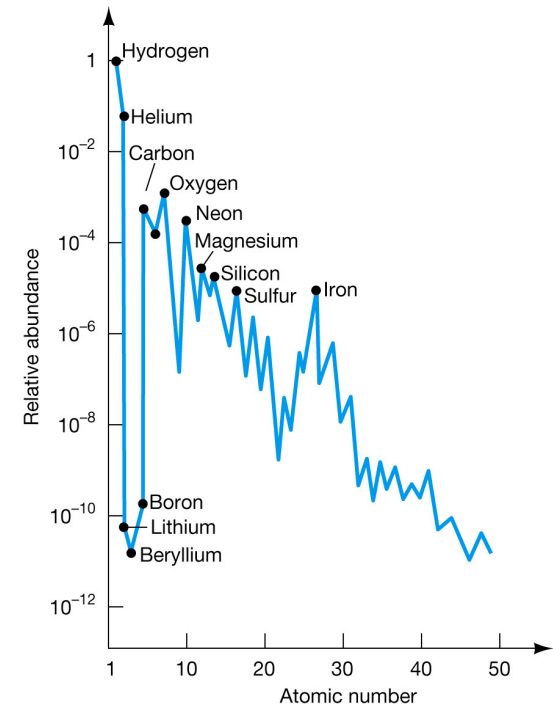
▶ Giant Branch ($T \sim 10^8 \text{ K}$)

- ▶ $2\alpha \rightarrow {}^8\text{Be}; {}^8\text{Be} + \alpha \rightarrow {}^{12}\text{C}$
- ▶ Causes core expansion for $M > 2M_{\odot}$



Nucleosynthesis – later stages

- ▶ Higher mass stars → past He burning
 - ▶ $^{12}\text{C} + \alpha \rightarrow ^{16}\text{O} + \text{energy}$ ($M < 8M_{\odot}$)
 - ▶ $^{16}\text{O} + \alpha \rightarrow ^{20}\text{Ne} + \text{energy}$ ($M > 8M_{\odot}$)
 - ▶ $^{20}\text{Ne} + \alpha \rightarrow ^{24}\text{Mg} + \text{energy}$
- ▶ More complex reactions:
 - ▶ $^{14}\text{N} \xrightarrow{\alpha} ^{18}\text{F} \xrightarrow{\alpha} ^{18}\text{O} \xrightarrow{\alpha} ^{22}\text{Ne} \xrightarrow{\alpha} ^{25}\text{Mg} + n$
(α reactions)
 - ▶ $^{12}\text{C} + ^{12}\text{C} \rightarrow ^{23}\text{Mg} + n$
 - ▶ *Free neutrons!*
- ▶ Highest mass stars
 - ▶ $^{24}\text{Mg} + \alpha \rightarrow ^{28}\text{Si}$
 - ▶ $^{16}\text{O} + ^{16}\text{O} \rightarrow ^{32}\text{S}$
 - ▶ Leads to Fe peak → Type-II SNe (core collapse, bounce)



Dispersing the Elements

▶ Intermediate mass stars

- ▶ $M < 2.5 M_{\odot} \rightarrow$ CO degenerate core, PN, some He output
- ▶ $2.5 M_{\odot} < M < 8 M_{\odot}$
 - ▶ Convective overshoot \rightarrow dredge-up of CNO cycle products (e.g., ^{14}N)
 - ▶ Dredge-up can reach He-burning products on AGB \rightarrow C, O
 - ▶ Pulses drive mass loss (10^{-7} to $10^{-5} M_{\odot}\text{yr}^{-1}$)
 - PN enriched in C,O,N, “s-process”
 - AGB shells good place to form molecules (CO)

▶ High mass stars ($M < 8 M_{\odot}$)

- ▶ Dispersal via SNe
- ▶ Primary products are α elements
- ▶ Some “r-process”



Neutron Capture Elements

- ▶ Certain elements are rich in neutrons
- ▶ Formation can't be explained by standard nucleosynthesis
- ▶ Neutron capture
 - ▶ $(t_{1/2})^{-1} \sim \sigma\Phi$ (cross section x neutron flux)
 - ▶ $(Z,A) + n \rightarrow (Z,A+1)$; is this stable?
 - ▶ Yes: sits around and waits for another n
 - ▶ No: decays to $(Z+1,A+1)$; is this stable?
 - ▶ Stable isotopes have higher abundances
- ▶ “Valley of Stability”



s-Process Valley of Stability

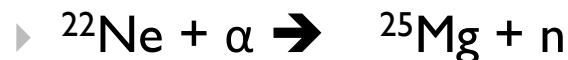
Se	Se65	Se66	Se67 60 ms	Se68 35.5 s 0+	Se69 27.4 s (3/2-)	Se70 41.1 m 0+	Se71 4.74 m 3/2-, 5/2-	Se72 8.40 d 0+	Se73 7.15 h 9/2+ *	Se74 0+	Se75 119.779 d 5/2+	Se76 0+	Se77 4/2- *	Se78 0+	Se79 1.19E6 y 7/2+ *	Se80 0+	Se81 18.45 m 1/2- *	Se82 1.08E+20 y 0+ 6.75	Se83 22.3 m 9/2+ *
+4/-2 78.96 2.03x10 ⁻⁶ %	ECp	3+	ECp	EC	ECp	EC	EC	EC	EC	0.89	EC	9.36	7.63	23.78	β ⁻	49.61	β ⁻ *	β ⁻ *	β ⁻ *
As63	As64	As65 0.19 s	As66 95.77 ms	As67 42.5 s (5/2-)	As68 151.6 s 3+	As69 15.2 m 5/2+	As70 52.6 m 4+	As71 65.28 h 5/2-	As72 26.0 h 2+	As73 80.30 d 3/2+	As74 17.77 d 2+	As75 3/2- *	As76 19778 d 3/2- *	As77 38.83 h 3/2+	As78 90.7 m 2+	As79 9.01 m 3/2+	As80 15.2 s 1+	As81 33.3 s 3/2+	As82 19.1 s (1+)
		EC	EC	EC	EC	EC	EC	EC	EC	EC	EC, β ⁻	100	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻ *
Ge62	Ge63	Ge64	Ge65	Ge66	Ge67	Ge68	Ge69	Ge70	Ge71	Ge72	Ge73	Ge74	Ge75	Ge76	Ge77	Ge78	Ge79	Ge80	Ge81
0+	95 ms	3+	30.9 s (3/2-)	2.26 h 0+	18.9 m 1/2+	270.8 d 0+	39.05 h 5/2-	21.23 0+	11.43 d 1/2- *	27.66 0+	7.73 0+	35.94 0+	62.78 m 3/2- *	0+	11.30 h 7/2+ *	88.0 m 0+	18.98 s (1/2-)	29.5 s 0+	7.6 s (9/2+)
EC	EC	EC	ECp	EC	EC	EC	EC	EC	EC	EC	EC	β ⁻	β ⁻ *	β ⁻	β ⁻ *	β ⁻	β ⁻ *	β ⁻	β ⁻ *
Ga61	Ga62	Ga63	Ga64	Ga65	Ga66	Ga67	Ga68	Ga69	Ga70	Ga71	Ga72	Ga73	Ga74	Ga75	Ga76	Ga77	Ga78	Ga79	Ga80
0.15 s (3/2-)	116.12 ms 0+	32.4 s 3/2-, 5/2-	2.627 m 0+	15.2 m 3/2+	9.49 h 0+	3.2612 d 3/2+	67.629 m 1+	60.108 3/2-	26.14 m EC, β ⁻	64.10 h 3/2- *	4.86 h 3/2-	8.12 m (3-)	126 s 3/2-	32.6 s (2+, 3+)	13.2 s (3/2-)	5.09 s (3+)	2.847 s (3/2-)	1.697 s (3)	
EC	EC	EC	EC	EC	EC	EC	EC	EC	EC, β ⁻	β ⁻ *	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻
Zn60	Zn61	Zn62	Zn63	Zn64	Zn65	Zn66	Zn67	Zn68	Zn69	Zn70	Zn71	Zn72	Zn73	Zn74	Zn75	Zn76	Zn77	Zn78	Zn79
2.38 m 0+	89.1 s 3/2-	9.186 h 3+	38.47 m 3/2+	0+	244.26 d 5/2+	0+	0+	0+	5.4 m 3/2- *	14 y 1+	7.45 m 3/2- *	46.5 h 0+	23.5 s (1/2-)	95.6 s 0+	10.2 s (7/2+)	5.7 s 0+	2.08 s (7/2+)	1.47 s 0+	995 ms (9/2+)
EC	EC	EC	EC	EC	EC	EC	EC	EC	EC	EC	EC	β ⁻	β ⁻	β ⁻	β ⁻ *	β ⁻	β ⁻ *	β ⁻	β ⁻
Cu59	Cu60	Cu61	Cu62	Cu63	Cu64	Cu65	Cu66	Cu67	Cu68	Cu69	Cu70	Cu71	Cu72	Cu73	Cu74	Cu75	Cu76	Cu77	Cu78
81.5 s 3/2-	23.7 m 2+	3.333 h 3/2-	9.74 m 1+	69.17 3/2-	1.579 h 1+	30.83 3/2-	5.078 m 1+	61.83 h 3/2-	31.1 s 1+	2.85 m 3/2-	4.5 s (1+)	19.5 s (3/2-)	6.6 s (1+)	3.9 s	1.594 s (1+, 3+)	1.224 s	0.641 s *	469 ms *	342 ms
EC	EC	EC	EC	EC	EC, β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻
Ni58	Ni59	Ni60	Ni61	Ni62	Ni63	Ni64	Ni65	Ni66	Ni67	Ni68	Ni69	Ni70	Ni71	Ni72	Ni73	Ni74	Ni75	Ni76	Ni77
0+	7.6E+4 y 3/2-	3+	3/2-	0+	10.1 y 1/2-	0+	2.6172 h 0+	54.6 h 0+	21 s (1/2-)	19 s 0+	11.4 s	0+	1.86 s	2.1 s 0+	0.90 s	1.1 s 0+	0+	0+	0+
68.077	EC	26.223	1.140	3.634	β ⁻	0.926	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻	β ⁻

Slow Neutron Capture

- ▶ “s-process”

- ▶ Neutron densities $\sim 10^5 \text{cm}^{-3}$

- ▶ Neutrons originate in minor He-burning reactions



- ▶ Where?

- ▶ H, He shells where burning takes place

- ▶ Example elements (Tc, Ba, La, Zr)

- ▶ Tc is the lightest element with no stable isotopes; lifetime $<$ stellar lifetime so presence of Tc implies in situ production and confirmation of s-process

- ▶ Nice review: Busso et al 2001, ApJ, 557, 802



Rapid Neutron Capture

▶ “r-process”

- ▶ Neutron capture rate $> \beta$ -decay rate (hours)
- ▶ Neutron densities $\sim 10^{23}\text{cm}^{-3} \rightarrow$ only see this in SNe
- ▶ Same fundamental process \rightarrow n capture to stable nuclei
- ▶ Example products: Eu, Ur, etc

▶ Mixed origins

- ▶ Rb, Pr, Nd \rightarrow 50/50 s/r
- ▶ Ba, La, Ce \rightarrow 85/15 s/r
- ▶ Eu \rightarrow 3/97 s/r



Type Ia Supernovae (SN Ia)

- ▶ CO white dwarf + companion
- ▶ Companion fills Roche lobe, dumps matter onto WD until electron degeneracy is overwhelmed:
 - ▶ Chandrasekhar mass = $1.4 M_{\odot}$
- ▶ Collapse and deflagration:
 - ▶ Explosive nucleosynthesis → whole thing goes
- ▶ Produces burning up to iron:
 - ▶ Mg, Si, Cr, Ni, Fe (main production of Fe)



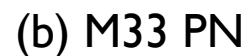
Abundance patterns in galaxies

- ▶ SFH reflected in abundances...
- ▶ Stellar lifetimes
 - ▶ $M > 20 M_{\odot}$ → $t < 10 \text{ Myr}$
 - ▶ $1.5 M_{\odot} < M < 5 M_{\odot}$ → $1.4 > t > 0.1 \text{ Gyr}$
 - ▶ $M > 1.5 M_{\odot}$ → $t > 1.4 \text{ Gyr}$
- ▶ Single massive stars produce
 - ▶ Little Fe (it's locked up)
 - ▶ Lots of α -elements, r-process elements
 - ▶ $40 M_{\odot}$ star produces $7 M_{\odot}$ of O
- ▶ Intermediate mass stars produce
 - ▶ O, C, N, plus s-process elements
 - ▶ $0.1 M_{\odot}$ of N

What are the implications for the SFH for finding stars and gas that is α -element rich?



- ▶ (a) Stellar spectra: bright stars
- ▶ (b) Emission line spectra: HII regions and Planetary Nebulae (PN)
- ▶ (c) QSO absorption lines



Extragalactic Abundances: Definitions

▶ Relative Abundances

- ▶ $[X/H] = \log_{10}(n(X)/n(H)) - \log_{10}(n(X)/n(H))_{\odot}$

- ▶ where X is any element

- ▶ Doesn't have to be H

- ▶ $[O/Fe] = \log_{10}(n(O)/n(Fe)) - \log_{10}(n(O)/n(Fe))_{\odot}$

▶ Absolute abundances

- ▶ $12 + \log_{10}(O/H)$ (small numbers!)



Solar/Orion Context

▶ Sun

- ▶ $\log_{10}(\text{He}/\text{H}) = -1.0$
- ▶ $\log_{10}(\text{O}/\text{H}) = -3.1$
- ▶ $\log_{10}(\text{C}/\text{H}) = -3.4$
- ▶ $\log_{10}(\text{Fe}/\text{H}) = -4.5$
- ▶ $\log_{10}(\text{Ne}/\text{H}) = -3.9$
- ▶ $\log_{10}(\text{N}/\text{H}) = -4.0$
- ▶ $\log_{10}(\text{Z}/\text{H}) = -8.5$

▶ Orion

- ▶ $\log_{10}(\text{O}/\text{H}) = -3.3$
- ▶ $\log_{10}(\text{C}/\text{H}) = -3.5$
- ▶ $\log_{10}(\text{Fe}/\text{H}) = -4.52$

- ▶ Sun is slightly more metal rich than Orion!

- ▶ (remember the local bubble?)

- ▶ LMC is 50-70% solar

- ▶ $[\text{O}/\text{H}] = -0.3$ to -0.15

- ▶ SMC ~ 20-25% solar

- ▶ $[\text{O}/\text{H}] = -0.7$ to -0.65



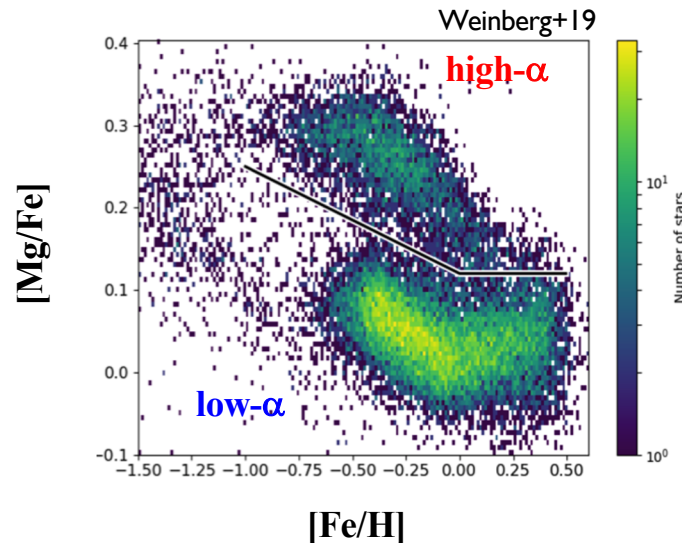
Abundance Patterns in the Milky Way

- ▶ **Solar neighborhood**
 - ▶ [Fe/H]-age relationship
 - ▶ [O/Fe] vs [Fe/H] correlation
 - ▶ Decreases with [Fe/H]
 - ▶ Similar for Mg, Si (α process)
 - ▶ [Ni/Fe], [Ba/Fe] flat with [Fe/H]
 - ▶ [s-process/Fe] correlates with [Fe/H]
 - ▶ e.g., [Ni/Fe], [Ba/Fe]
 - ▶ Why?
- ▶ **Halo stars generally metal poor**
 - ▶ [Fe/H] $\sim -1.6 \rightarrow -2.4$
 - ▶ $[\alpha/\text{H}] \sim 0.25\text{-}0.30$
 - ▶ [Fe/H] decreases with R ($0.07 \text{ dex kpc}^{-1}$)
- ▶ **Thick disk**
 - ▶ [O/Fe], [Mg/Fe] enhanced
 - ▶ Eu enhanced
 - ▶ $[\alpha/\text{Fe}]$ enhancement decreases with [Fe/H]
 - ▶ Looks like metal-poor halo, but kinematics of a disk



Classical MW Chemical Cartography:

Assembly and enrichment of stellar populations in our Galaxy



Striking chemical duality: Typical of other (MW-mass) galaxies?

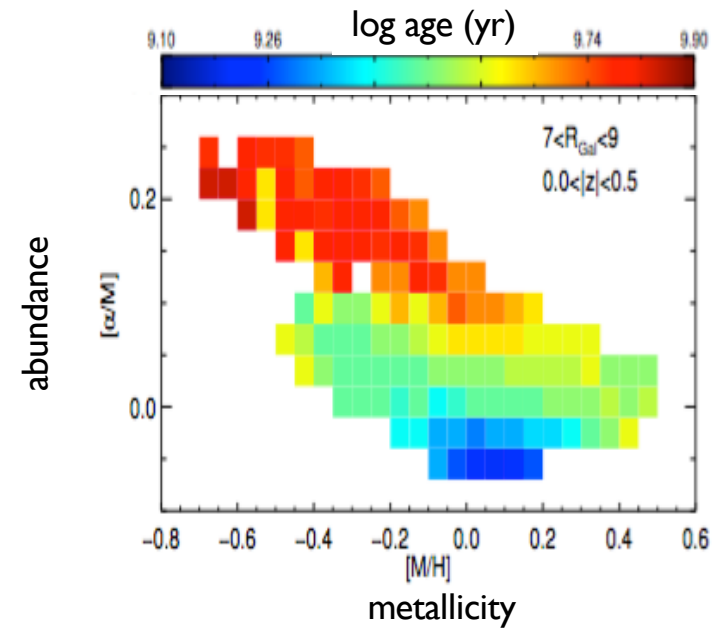
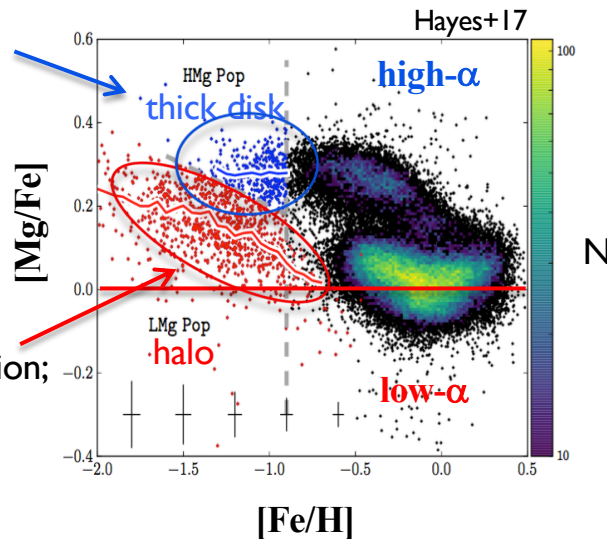
APOGEE Surveys: SDSS-III/IV

Classical MW Chemical Cartography:

In-situ vs accreted populations

Rotating population;
in-situ formation
thick disk

Non-rotating population;
accreted halo



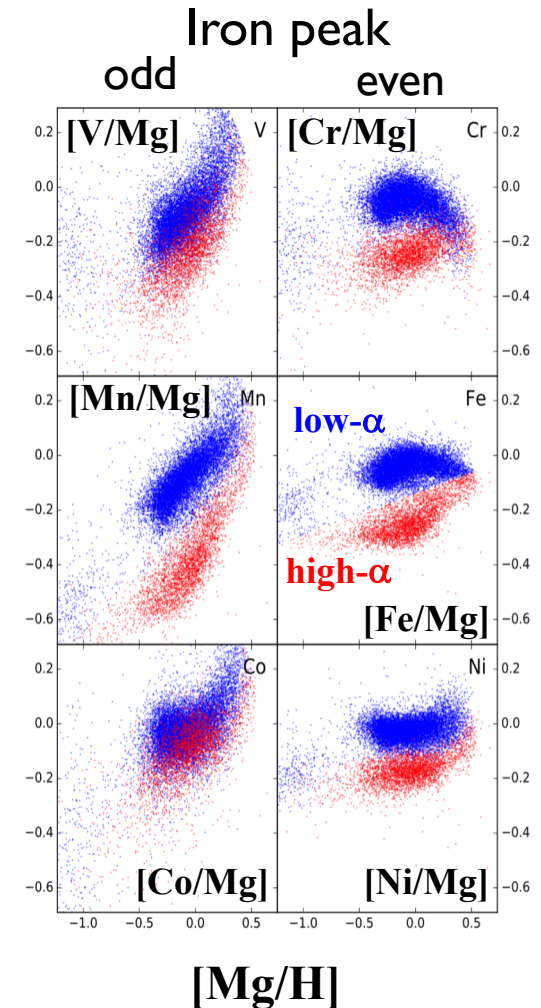
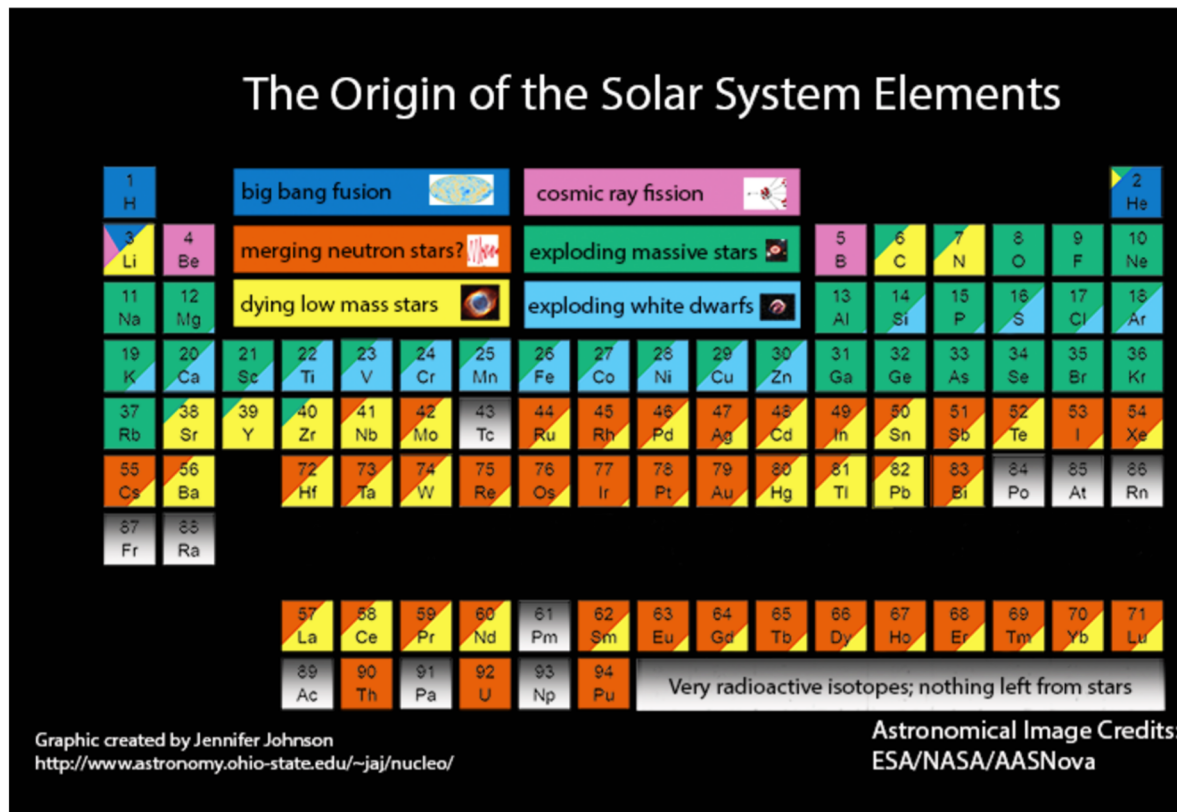
➤ Similar results for MW globular clusters

Hayes+17, Fernandez-Alvar+17, Darrington+19

Ages from Gaia distances
and isochrone fitting

Classical MW Chemical Cartography:

Multi-element abundance ratios



Weinberg et al. 2019

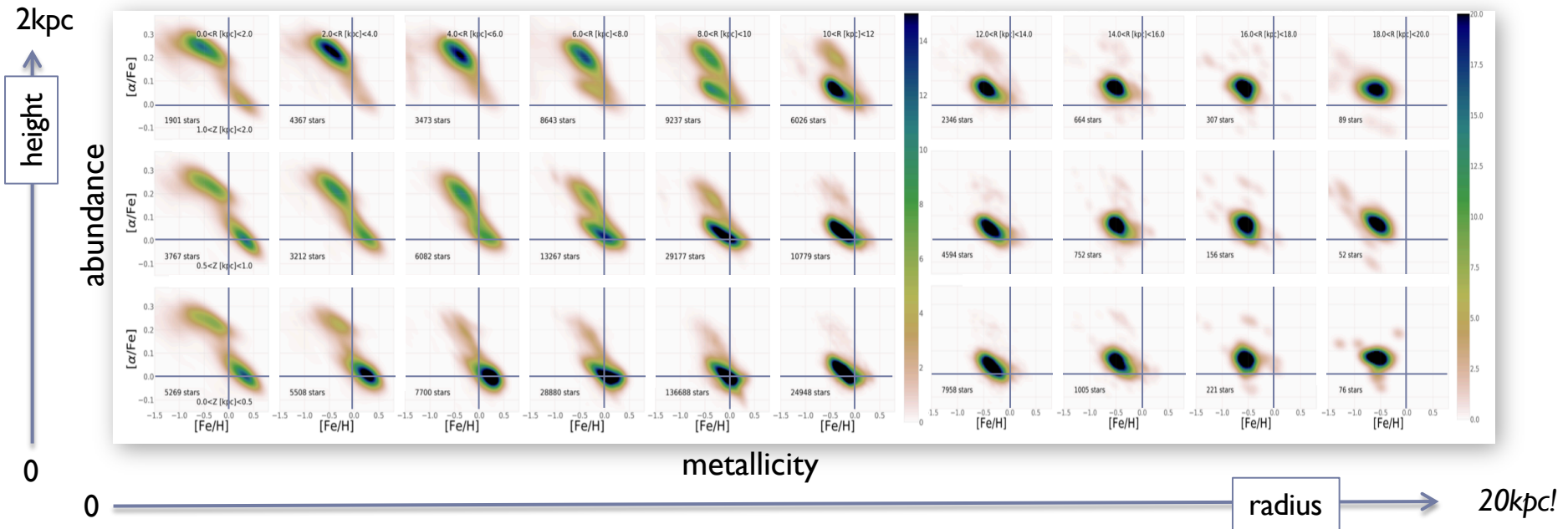
- CCSN yields?
- Non-LTE systematics?

Abundance Patterns in the Milky Way

APOGEE Surveys: chemical cartography

“striking chemical duality in the innermost regions of the disk, now clearly extending to the inner bulge”

Hayden+15 Queiroz+2020 Abudurro'uf+2022



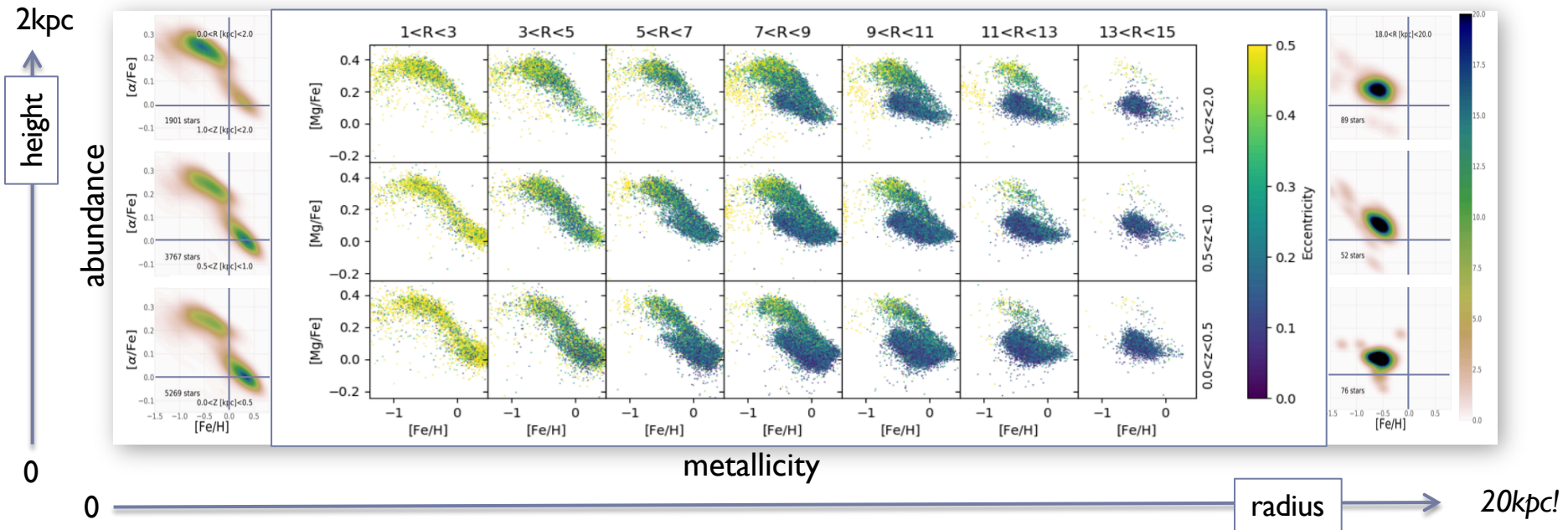
APOGEE-2: abundances *throughout* the galaxy

Abundance Patterns in the Milky Way

APOGEE Surveys: chemical cartography

“striking chemical duality in the innermost regions of the disk, now clearly extending to the inner bulge”

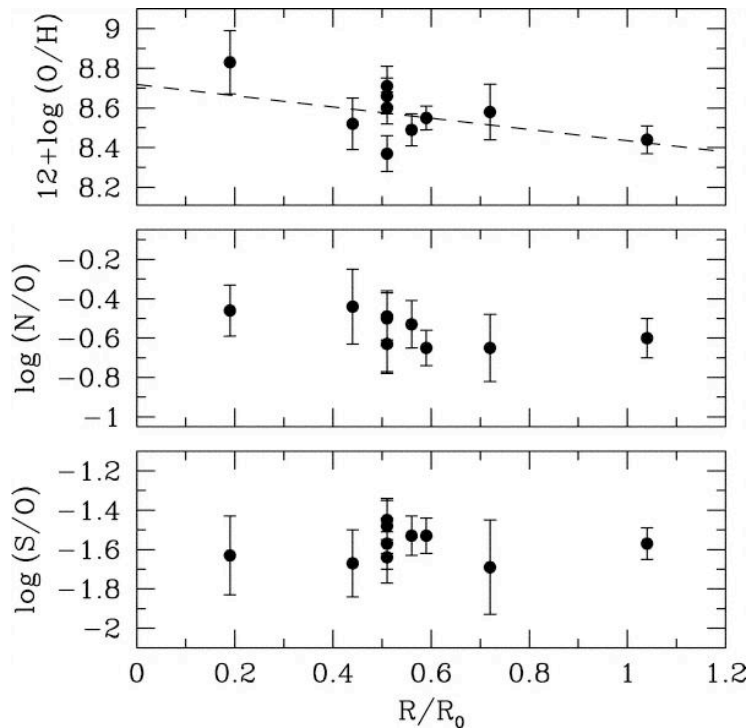
Hayden+15 Queiroz+2020 Abudurro'uf+2022



APOGEE-2: abundances *throughout* the galaxy

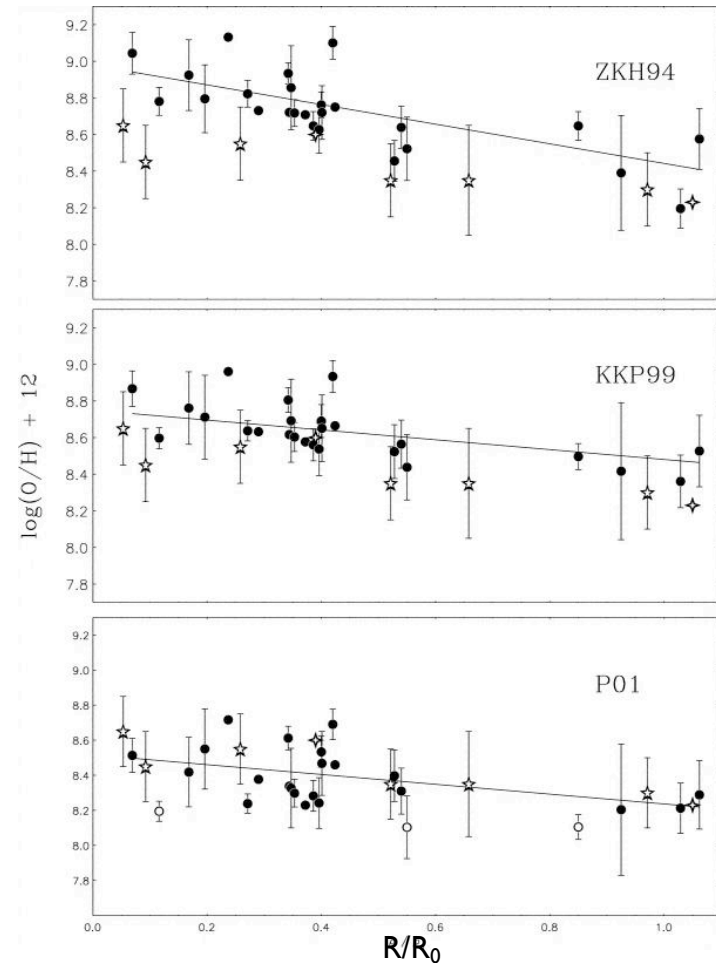
Abundance Gradients in Disk Galaxies

► HII regions in M51



$$\log(\text{O}/\text{H})_{\odot} = -3.1 \rightarrow$$
$$12 + \log(\text{O}/\text{H})_{\odot} = 8.9$$

► HII regions in N300



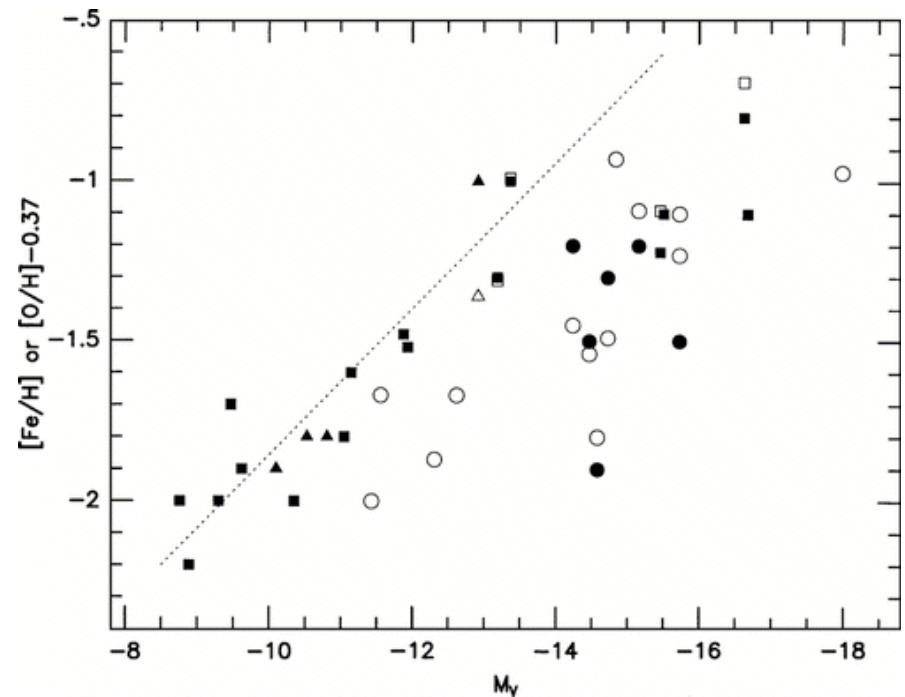
Disk Gradients (continued)

- ▶ General characteristics
 - ▶ $12 + \log(\text{O}/\text{H}) + 12 = 8.58 - 0.32 R/R_0$
 - ▶ Generally: -0.04 to -0.07 dex/kpc
 - ▶ Flatter in late-types, steep in barred galaxies
- ▶ Why are there gradients?
 - ▶ Radial dependence on SFR/SFH?
 - ▶ Radial gas flows?
 - ▶ Radial dependence on yield?
 - ▶ Radial dependence on infalling gas?
- ▶ Why aren't there larger gradients?
 - ▶ Radial migration?



Extragalactic Abundances: Dwarfs

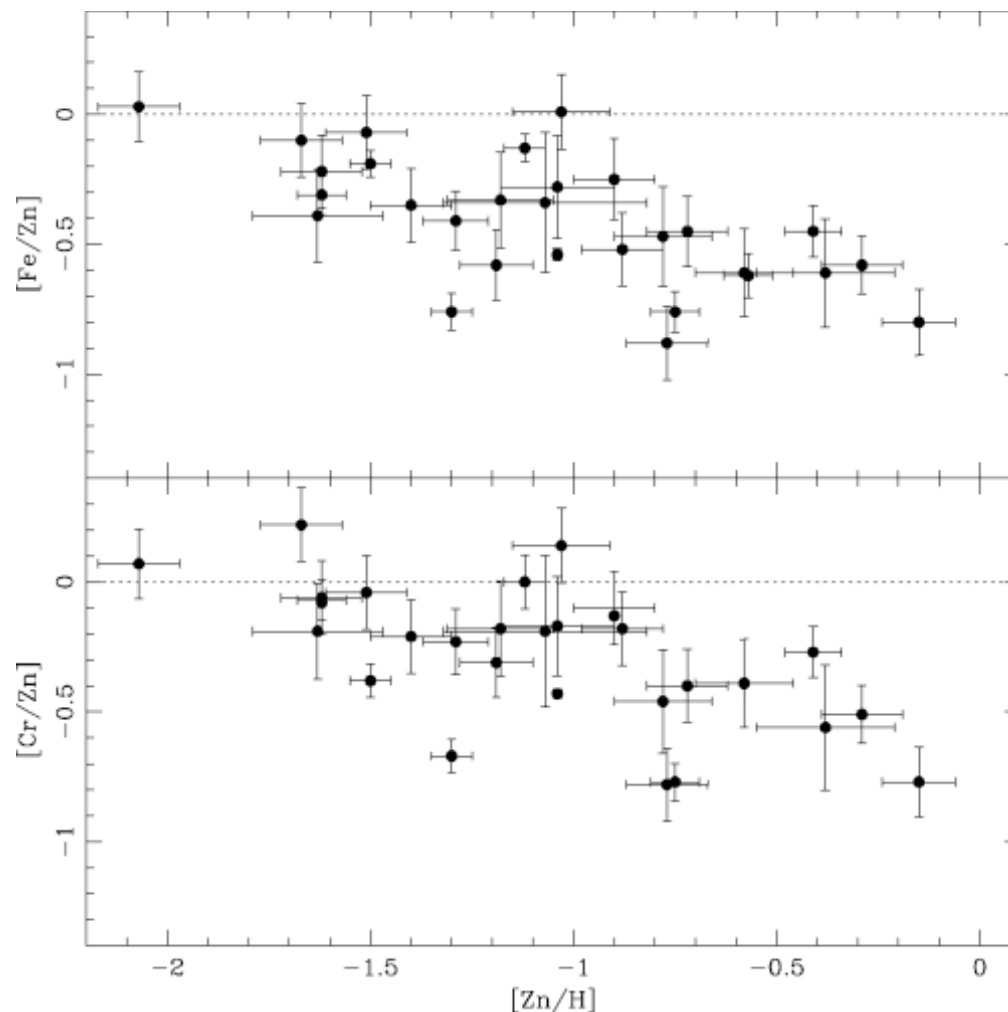
- ▶ LMC is 50-70% solar
 - ▶ $[O/H] = -0.3$ to -0.15
- ▶ SMC \sim 20-25% solar
 - ▶ $[O/H] = -0.7$ to -0.65
- ▶ Some dwarfs extremely metal poor (1/10 solar)
- ▶ Why?



← Decreasing luminosity

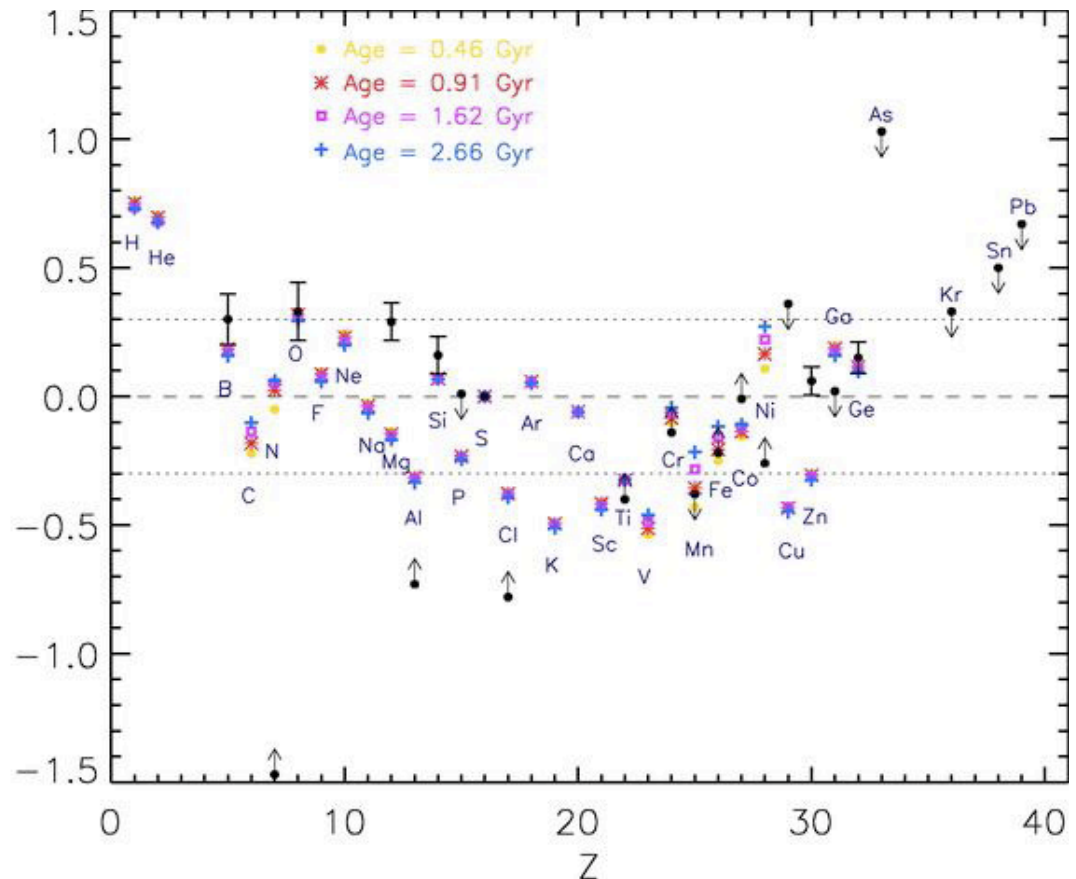
QSO Absorption Lines

- ▶ Absorption line systems detected against background quasars
- ▶ Gas phase abundances can be measured via absorption lines
- ▶ Most metal-poor gas systems ever found
- ▶ Enrichment histories vary from solar



QSO Absorption Lines

- ▶ Damped Ly- α systems have high column, high velocities \rightarrow correlated with galaxies
- ▶ Thought to be progenitors of today's massive galaxies
- ▶ Consistent with:
 - ▶ young ages
 - ▶ 1/3 solar
 - ▶ Enrichment dominated by massive stars
 - ▶ few Type Ia SNe



Fenner, Prochaska, & Gibson 2004 ApJ

Chemical Evolution of Galaxies

Simple models

- ▶ $M_g(t)$ = gas mass
- ▶ $M_r(t)$ = remnant mass
- ▶ M_s = mass in stars
- ▶ $M_h(t)$ = mass in heavy elements
- ▶ $Z(t) = M_h/M_g$ = metallicity
- ▶ ΔM = change in mass
- ▶ p = fractional yield of heavy elements



$$\begin{aligned}\Delta M_h &= p\Delta M_s - Z\Delta M_s \\ &= (p-Z)\Delta M_s \\ \Delta Z &= \Delta(M_h/M_g) \\ &= [p\Delta M_s - Z(\Delta M_s + \Delta M_g)]/M_g\end{aligned}$$

See S&G 4.3.2

▶ In a closed box $\Delta M_s + \Delta M_g = 0$

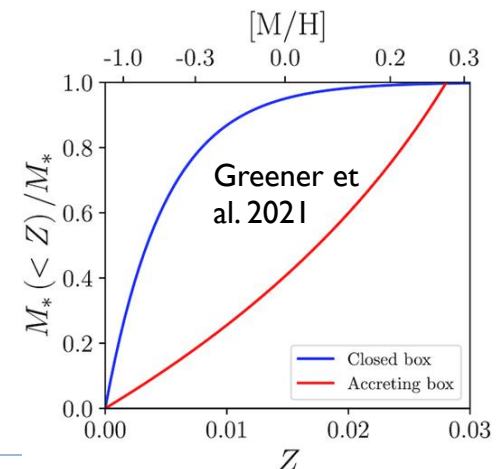
- ▶ $Z(t) = p \ln [M_g(t)/M_g(0)]$
- ▶ Implies gas-rich things should have lower Z
- ▶ Also: $M_s(<Z(t)) = M_g(0)[1 - e^{-Z(t)/p}] \rightarrow$

- ▶ We should see lots of really low metallicity G stars
- ▶ Something like 50% of G dwarfs should have $z < 0.25Z_\odot$!
- ▶ But we don't: closer to 25% for Fe and <1% for O
- ▶ → so-called G-dwarf problem

van den Bergh 1962

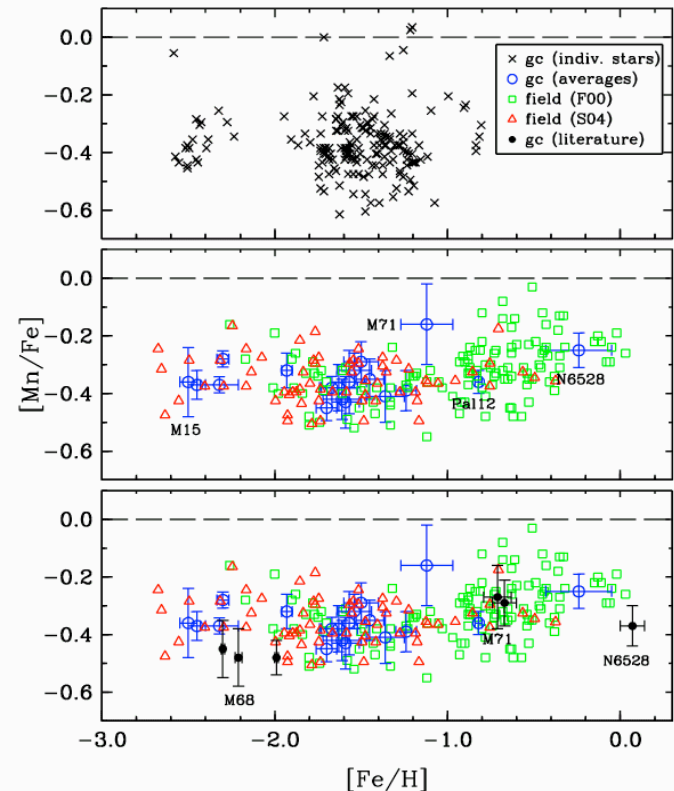
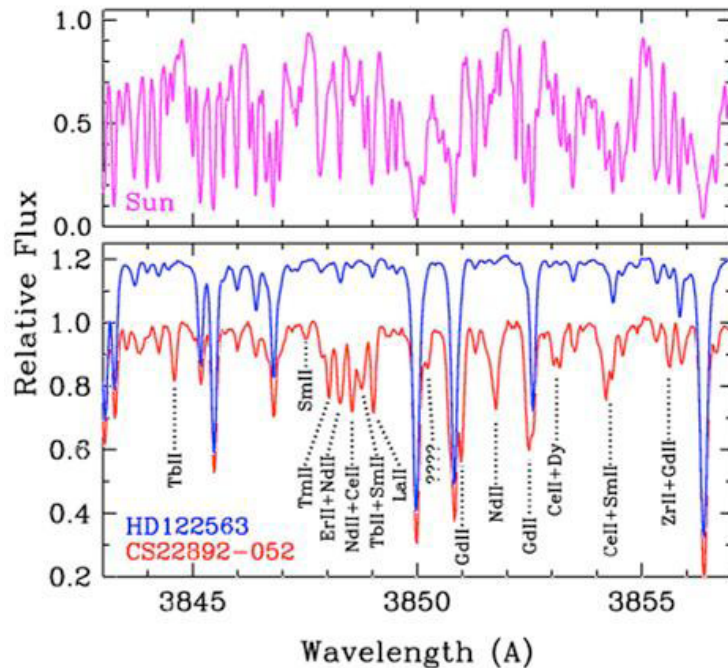
Binney & Merrifield, 1998 (5.3.1)

Pagel 2009



Summary: Chemical Evolution

- ▶ What is the correlation between these observed absorption lines and the star formation history of this stellar system? *Alt:* What are the constraints on how and when stars form based on their chemical abundances?



Summary: Chemical Evolution

- ▶ Other themes:
 - ▶ Disk gradients
 - ▶ Trends with galaxy luminosity
 - ▶ Abundance patterns in QSO absorbers
 - ▶ The G-dwarf problems

