

# Astronomy

# 730

## Disk Galaxies

# Outline

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- ▶ Disk Galaxies
  - ▶ Structural properties and trends
    - ▶ B/D decomposition
    - ▶ Spiral structure
  - ▶ Star-formation and feedback (see ISM Notes)
  - ▶ Kinematics
  - ▶ Scaling relations
  - ▶ Evolution:
    - ▶ Heating versus cooling
    - ▶ Disk heating model



# Disk Galaxies

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# Disk Galaxies: distribution of starlight

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- ▶ De-composition of the light profile
  - ▶ Disk – generally fit with an exponential or two
    - ▶  $I(r) = I_0 e^{-r/h_R}$
    - ▶  $I_0$  = central surface brightness
    - ▶  $h_R$  = scale length of the exponential
  - ▶ Bulge – generic function that goes as  $r^{1/n}$ 
    - ▶  $I(r) = I_e e^{-k} \text{ where } k = b_n [(r/r_e)^{1/n} - 1]$ 
      - Sersic profile:  $n=4$  fits many ellipticals;  $n=1$  is exponential;  $n=1/2$  is Gaussian
    - ▶  $I_e$  = effective surface brightness,  $r_e$  = effective radius :
      - where half the total light is enclosed
    - ▶  $b_n \sim 2n - 0.33$  for  $1 < n < 10$ .
    - ▶  $n = 1.7 \pm 0.7$  (Balcells et al. 2003)
  - ▶ Halo
    - ▶ Doesn't contribute much light, treat as extension of bulge



# Disk Galaxies: distribution of starlight

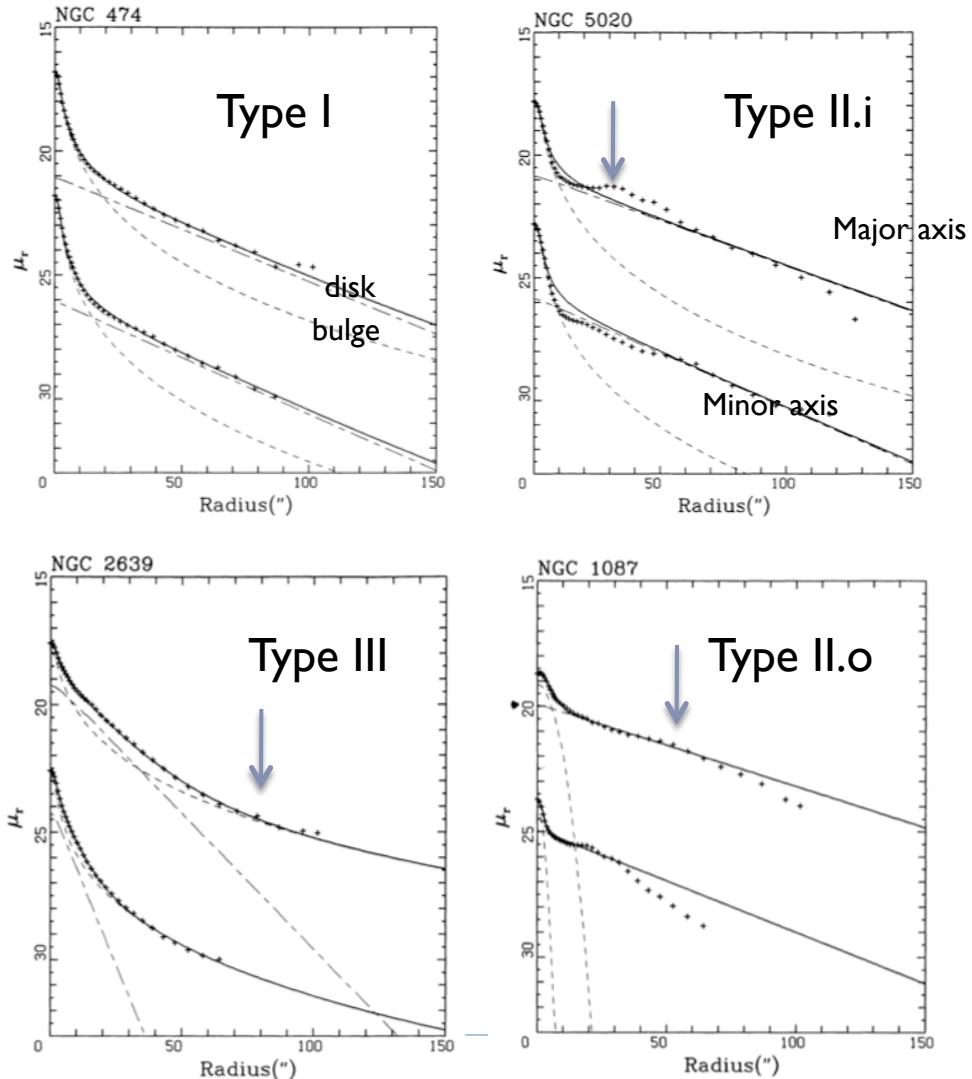
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- ▶ **Central surface brightness**
  - ▶ Usually measured in mag arcsec<sup>-2</sup> ( $\mu = -2.5 \log I + \text{const.}$ )
  - ▶ *It is independent of distance!* (ignoring cosmological dimming)
- ▶ **Freeman's law (1970):** luminous spirals have nearly constant disk central surface-brightness:
  - ▶  $\mu_0 = 21.65$  (B-band), 21 (R-band), 20.65 (I-band)  $\pm 0.65$  mag arcsec<sup>-2</sup>
    - ▶ Turns out to be a Malmquist-like bias; lower-luminosity systems have lower  $\mu_0$
- ▶ **Central surface-brightness for bulges:**
  - ▶ typically 10-100 times higher.
  - ▶ *Easy to see!*
- ▶ **Bulge-to-disk (B/D) luminosity ratio** a key parameter in describing disk-galaxies



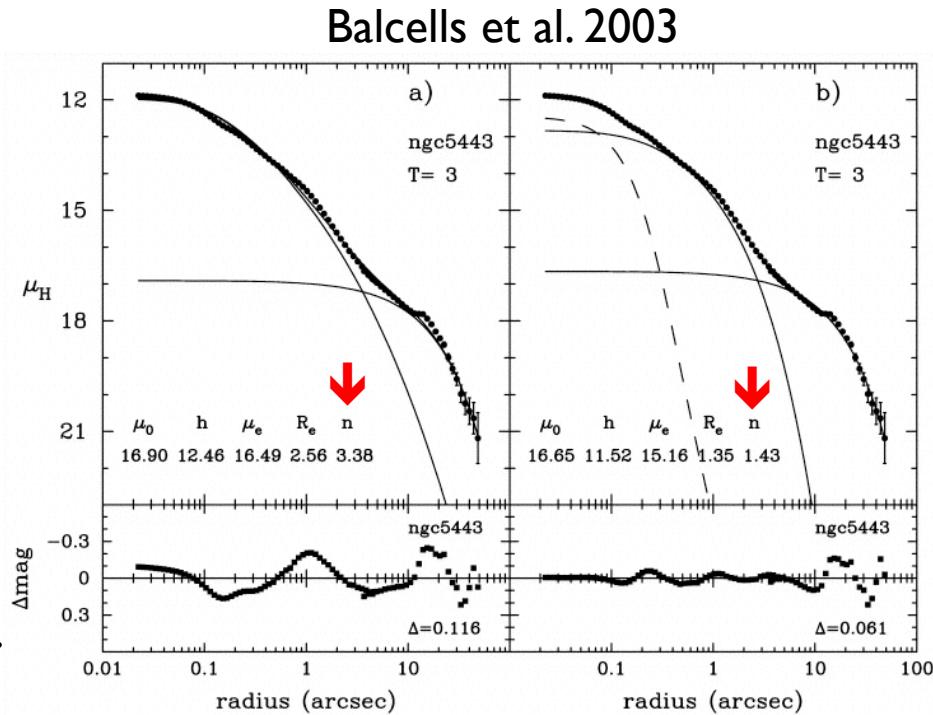
# Bulge/Disk decomposition

- ▶ Traditionally these have been done as 1D fits in radius (Kent 1985, ApJS, 59, 115) →
- ▶ Several distinct *disk* profile types:
  - ▶ Inner breaks (Freeman 1970)
    - ▶ Type I, II(.i)
  - ▶ Outer breaks (Erwin et al. 2006, Pohlen & Trujillo 2006, A&A, 454, 759)
    - ▶ Type II.o, III
- ▶ Most disks show smooth exponential behavior between  $1 < R/h_R < 4$
- ▶ Few extend far beyond  $R/h_R = 4$  in starlight



# Bulge/Disk decomposition

- ▶ Recent work has focused on high-resolution in the NIR to probe bulge structure
  - ▶ HST H-band SB profile: NGC 5443 (Sb).
    - ▶ (a) Solid lines = Sersic bulge + exponential disk
    - ▶ (b) Adding central point source in leads to a better fit
    - ▶  $\rightarrow n = 1.7 \pm 0.7$
    - ▶ w/o central source, overestimate  $n$ .
    - ▶ What is the cusp?
- ▶ Bulges have near-exponential radial light-profiles, like disks, but not highly flattened.
  - ▶ Heated inner disks?



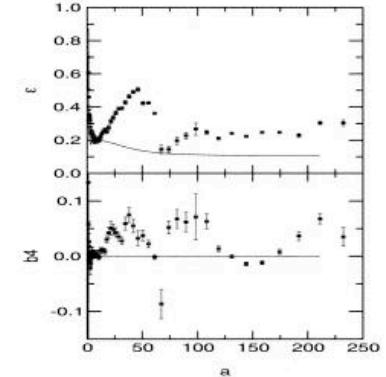
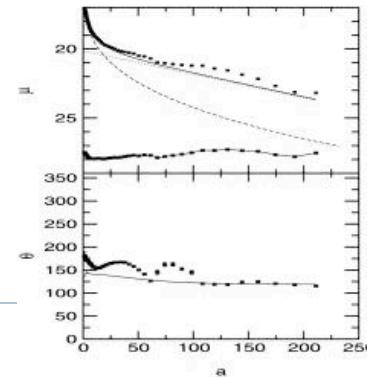
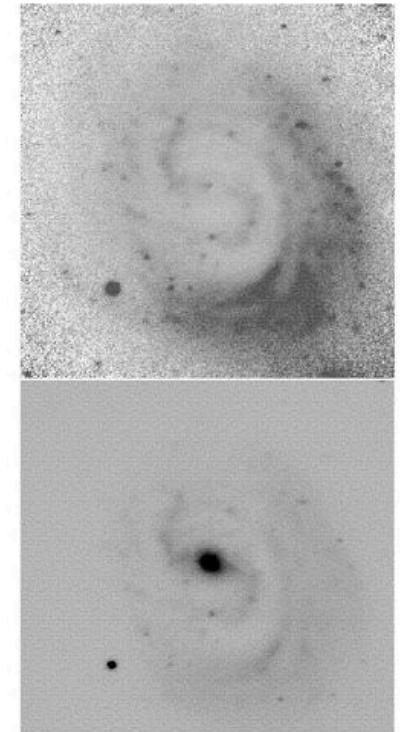
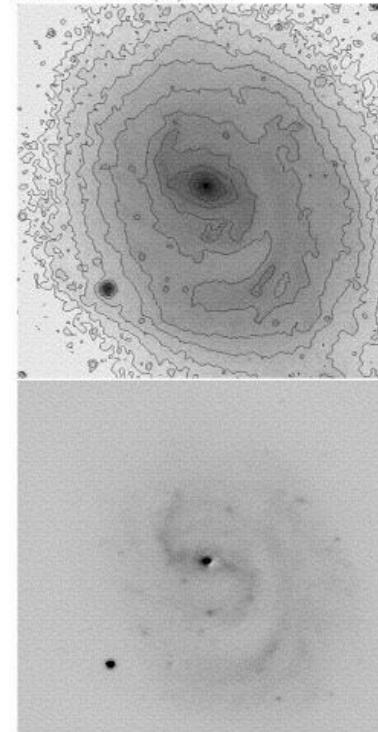
↓ core  
$$\rho_{\text{pseudo-isothermal}}(r) = \rho_0 [1 + (r/r_c)^2]^{-1}$$
$$\rho_{\text{NFW}}(r) = \rho_n (r/a_n)^{-1} [1 + (r/a_n)]^{-2}$$
  
↑ cusp

# Bulge/Disk decomposition

- ▶ Best modern methods do simultaneous fits of both *inclined exponential disk* and a *Sersic-profile bulge* in 2D
  - ▶ e.g., De Souza et al. 2004, ApJS, 153, 411
- ▶ Reveals wealth of residual structure:
  - ▶ Lopsidedness ( $m=1$ )
  - ▶ Bars, oval distortions ( $m=2$ )
  - ▶ spiral arms ( $m=2,3,\dots$ )

Fourier modes  $\uparrow$

N1637 - SABc(rs) - 200"



# Oval distortions

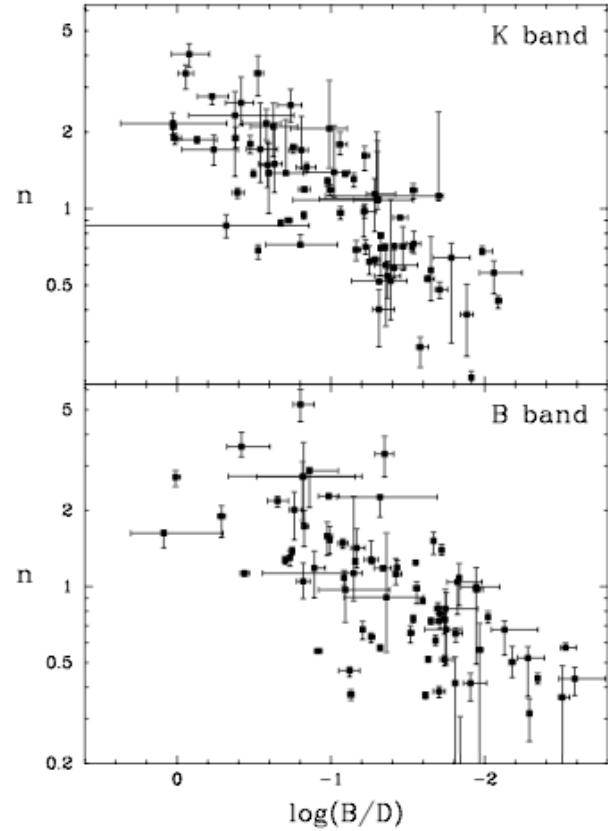
- ▶ 50% of disk galaxies have some sort of oval distortion
  - ▶ (bar, linear structure,  $m=1$  Fourier mode at center of galaxy):
    - ▶ stars and gas in largely radial orbits, precessing in phase.
    - ▶ More easily seen in red light (old stars), but often gas
- ▶ Outstanding questions:
  - ▶ Are bars *long-lived or short-lived phenomenon?*
    - ▶ Investigations of distant samples inconclusive.
      - e.g., Abraham et al. 1999, MNRAS, 308, 569
  - ▶ Do bars give rise to bulges?
    - ▶ e.g., pseudo-bulges (Kormendy & Freeman 2004)



NGC 1300

# Trends along Hubble sequence

- ▶ Important structural parameters:
  - ▶  $\mu_0$ ,  $h_R$ ,  $n$ , B/D ratio
- ▶ Also gas and stellar content
- ▶ Early → Late
  - ▶ Decreasing:
    - ▶ disk size ( $h_R$ ), disk surface-brightness  $\mu_0$
    - ▶ B/D and bulge Sersic index  $n$
    - ▶ Overall luminosity, rotation speed
    - ▶ metallicity, mean stellar age
  - ▶ Increasing:
    - ▶ gas content
    - ▶ star-formation (per unit mass)
    - ▶ disk thickness
    - ▶ Lopsidedness, asymmetry (i.e., *irregularity!*)



Graham 2001, AJ 121, 820

# Trends along Hubble sequence

- ▶ Kent (1985) showed that light-concentration (C) and mean surface-brightness ( $\mu_e$ ) correlated with each other, B/D, and the Morgan spectral type.
- ▶ → Requires no B/D decomposition to characterize disk systems

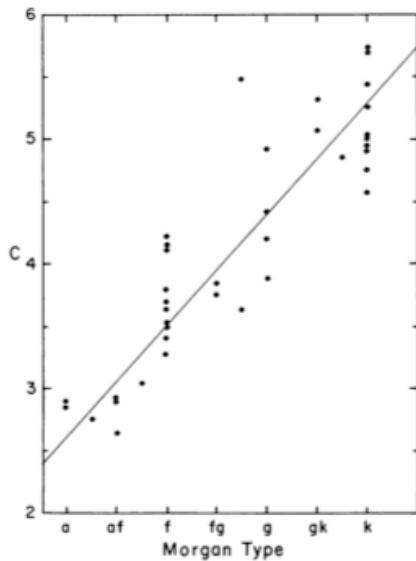


FIG. 9.—Correlation between concentration parameter  $c$  and Morgan type. The line drawn is an eyeball fit to the points.

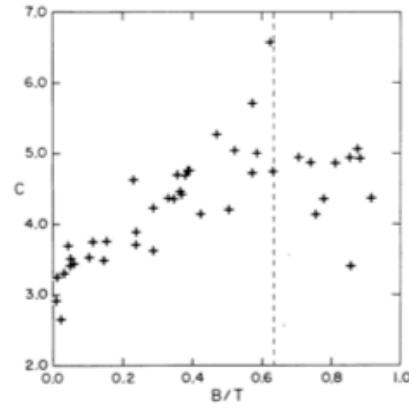


FIG. 10.—Correlation between concentration parameter  $c$  and  $B/T$ . Dashed line at  $B/T = 0.63$  marks the point where bulge/disk decompositions become unreliable.

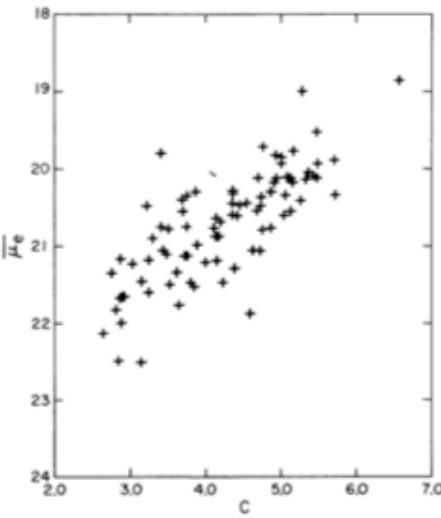
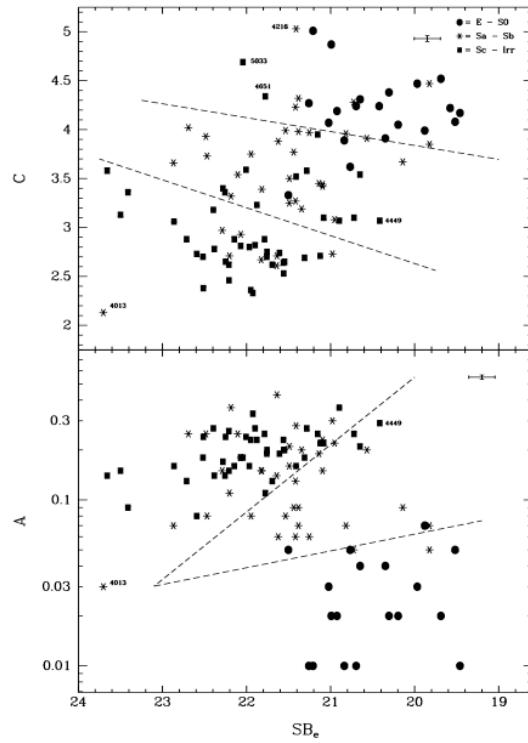
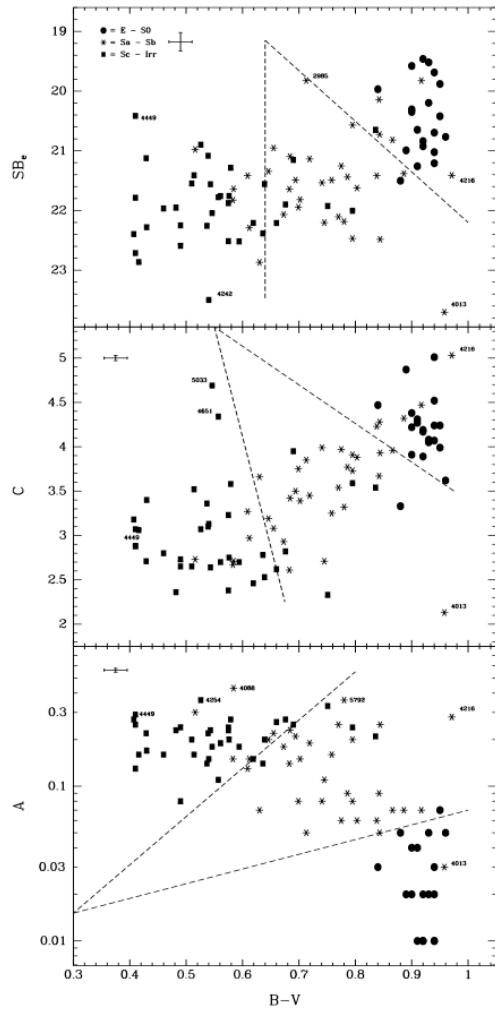
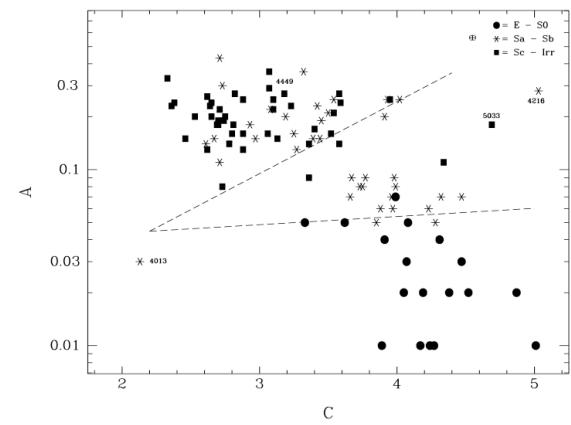


FIG. 12.—Correlation between mean surface brightness  $\mu_e$  inside effective radius  $r_e$  as a function of concentration parameter  $c$ .

# Alternative classifications



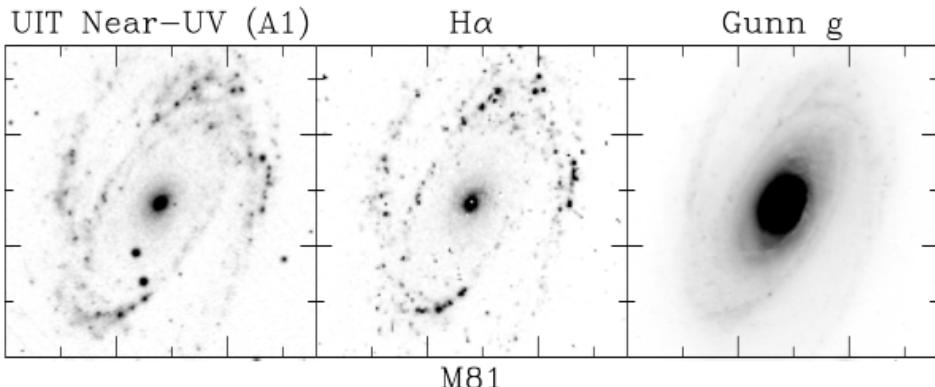
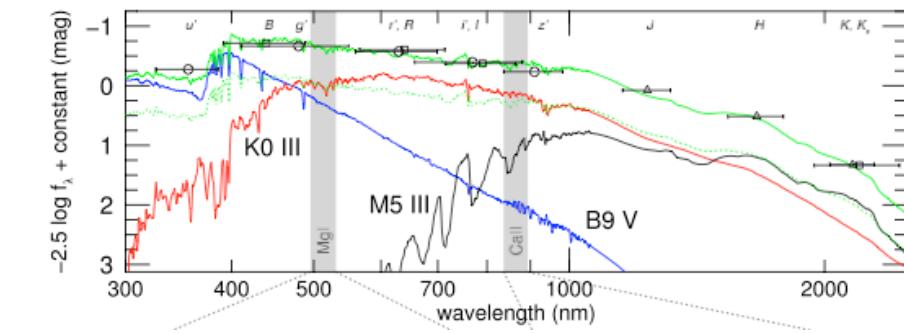
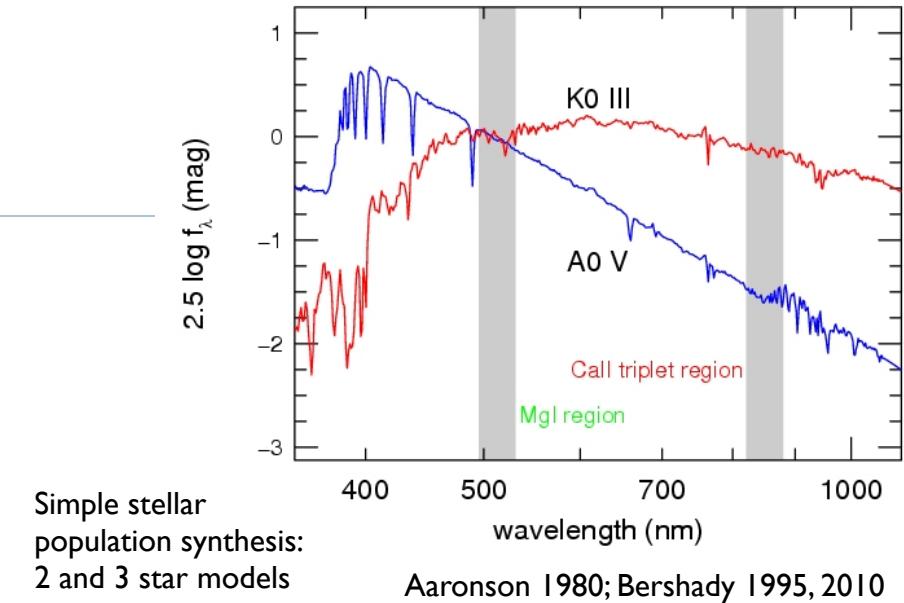
Bershady et al. 2001  
Conselice et al. 2001



Mean surface-brightness ( $SB_e = \mu_e$ ), image concentration ( $C$ ) and asymmetry ( $A$ ) correlate with color (stellar populations)

# Optical vs NIR view

- ▶ Modern measurements
  - ▶ Digital detectors: CCDs or IR arrays
- ▶ Hot stars emit relatively little in the near-IR compared to cool stars of comparable total (bolometric) luminosity.
- ▶ Giant stars emit much of their radiation in near-IR
  - ▶ → Galaxies appear less “splotchy” in the red and NIR because you see mostly the cool, older stars that are relaxed.
  - ▶ Effects of extinction mitigated:
    - ▶  $A \equiv -2.5 \log(I_{\text{obs}}/I_{\text{em}}) = 1.065 \tau$ , where  $\tau$  is optical depth, and goes as  $\sim \lambda^{-1}$
    - ▶ more accurate view of the stellar distribution.



# Spiral arms

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- ▶ Recall Hubble's classification criteria
  - ▶ Openness of arms
  - ▶ Resolution of arms into “stars”
  - ▶ Bulge/disk ratio
    - ▶ **Sa** - tightly wound, large b/d ratio, some gas, steeply rising rotation curves
    - ▶ **Sb** - intermediate
    - ▶ **Sc** - open spiral arms, lots of substructure, small bulge, lots of gas, slowly rising rotation curves, lots of HII regions
    - ▶ **Sd** - no bulge, open arms, lots of HII regions
    - ▶ **Sm** - lopsided (like LMC)



# Spiral sequence

Sb  
M31



Sm  
LMC



Sc  
M101



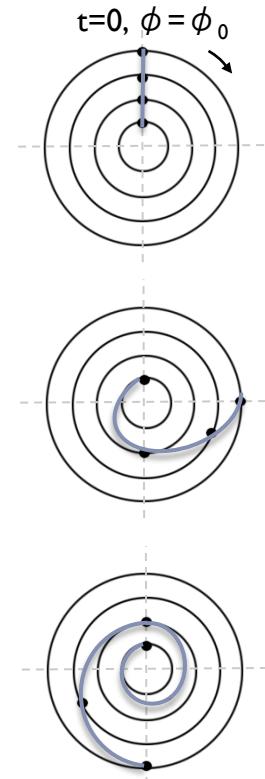
Sd  
M33



# Spiral arms: winding problem?

## ▶ Assumptions:

- ▶ Start with an arm as a straight radial strip at  $t = 0$  and  $\phi = \phi_0$ .
- ▶ Pattern speed of arm is locked to the rotation of the disk:  $\omega_p = \omega(R)$ .
- ▶ Disk rotates with  $\omega(R) = V(R)/R \neq \text{constant}$
- ▶ In general  $V(R) \sim \text{constant}$  over most of the disk.
- ▶ → Within a few  $\langle t_{\text{dyn}} \rangle$ , arms wrap up
  - ▶ Recall  $t_{\text{dyn}} \sim T/4$
  - ▶ For  $V = 220 \text{ km/s}$ ,  $R = 8.5 \text{ kpc}$ ...  $T = 2.4 \times 10^5 \text{ yr}$



# Winding problem resolutions

- ▶ There is likely no one solution, so the situation is complicated:
  - ▶ Arms are constantly regenerated.
    - ▶ Transient phenomenon (interactions?)
    - ▶ Star-formation generated/stochastic wave
      - Might be a suitable explanation for flocculent spirals
  - ▶ Kinematic wave:
    - ▶ Nesting of oval orbits (see S&G Figure 5.29)
    - ▶ Still a winding problem, but twice as slow as for case where  $\omega_p = \omega(R)$ .
      - Might be suitable for spirals in gas-free disks
  - ▶ “Density wave” arising in the gravitational potential
    - ▶ Stars and gas gravitational attraction offset kinematic wave from winding up by making  $\omega_p(R) = \text{constant}$ .
    - ▶ Disk stability must be low:
      - $Q = (\sigma_R \kappa) / 3.36\pi G \Sigma \sim 1$  ratio of kinetic : potential energy

Random motions

Epicyclic frequency

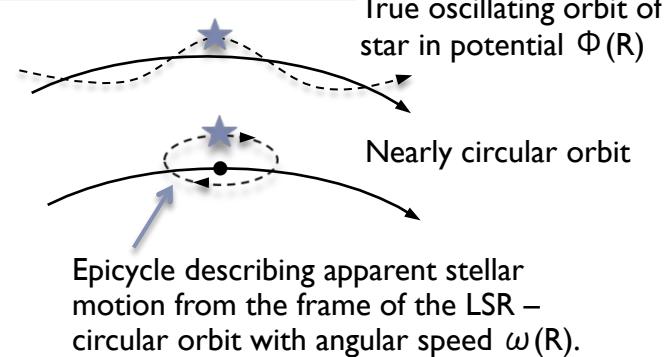
Disk mass surface-density



# Density waves

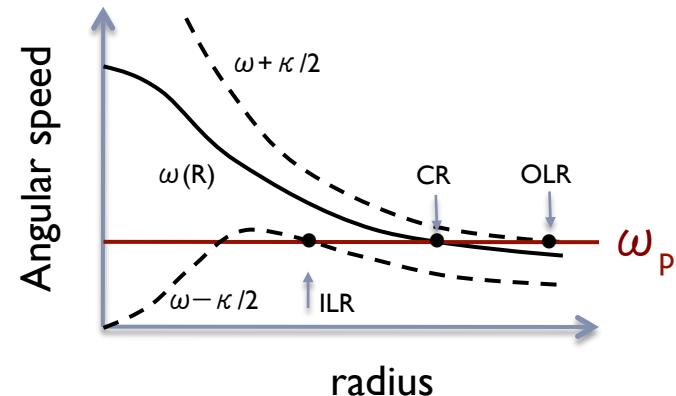
- ▶ Epicycles: stars oscillations (random motions) about circular orbit described as elliptical epicycles with frequency  $\kappa$ .
  - ▶  $\kappa^2(R) = -4B(R) \omega(R)$
  - ▶  $B = \text{(Oort's constant)}$
- ▶ Spiral is strengthened when
  - ▶  $m|\omega_p - \omega(R)| < \kappa(R)$
  - ▶  $m = \text{number of arms}$
- ▶ Continuous wave propagates only between inner and outer Linblad resonances:
  - ▶  $\omega_p = \omega(R) - \kappa/m$  (ILR)
  - ▶  $\omega_p = \omega(R) + \kappa/m$  (OLR)
- ▶ Co-rotation (CR):  $\omega_p = \omega(R)$
- ▶ Beginning and end of spirals arms indicate location of resonances

In the disk plane:



There's also a component out of the disk plane ( $z$ ) -- not relevant here.

Schematic for  $m=2$ :



# Star Formation and Feedback

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- ▶ See ISM Notes.



# Disk Galaxy Kinematics: 3D

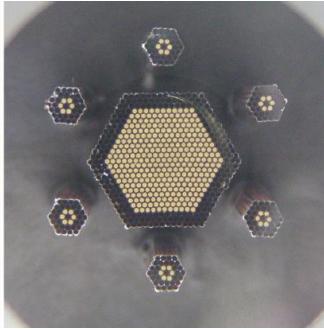
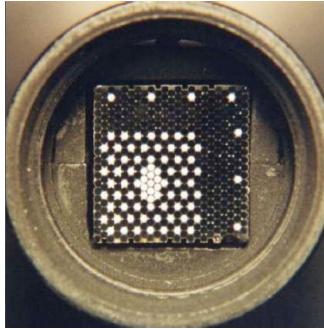
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- ▶ From easy to hard:
  - ▶ Ionized gas kinematics based on centroids of the optical emission lines ([OII], [OIII], H $\alpha$ ).
  - ▶ HI kinematics based on radio interferometric studies.
  - ▶ Stellar velocity fields and dispersions largely based on centroids and widths of stellar absorption lines.
    - ▶ We'll come back to this.



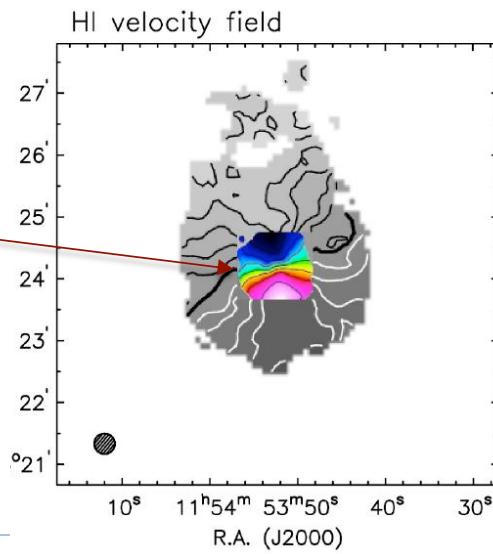
# Disk Galaxy Kinematics: 3D

- ▶ Optical fibers and image slicers...
  - ▶ ....feeding conventional long-slit spectrographs...
  - ▶ ....have opened up 2D mapping of disk velocities (3D data = data cube).
- ▶ Data cubes:
  - ▶ Once only the domain of radio astronomy, where we could probe only neutral or molecular gas
  - ▶ We can now probe ionized gas and stars, much more quickly.
- ▶ *Why bother with radio ??* Here's just one of several critical reasons:

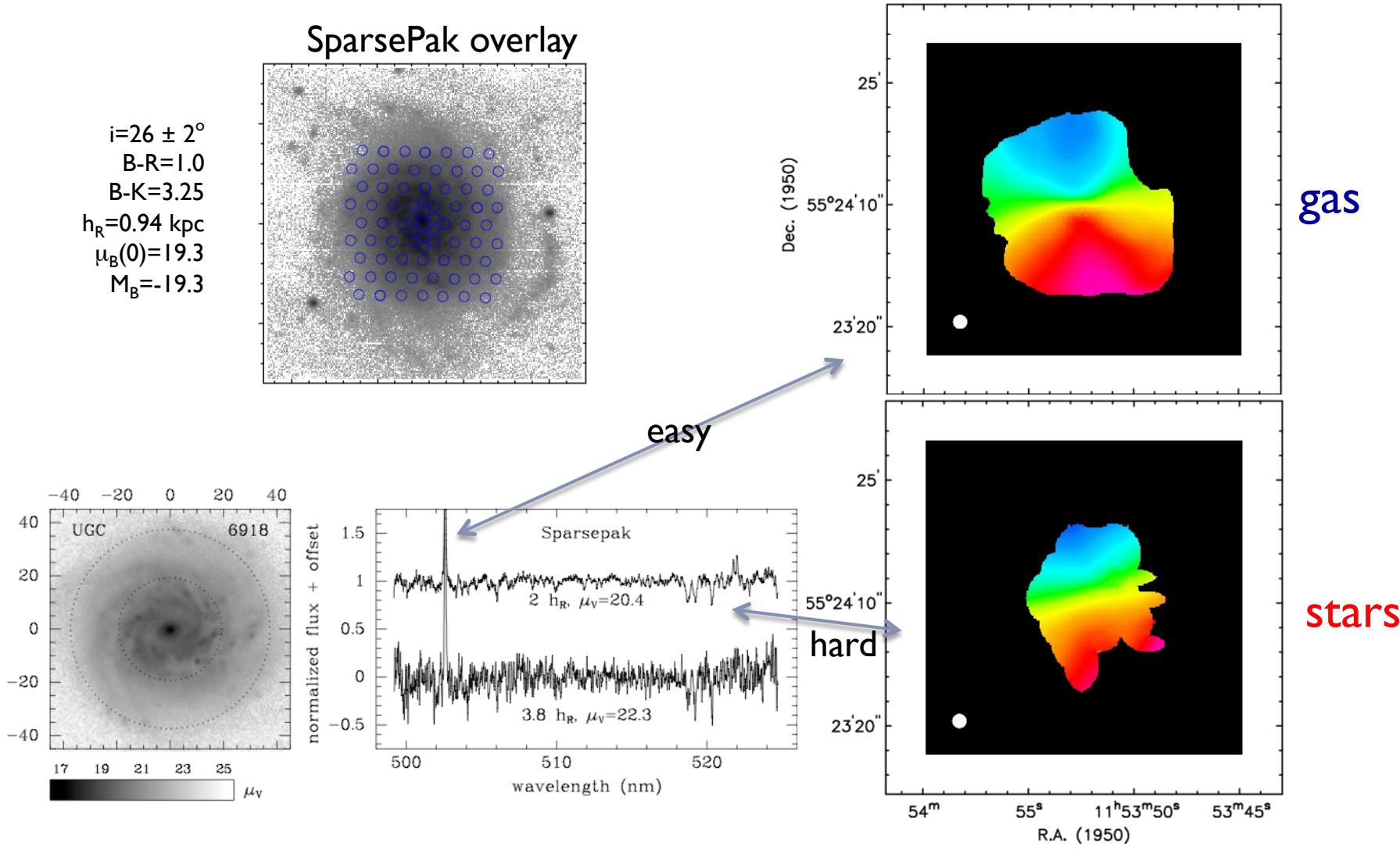


- ▶ WIYN 3.5m/ SparsePak FFU
  - ▶ 82 fibers, 4.7" diameter
  - ▶ 72" FOV
  - ▶  $\lambda/\Delta\lambda = 11,000$
- ▶ (Bershady et al.'04,'05)
- ▶ Calar Alto 3.5m / PPak IFU
  - ▶ 331 fibers, 2.7" diameter
  - ▶ 75" FOV
  - ▶  $\lambda/\Delta\lambda = 8000$
- ▶ (Verheijen et al.'05)

H $\alpha$



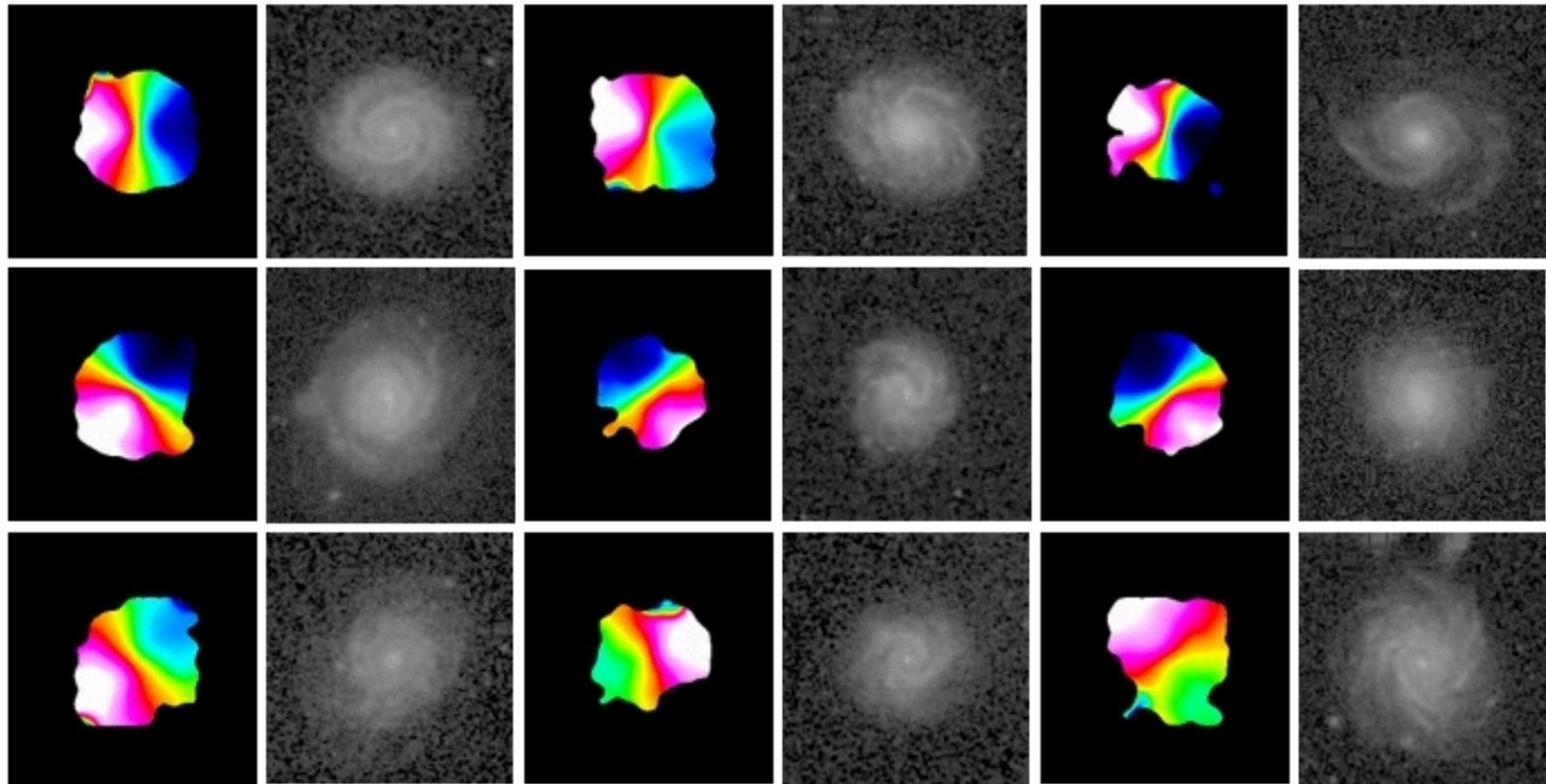
# Disk kinematics: UGC 6918 = NGC 3982



# Symmetric, normal galaxies

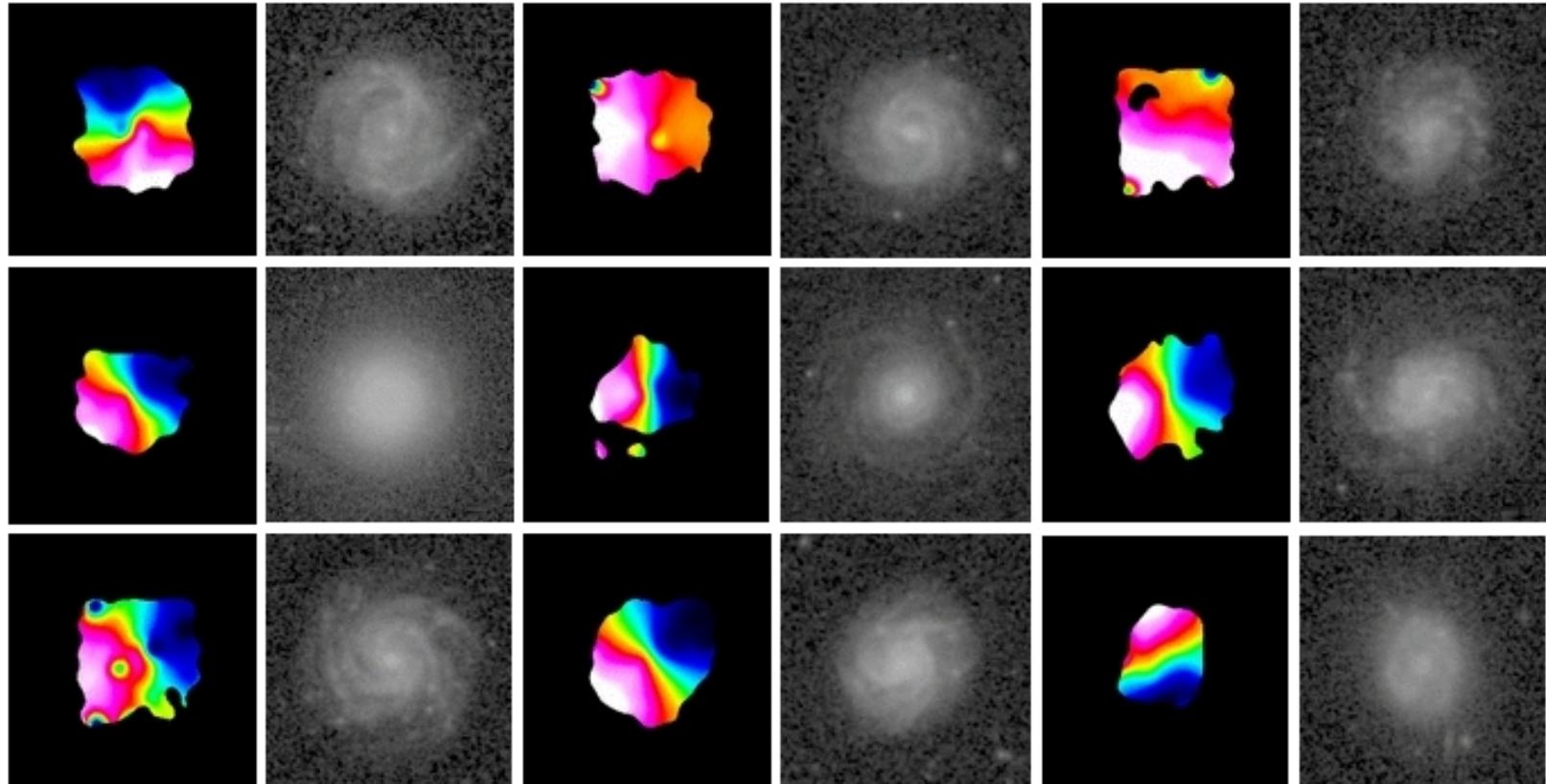
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WIYN/SparsePak H $\alpha$  velocity fields



# Bi-symmetries and Asymmetries

WIYN/SparsePak H $\alpha$  velocity fields



This is easy: 1hr in bright-time on a 3.5m telescope



# Radio Telescopes

Single dish: Green Bank



Interferometers: VLA



# HI Kinematics of Disk Galaxies

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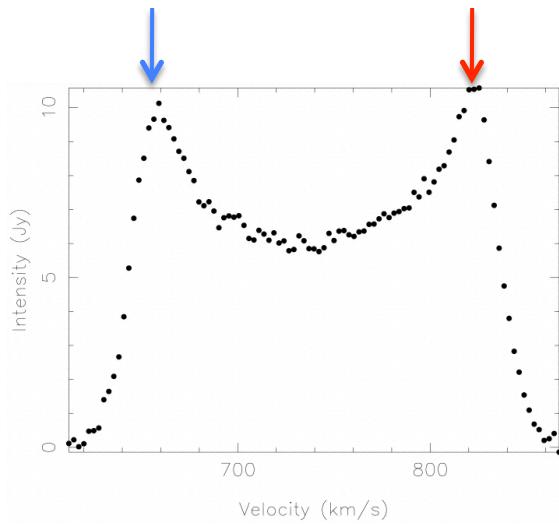
- ▶ Until the last decade, this has been the only source of bi-dimensional kinematics of external galaxies.
- ▶ Interferometric observations yield a 3-dimensional map (a data cube) of the distribution and kinematics of HI
  - ▶ → x,y,z (RA, DEC, velocity).
    - ▶ Moment 0 = total intensity (integrate over v)
    - ▶ Moment 1 = velocity field (mean velocity as function of position)
    - ▶ Moment 2 = velocity dispersion
    - ▶ etc. (skew, kurtosis)
  - ▶ These concepts are generic and apply to all line data, e.g., optical emission lines, stellar absorption lines.
  - ▶ HI data cubes take 10's of hours to collect on the world's biggest interferometers.



# Single-dish vs Interferometer

- ▶ Sensitivity vs spatial information
- ▶ Analogous to single-fiber vs IFU

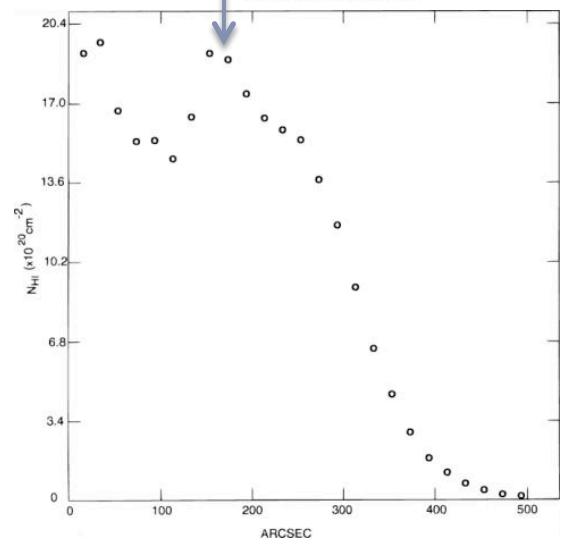
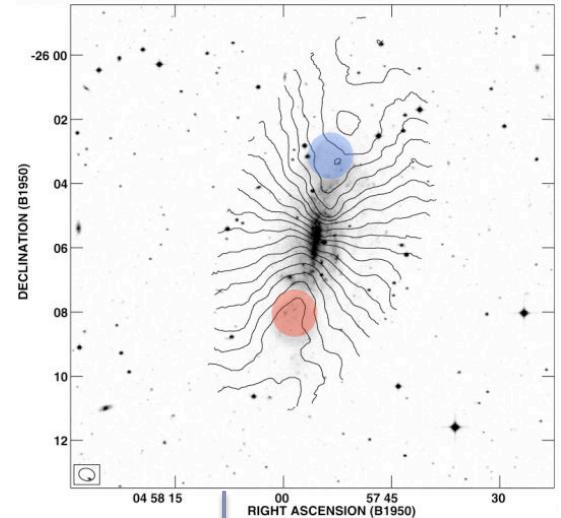
Single dish:



Interferometer:

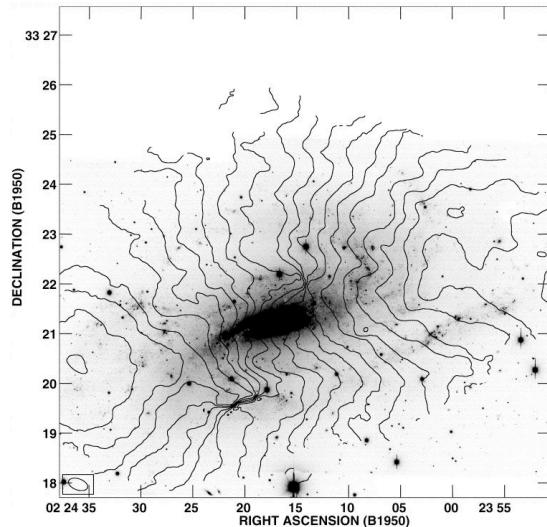
Velocity field:

Radial profile:



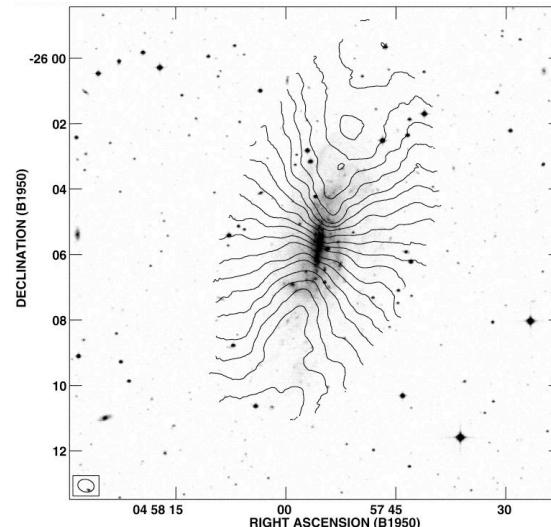
# HI spider diagrams

**Moderate inclination:**  
Note beam size relative to  
optical structure.



**Highly inclined:**

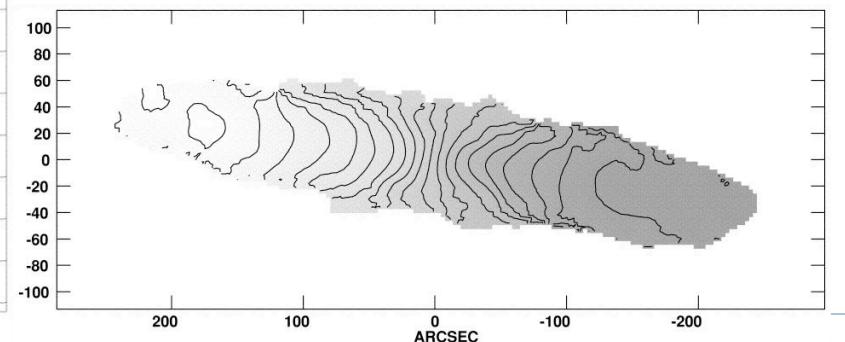
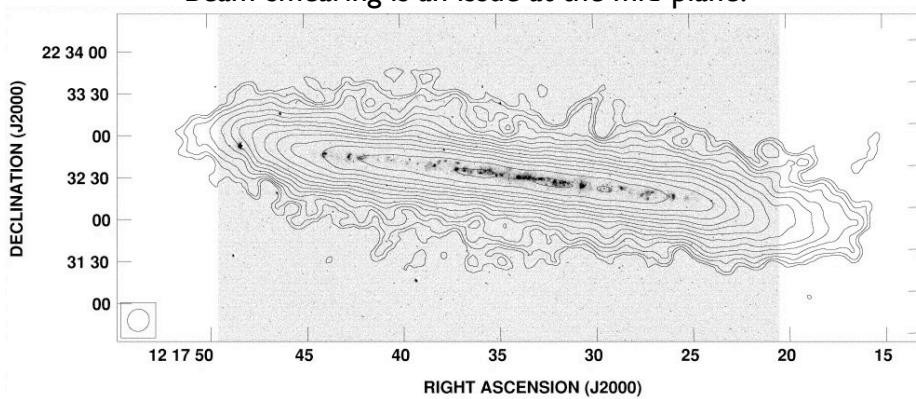
NGC 925



NGC 1744

0<sup>th</sup> moment map superimposed on optical image.  
Beam-smearing is an issue at the mid-plane.

1<sup>st</sup> moment map = Velocity field



1<sup>st</sup>  
moment  
maps =  
velocity  
field

# Deriving the rotation curve

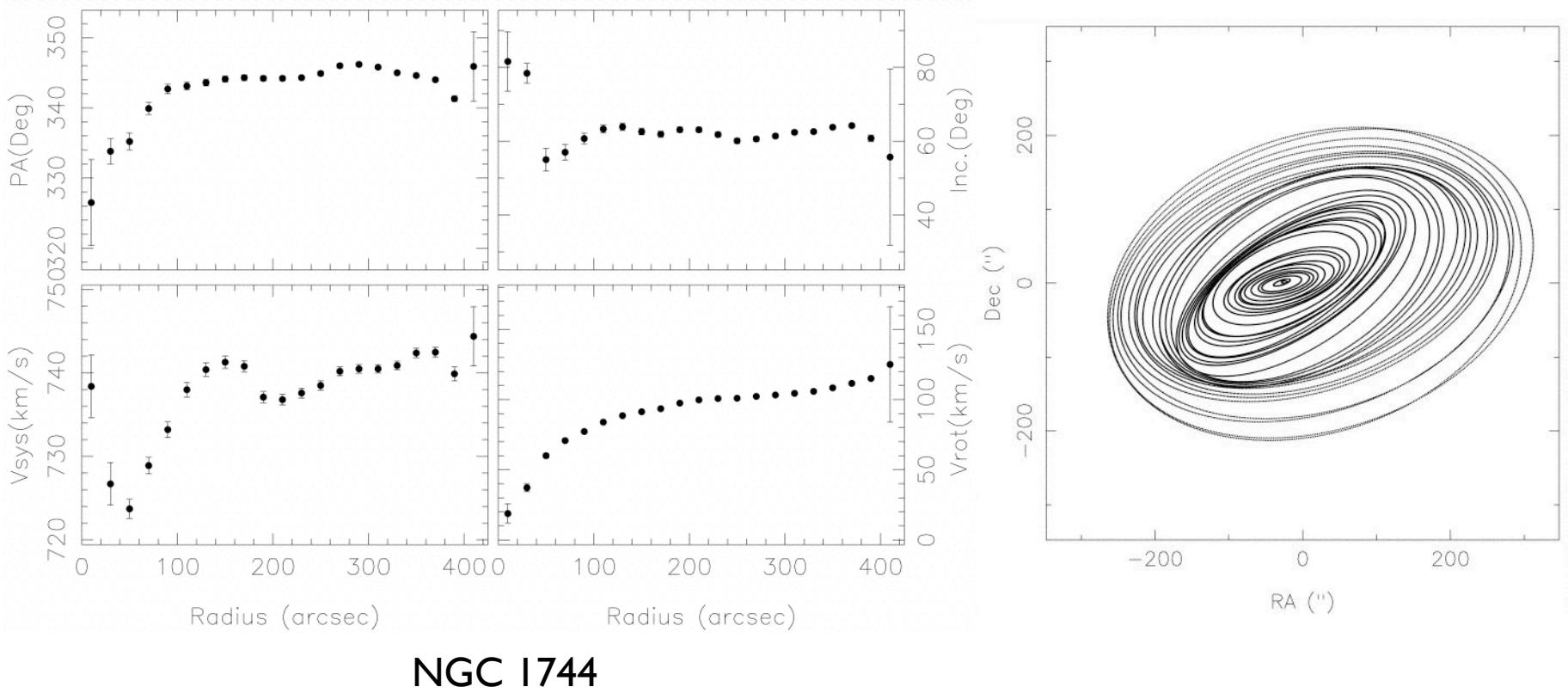
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- ▶ We only measure the radial velocity (i.e. velocity along the line of sight). How do we translate this into a velocity field?
- ▶ Components
  - ▶ Systemic velocity (e.g. Hubble flow)
  - ▶ Inclination,  $i$ , (i.e. if its face-on we see no rotation)
  - ▶ Azimuthal angle (of the major axis)
  - ▶  $V_c = V_{SYS} + V(R)(\sin i)(\cos \phi)$



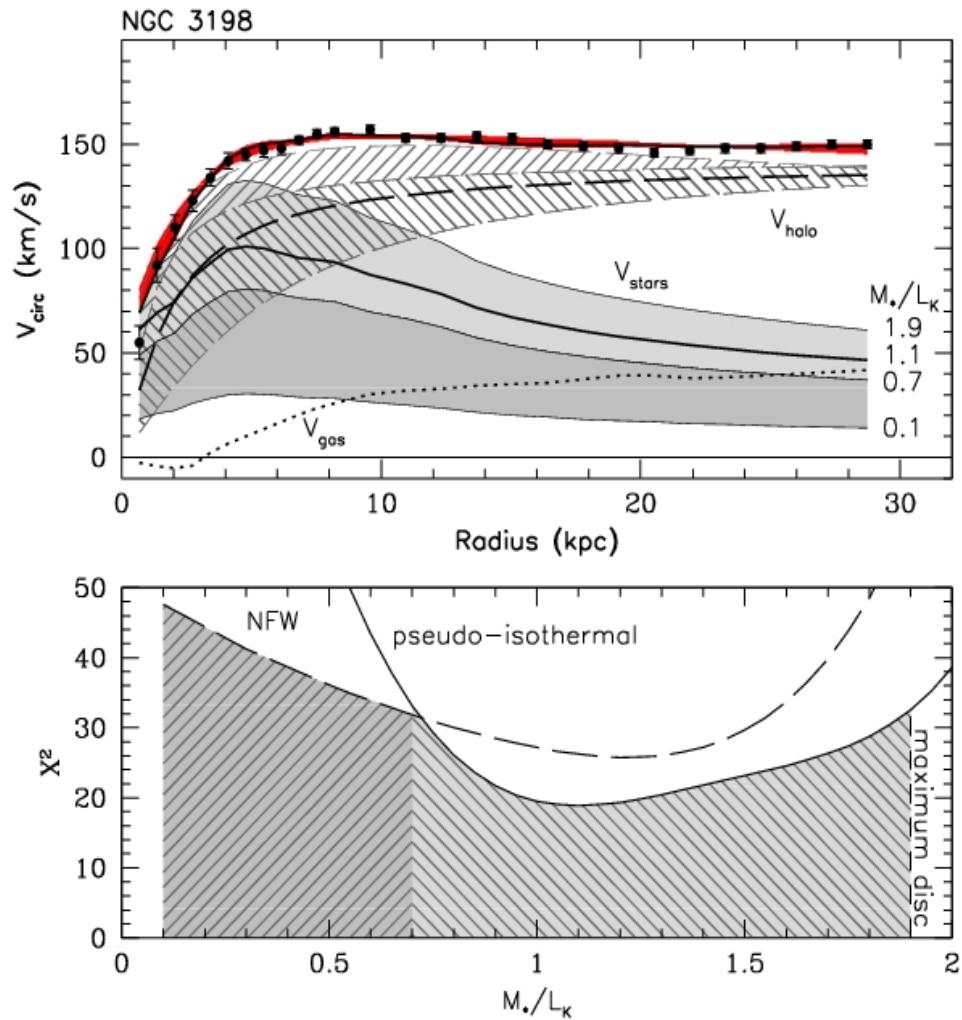
# Deriving the rotation curve

- ▶ Tilted ring models allow you to fit the circular velocity, inclination, position angle as a function of radius.



# Deriving the rotation curve

- ▶ But it's still just a rotation curve, degenerate to disk+halo, good for estimating total mass only.

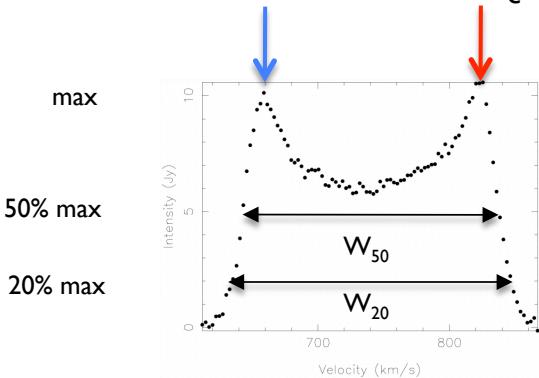


# Surrogates measures of rotation

## ► Spatial information vs sensitivity:

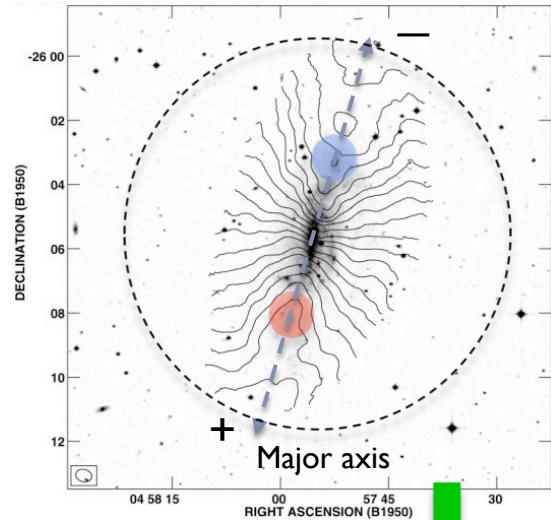
### 4. Single dish (fiber):

Line width  $W \sim 2V_c$



### I. Interferometer/IFU:

→ Velocity field  
2D map of velocities,  
or data cube

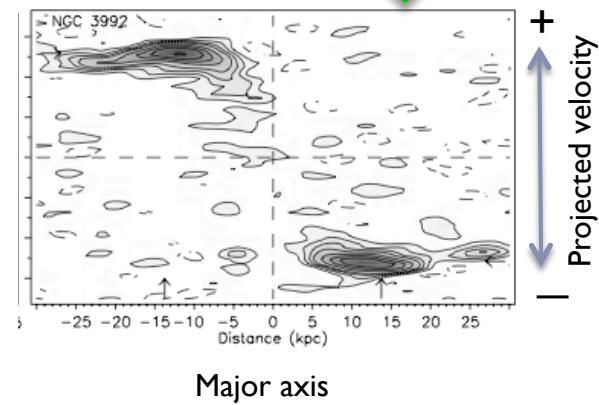
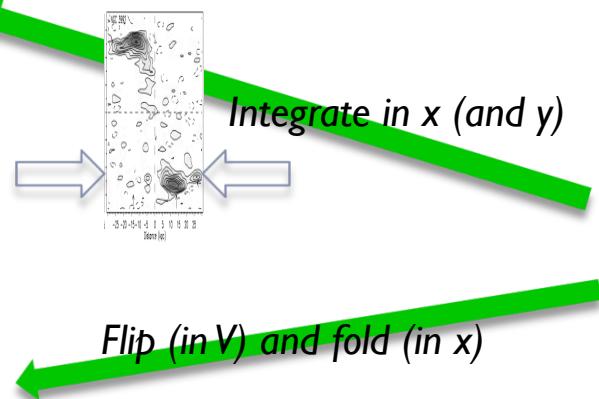
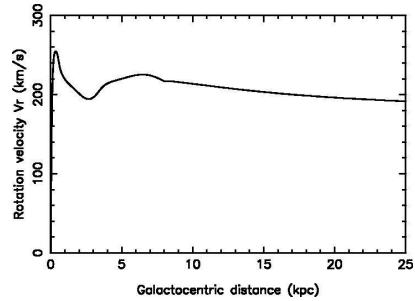


### 2. Position-velocity diagram (PVD):

Equivalent to long-slit spectrum

*Slice down the major axis*

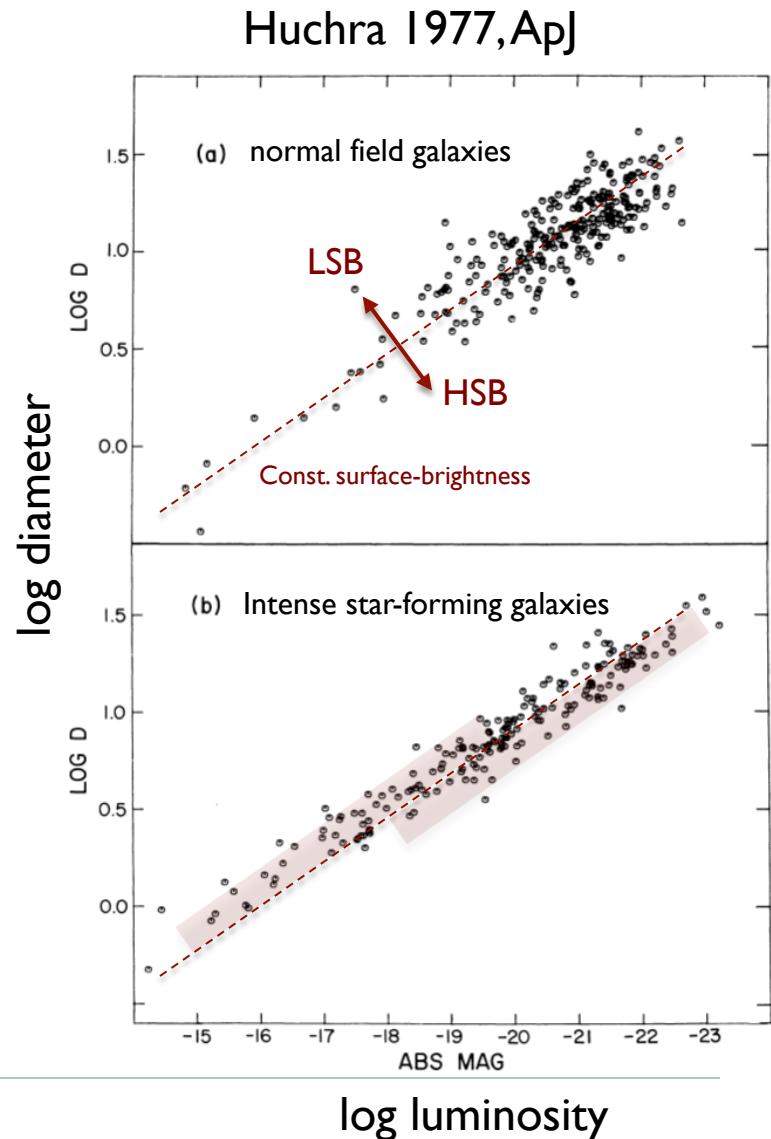
### 3. Rotation curve



# Scaling relations

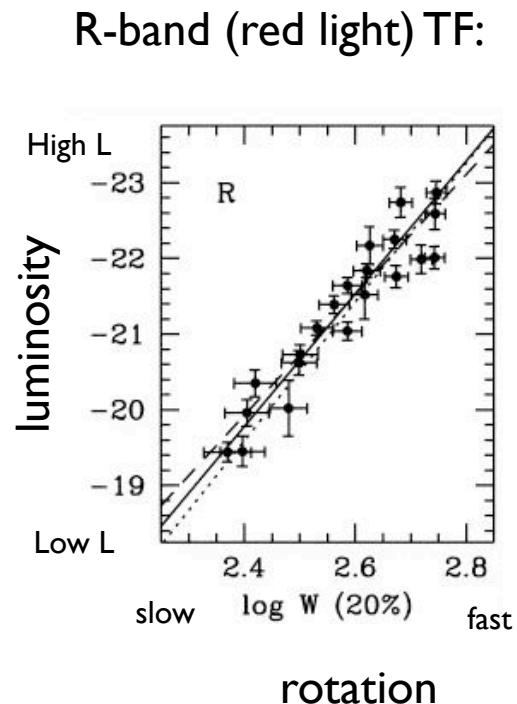
- ▶ **V, L, size correlate (the physical scale of disk systems)**
  - ▶ “Larger” systems tend to have higher disk surface-brightness, older stellar populations, less gas, higher metallicity (i.e., the Hubble Sequence)
- ▶ **Important 2<sup>nd</sup>-order effect:**
  - ▶ matter-density increases with V, L, size
    - ▶ concentration, surface-brightness
    - ▶  $\rightarrow$  dynamical time-scales decrease
    - $$t_{\text{dyn}} \sim \sqrt{1/G \rho}$$
    - ▶  $\rightarrow$  SFR, gas consumption and enrichment more rapid
    - ▶  $\rightarrow$  drives Hubble Sequence ???

*At some level it must.*



# Scaling relations *continued*

- ▶ What about mass?
  - ▶ The tightest correlation for disk galaxies is between  $V$  and  $L$ . This is called the **Tully-Fisher (TF) relation**



# Tully-Fisher relation: Measurement

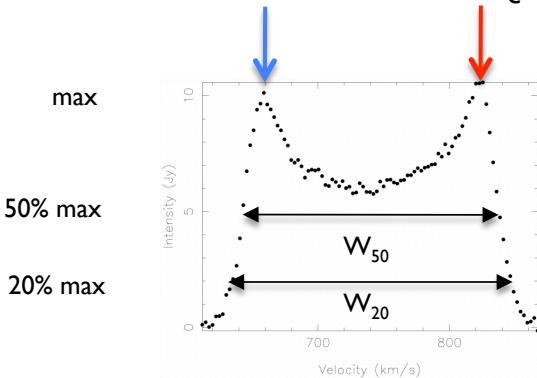
- ▶ Details of the measurement
- ▶ Velocity:
  - ▶ Measure of circular rotation
    - ▶ line-width or rotation curve
  - ▶ Corrections:
    - ▶ inclination ( $1/\sin i$ )
    - ▶ turbulent broadening (if line width)
- ▶ Luminosity:
  - ▶ Corrections:
    - ▶ total flux
    - ▶ Galactic extinction
    - ▶ internal extinction (which depends on inclination)
    - ▶ distance
      - distance modulus
      - redshifting of band-pass, the so-called “k” correction
- ▶ Inclination:
  - ▶ Axial ratios of light profile (photometric ellipticity)
    - ▶ Correct for disk oblateness
  - ▶ Shape of iso-velocity contours (if 2D kinematics are available)

# Surrogates measures of rotation

## ► Spatial information vs sensitivity:

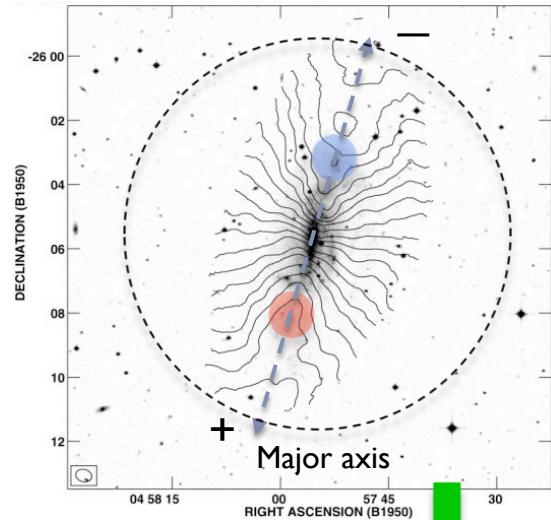
### 4. Single dish (fiber):

Line width  $W \sim 2V_c$



### I. Interferometer/IFU:

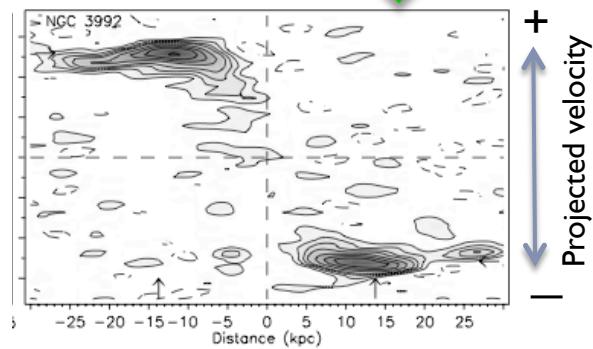
→ Velocity field  
2D map of velocities,  
or data cube



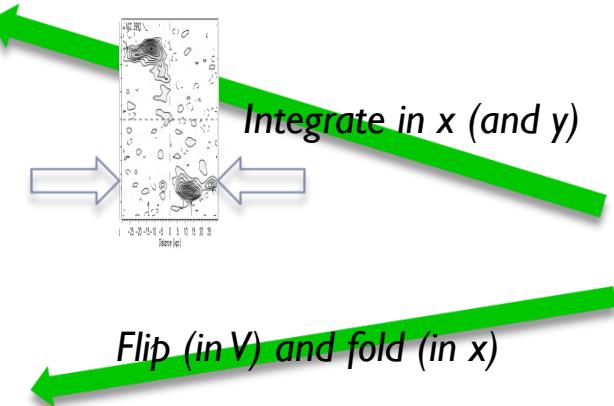
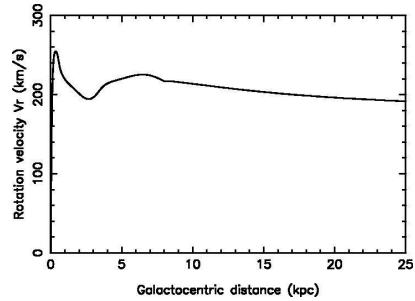
### 2. Position-velocity diagram (PVD):

Equivalent to long-slit spectrum

*Slice down the major axis*



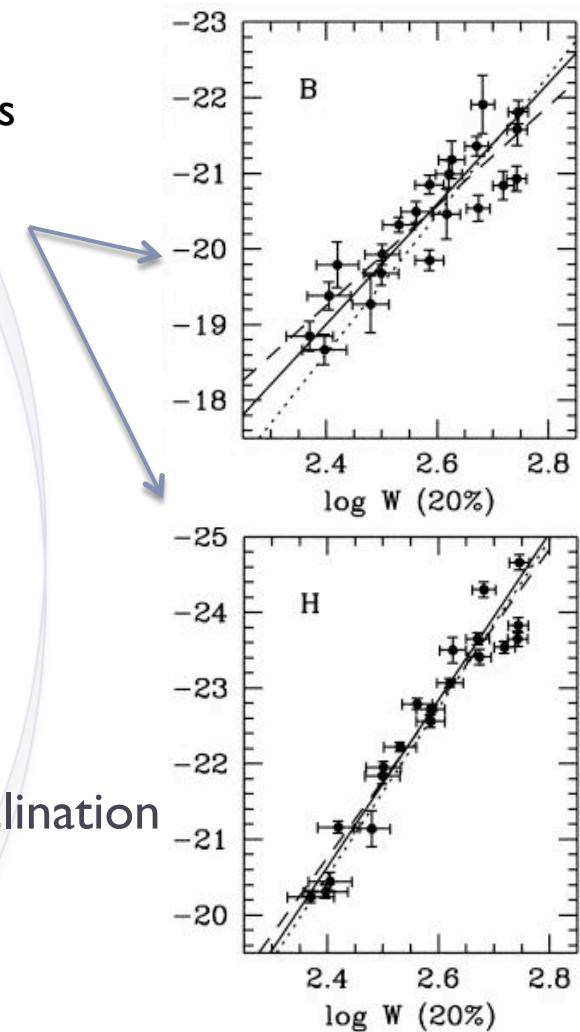
### 3. Rotation curve



# Tully-Fisher relationship: Scatter

- ▶ **Small!**
  - ▶ 0.5-0.3 mag in blue (B,  $0.44 \mu\text{m}$ )
  - ▶ 0.1 mag in near-IR (H,  $1.6 \mu\text{m}$ )
  - ▶ 0 mag (!) *intrinsic*: K-band for subset of galaxies with rotation curves and flat  $V(R)$  (Verheijen 2001)
    - ▶ *Too small?*
- ▶ **Source of dispersion**
  - ▶ Measurement errors (random)
  - ▶ Measurement errors (systematic)
    - ▶ Extinction
    - ▶ Shape of light-distribution (oblateness) → inclination
    - ▶ Shape of rotation curve →  $V_c$
  - ▶ Cosmic variance
    - ▶ Variations in M/L with galaxy type

Why this trend?



gasp!

# Tully-Fisher relation: Implications

---

- ▶ Why is M/L so constant from galaxy to galaxy?
  - ▶ Here we're talking about M/L of the entire galaxy:
    - ▶ Mass is dominated by dark halo
    - ▶ Luminosity is dominated by disk
  - ▶ Total mass:  $M \propto [V_{\max}^2 h_R]$
  - ▶ Total luminosity:  $L \propto [I_0 h_R^2]$  (ignoring bulge)
  - ▶  $\rightarrow L \propto [V_{\max}^4 (M/L)^{-2} I_0^{-1}]$
  - ▶ A universal M/L implies remarkable constancy of the ratio of dark to luminous matter
    - ▶ Or worse, a fine-tuning of the dark-to-luminous mass ratio as the stellar M/L varies.
- ▶ What does this tell us about galaxy formation and feedback?



# Tully-Fisher relation: diagnostic tool

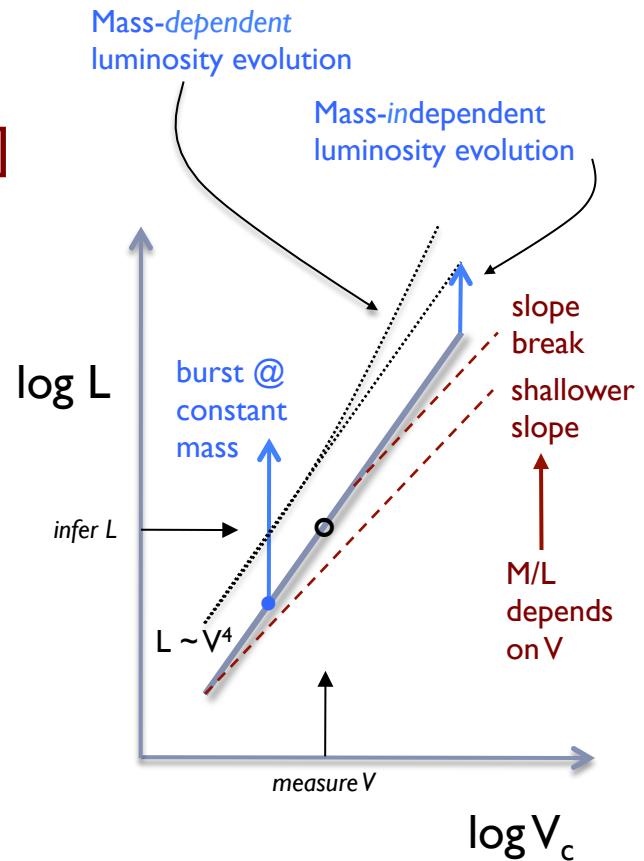
- ▶ Standard candle:  $V$  is distance-independent

- ▶ Structural probe: slope and scatter

- ▶ Since  $L$  is proportional to  $[V_{\max}^4 (M/L)^{-2} I_0^{-1}]$
- ▶ →  $M$  vs  $\log(V)$  should have slope of 10
- ▶ and should depend on surface-brightness
  - ▶ Slope is  $< 10$ , varies with wavelength
  - ▶ No dependence on surface-brightness

- ▶ Evolutionary probe

- ▶ Changes in  $M/L$  with time
  - ▶ Assume  $M$  roughly constant
    - Secular changes in  $L$ : star-formation history
    - Stochastic changes in  $L$  (star-formation bursts)
      - Scatter increases with burst duty-cycle



# Disk heating in the solar neighborhood

- ▶ For a disk in equilibrium the Virial theorem implies  $\sigma_z^2/h_z$  ought to be a constant for any given stellar-population age in the disk

tracer	$h_z$ (pc)	$\sigma_z$ (km/s)	$\sigma_z^2/h_z$
OV	50	6	0.7
BV	60	6	0.8
AV	120	9	0.7
FV	190	13	0.9
GV	350	17	0.8
KV	340	14	0.6
K III	270	16	1.0

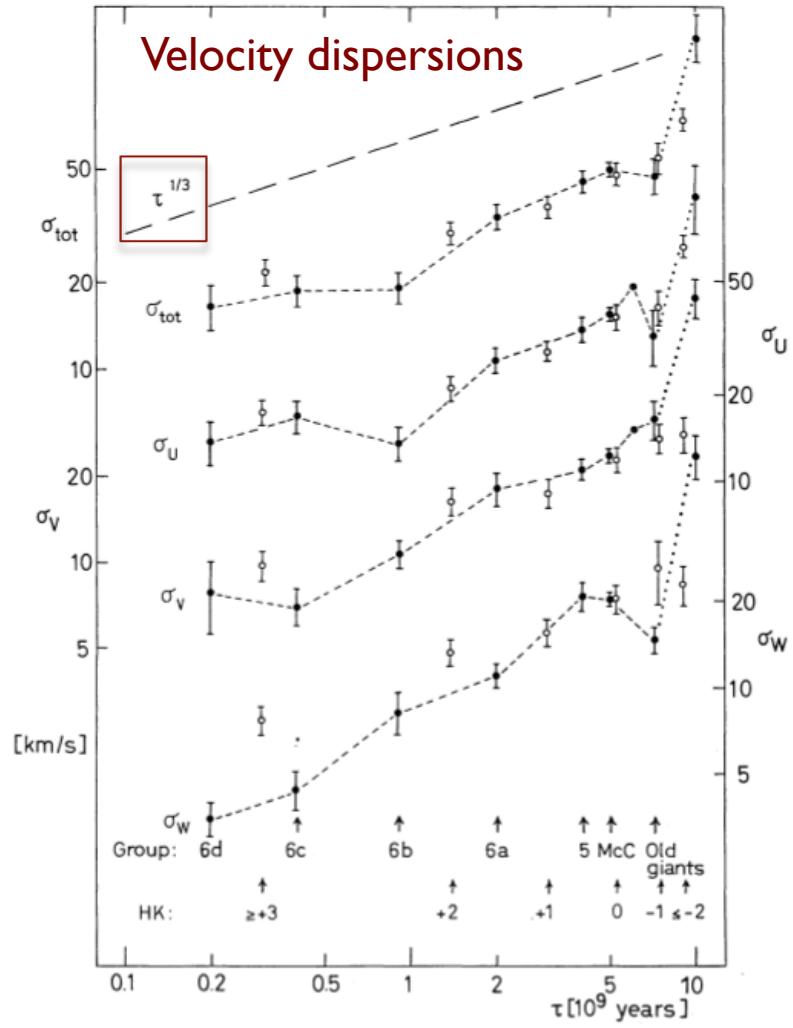


Fig. 4. Velocity dispersions as a function of age.

# How are disk stars heated?

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- ▶ A number of options.... but:
- ▶ Limited constraints
  - ▶ Scale-height & vertical velocity dispersion of stars in the solar neighborhood *only*
  - ▶ Shape of velocity dispersion ellipsoid:
    - ▶  $\sigma_R:\sigma_z:\sigma_\phi \iff \langle u^2 \rangle^{1/2}:\langle v^2 \rangle^{1/2}:\langle w^2 \rangle^{1/2}$
  - ▶ Constant thickness with radius of external disks
  - ▶ Very limited data on a handful (<6) external galaxies: young stars are predominantly near the mid-plane (Seth et al. 2006)



# Disk heating options: 1 of 2

---

- ▶ Options I: Monolithic collapse scenario: early gas disk was thicker
  - ▶ This isn't heating!
  - ▶ Recent evidence *may* suggest early disks ( $z \sim 2$ ) were
    - ▶ comprised of very large gas clumps (Elmegreen & Elmegren 2006)
    - ▶ highly chaotic (smaller  $V/\sigma$ ; Förster-Schreiber et al. 2009)
    - ▶ Progenitors of today's disk systems or progenitors of today's massive spheroidals?
- ▶ **More fundamentally: disk heating in MW occurs most rapidly for young ages (recent times). This requires disks to have been a lot thicker in the recent past. Not observed.**
  - ▶ Thicker gas disks *may* be relevant for some thick-disk component. TBD!



# Disk heating options: 2 of 2

## ▶ Option 2: Gravitational encounters (two-body relaxation)

- ▶ Energy equipartition → star-star encounters not interesting

$$\triangleright m_1 v_1^2 = m_2 v_2^2$$

- ▶ → requires objects much more massive than single stars:

- ▶ Star—GMC (giant molecular clouds)

- Encounters naturally due to differential galactic rotation
  - Produces isotropic scattering →  $\sigma_R : \sigma_z : \sigma_\phi$  of order unity

- ▶ Star—spiral wave

- Encounters naturally due to differences between pattern-speed and rotation (what happens at co-rotation?)

- ▶ Produces scattering primarily in plane:  $\sigma_z < \sigma_R$  and  $\sigma_\phi$

- ▶ Star—halo object

- globular clusters
  - black holes
  - satellites

Apparently cannot account for all of the heating observed in solar neighborhood

What is seen in solar neighborhood →

Outcome depends in detail on orbits (radial or tangential), masses, and spatial distribution (N vs radius)

# Disk heating via diffusion

---

- ▶ Each encounter delivers an impulse ( $\Delta\mathbf{v}$ ) to a star's velocity  $\mathbf{v}$
- ▶ Over many (random) encounters  $\langle \Delta\mathbf{v} \rangle = 0$ 
  - ▶  $\langle \Delta\mathbf{v} \rangle = [ (1/t) \sum_{i=1,n} \Delta\mathbf{v}_i ]_{t \rightarrow \infty} = 0$
  - ▶ But the sum of the squares does not (direction is randomized, but accelerations are cumulative in an energy sense):
    - ▶  $\sum_{i=1,n} (\Delta\mathbf{v}_i)^2 = D t$
    - ▶  $D$  is a diffusion coefficient that may, in general depend on  $t$  and  $\mathbf{v}$



# Disk heating via diffusion – Model 1

## ► Model I:

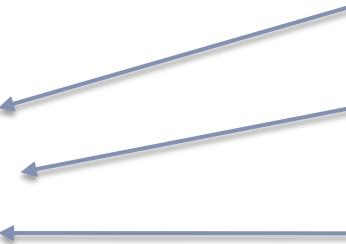
- assume diffusion is isotropic, independent of a star's orbit:

- $d(v^2)/dt = D t$

- For constant  $D = D_0$

- $v^2 = D_0 t + c$

- $\rightarrow v_{\text{rms}}(t) = v_{\text{rms}}(0)[1 + t/\tau]^{1/2}$

 $v_{\text{rms}} = \sigma = \langle v^2 \rangle^{1/2}$

$\tau$  is something we measure

What about  $v_{\text{rms}}(0)$ ?

- See Wielen 1977, A&A, 60, 263

# Disk heating via diffusion – Model 2

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## ► Model II:

- From theory of binary encounters (see S&G Ch. 3)  $D$  is inversely proportional to  $v$ , i.e.,  $D(v) = D_0/v$
- From our initial formulation of diffusion it follows:
  - $d(v^2)/dt = D t$
  - $v^3 = 3/2 D_0 t + c$
  - $v_{rms}(t) = v_{rms}(0)[1 + t/\tau]^{1/3}$



# Disk heating via diffusion: conclusions

---

- ▶ From these two models we expect an increase in  $\sigma$  to go as  $t^{1/n}$ , with  $2 < n < 3$
- ▶ Assuming  $v_{\text{rms}}(0) = 10 \text{ km s}^{-1}$ , Wielen (1977) estimated from solar neighborhood:
  - ▶  $\tau = 2 \times 10^8 \text{ yr}$  for  $n = 2$
  - ▶  $\tau = 5 \times 10^7 \text{ yr}$  for  $n = 3$ 
    - if GMCs  $\rightarrow M_{\text{GMC}} \sim 2 \times 10^6 M_{\odot}$ , roughly as observed (a bit high)
  - ▶  $\sigma_R : \sigma_\phi : \sigma_z \sim 1.0 : 0.64 : 0.53$ , roughly as observed
    - even for isotropic diffusion (don't need spiral arms!)



# Disk heating: initial conditions circa 1980

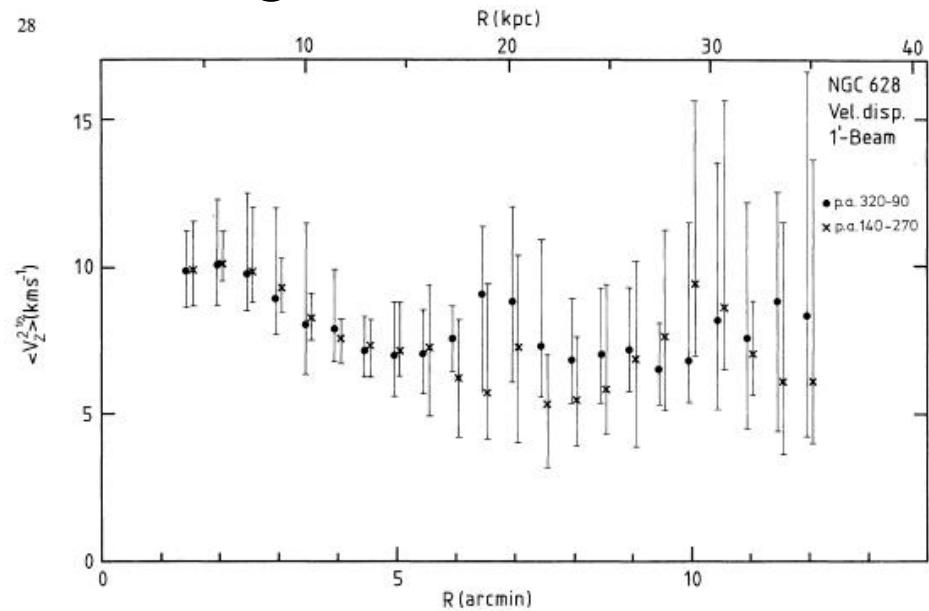
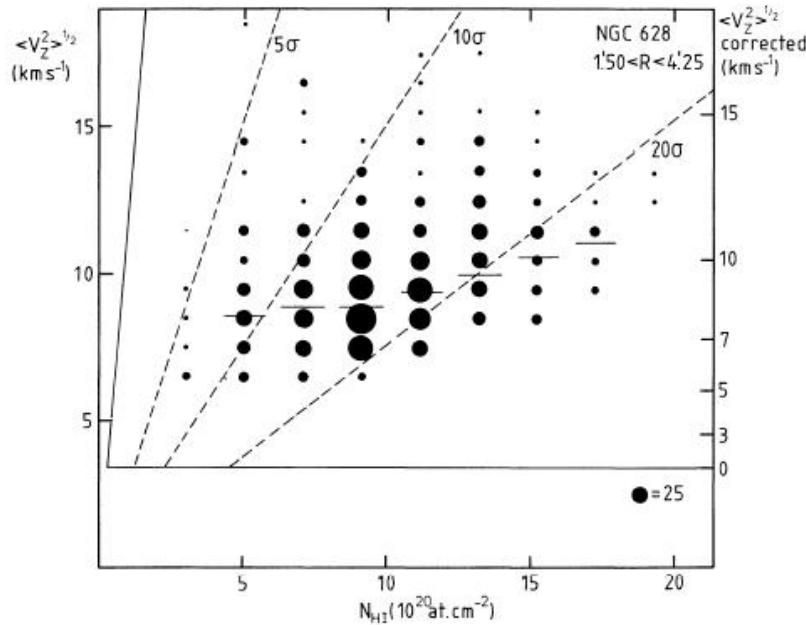
## ▶ Vertical velocity dispersions in cold gas

van der Kruit & Shostak (1982, 1984):

$$\sigma_{\text{HI}} = 6-12 \text{ km/s}$$

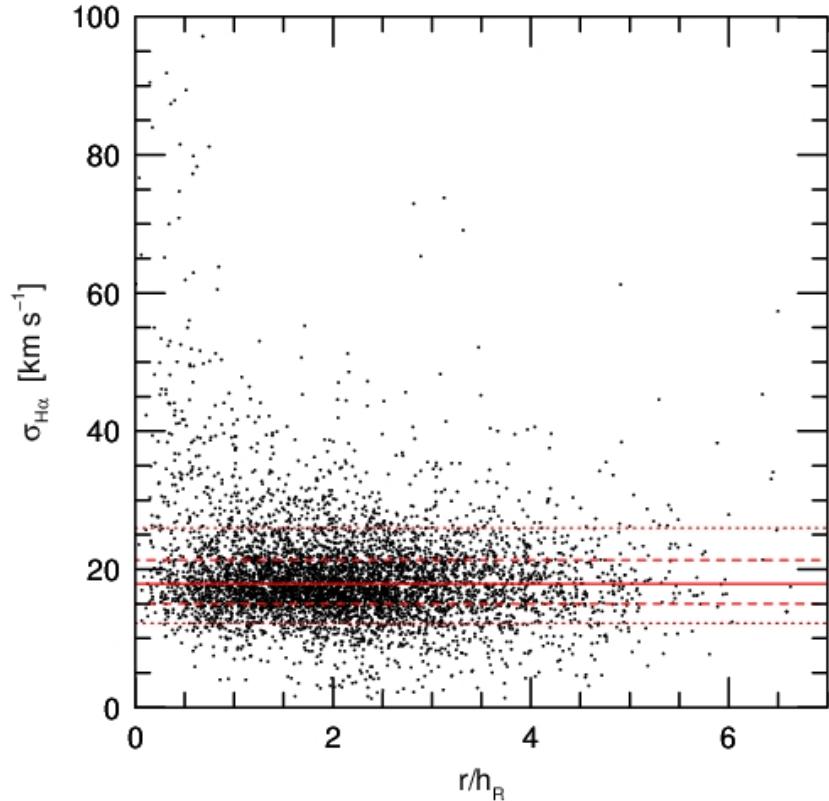
Combes & Bequaert (1997):

$$\sigma_{\text{CO}} = 6-9 \text{ km/s}$$

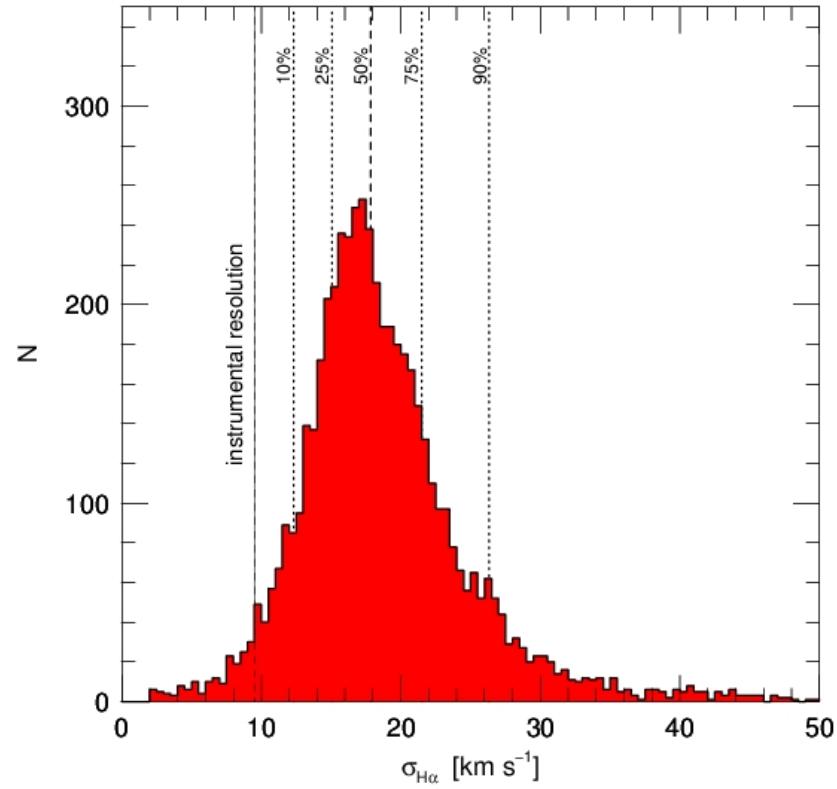


- ~constant with radius -- some density dependence
- Thermal values should be in the 6-8 km/s range

# Disk heating: ionized gas (not “initial”)



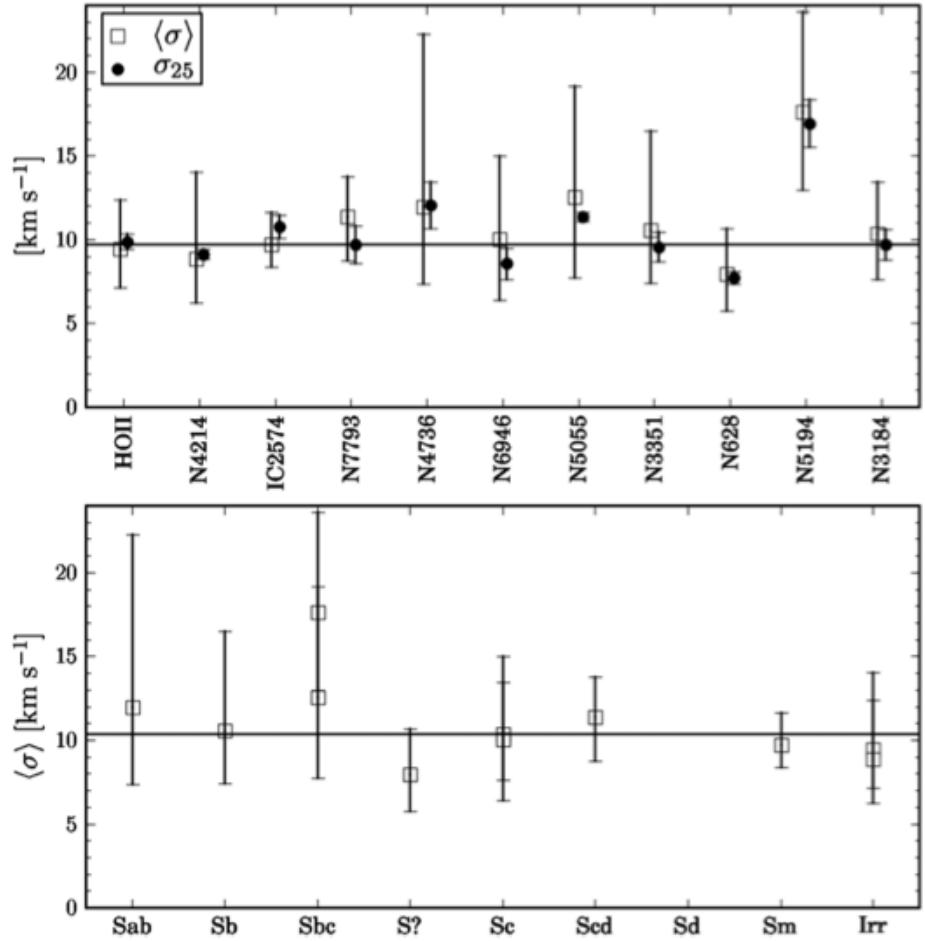
18 km s $^{-1}$



- ▶ Median  $\sigma_{\text{H}\alpha} = 18$  km/s, appears constant with radius.
- ▶ Significant dispersion and galaxy-galaxy variations.

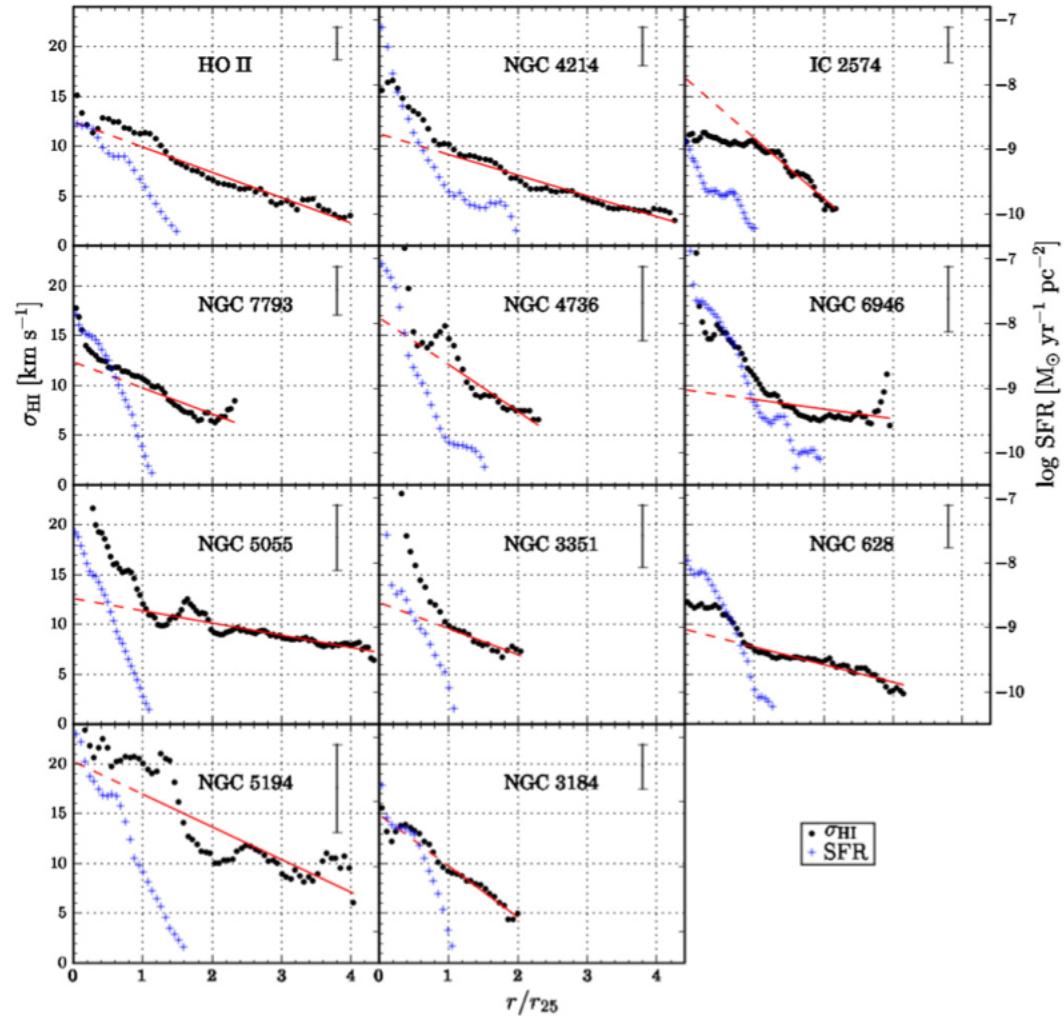
# Initial conditions updated:

- ▶ The good news:
  - ▶ The mean  $\sigma_{\text{HI}}$  appears very uniform from galaxy to galaxy and across galaxy types.



# Initial conditions updated:

- ▶ The bad news:
  - ▶ Almost all galaxies show radial gradients with values of  $\sigma_{\text{HI}}$  well above thermal values for warm HI
  - ▶ Likely input from star-formation in the form of wind-driven shocks and SNe



# Disk heating: beyond the solar neighborhood

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- ▶ While we have a plausible model for how stars heat in the solar neighborhood
  - (via diffusion and equipartition from many two-body encounters with massive objects)

the picture is incomplete:

- ▶ Diffusion theory doesn't give a good prediction for the time-scale  $\tau$
- ▶ GMCs and spiral arms don't appear to heat disk enough
  - ▶ Solution: add globular clusters and ubiquitous dark-matter dominated satellites (subhaloes) predicted by  $\Lambda$ CDM structure-formation theory.  
Ok, but...
- ▶ There has been a lot of work on looking at disk-heating from minor mergers but this tends to lead to disk-flaring in the vertical direction
  - ▶ Limits have been placed on the total amount of merging / accretion, e.g., Tóth & Ostriker (1992, ApJ, 389, 5)
- ▶ There hasn't been a study done which includes all of the ingredients
  - ▶ **Awesome thesis topic!**



# Disk heating: beyond the solar neighborhood

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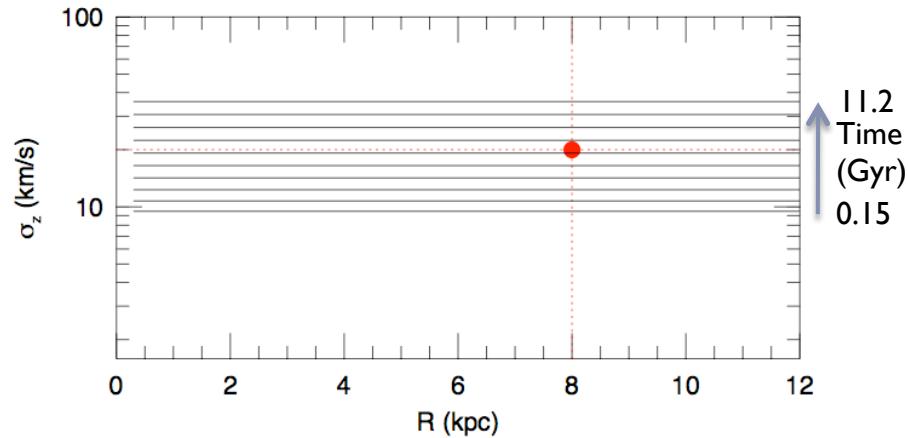
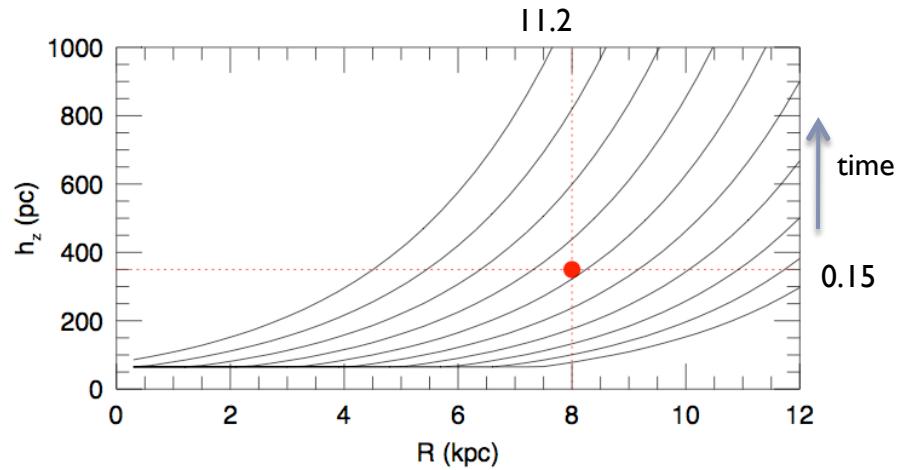
- ▶ How well does the model, calibrated in the solar neighborhood match the expectations for the MW and external galaxies overall?
  - ▶ Specifically, do we get constant scale-height disks?
- ▶ Let's try a few simple calculations for the MW:
  - ▶  $t_0 = 11$  Gyr (age of disk today)
  - ▶  $R_\odot = 8$  kpc
  - ▶  $\Sigma = \Sigma_0 \exp(-R/h_R - z/h_z)$
  - ▶  $h_R = 3$  kpc
  - ▶ old stars in thin disk in the solar neighborhood:
    - ▶  $h_z(R_\odot, t_0) = 350$  pc
    - ▶  $\sigma_z(R_\odot, t_0) = 20$  km/s
  - ▶ Generic assumptions:
    - ▶ Disk mass surface-density  $\Sigma$  and scale-length  $R$  independent of time



# Disk heating: beyond the solar neighborhood

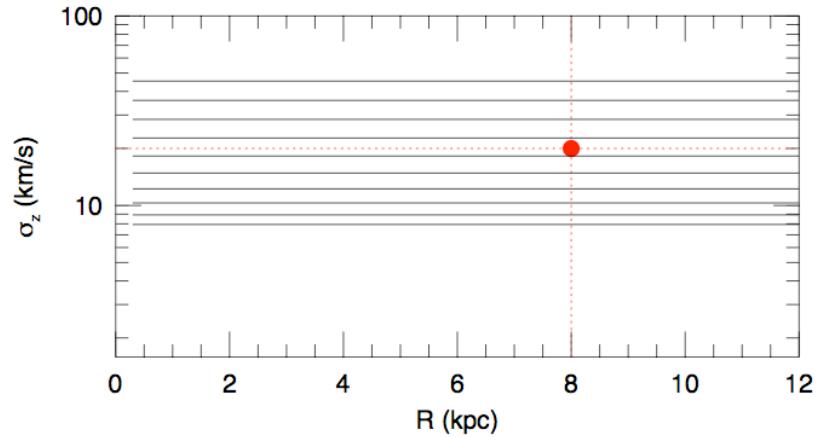
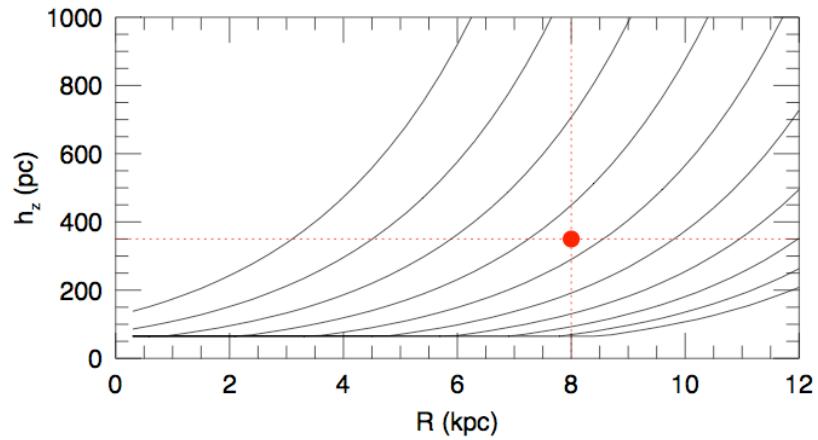
## ► Model I:

- Initial conditions:
  - $\sigma_z(t=0) = 6 \text{ km/s}$ , independent of radius
  - $h_z(t=0) = 65 \text{ pc}$ , independent of radius
- Final conditions:
  - $h_z(R_\odot, t_0) = 350 \text{ pc}$
  - $\sigma_z(R_\odot, t_0) = 20 \text{ km/s}$
- Other conditions:
  - Disk mass surface-density  $\Sigma$  and scale-length  $R$  independent of time
- Fixed parameters:
  - $n = 2$
  - $\tau = 0.2 \text{ Gyr}$
- Free parameters: none



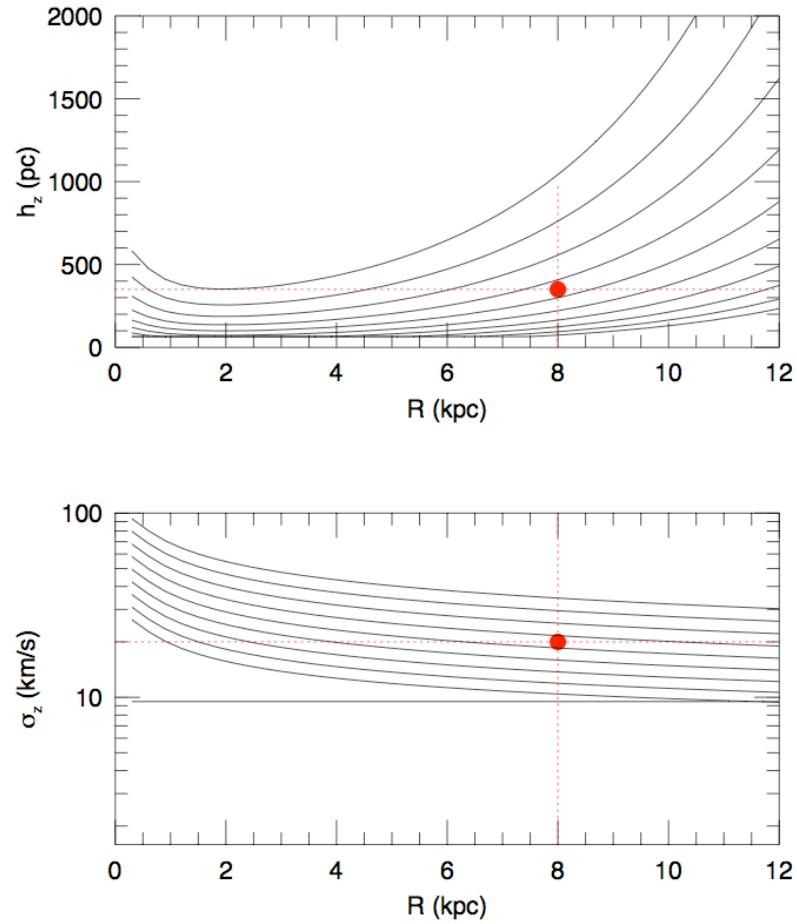
# Disk heating: beyond the solar neighborhood

- ▶ **Model 2:**
  - ▶ Initial conditions:
    - ▶  $\sigma_z(t=0) = 6 \text{ km/s}$ , independent of radius
    - ▶  $h_z(t=0) = 65 \text{ pc}$ , independent of radius
  - ▶ Final conditions:
    - ▶  $h_z(R_\odot, t_0) = 350 \text{ pc}$
    - ▶  $\sigma_z(R_\odot, t_0) = 20 \text{ km/s}$
  - ▶ Other conditions:
    - ▶ Disk mass surface-density  $\Sigma$  and scale-length  $R$  independent of time
  - ▶ Fixed parameters:
    - ▶  $n = 3$
    - ▶  $\tau = 0.05 \text{ Gyr}$
  - ▶ Free parameters: none



# Disk heating: beyond the solar neighborhood

- ▶ **Model 3:**
  - ▶ **Initial conditions:**
    - ▶  $\sigma_z(t=0) = 6 \text{ km/s}$ , independent of radius
    - ▶  $h_z(t=0) = 65 \text{ pc}$ , independent of radius
  - ▶ **Final conditions:**
    - ▶  $h_z(R_\odot, t_0) = 350 \text{ pc}$
    - ▶  $\sigma_z(R_\odot, t_0) = 20 \text{ km/s}$
  - ▶ **Other conditions:**
    - ▶ Disk mass surface-density  $\Sigma$  and scale-length  $R$  independent of time
  - ▶ **Fixed parameters:**
    - ▶  $n = 3$
    - ▶  $\tau = t_{\text{dyn}} = 2\pi R/V_c$ 
      - $V_c = V_{\text{flat}} \tanh(R/h_{\text{rot}})$
      - $V_{\text{flat}} = 220 \text{ km/s}$
      - $h_{\text{rot}} = h_R/10$
  - ▶ **Free parameters:** none



# Disk heating: beyond the solar neighborhood

## ► Model 4:

### ► Initial conditions:

- $\sigma_z(R_\odot, t=0) = 6 \text{ km/s}$

- $h_z(R_\odot, t=0) = 65 \text{ pc}$

- $\sigma_z(R, t=0) =$

- $\sigma_z(R_\odot, t=0) \exp(-R/2h_R) / \exp(-4/h_R)$

\*\* ? \*\*

### ► Final conditions:

- $h_z(R_\odot, t_0) = 350 \text{ pc}$

- $\sigma_z(R_\odot, t_0) = 20 \text{ km/s}$

### ► Other conditions:

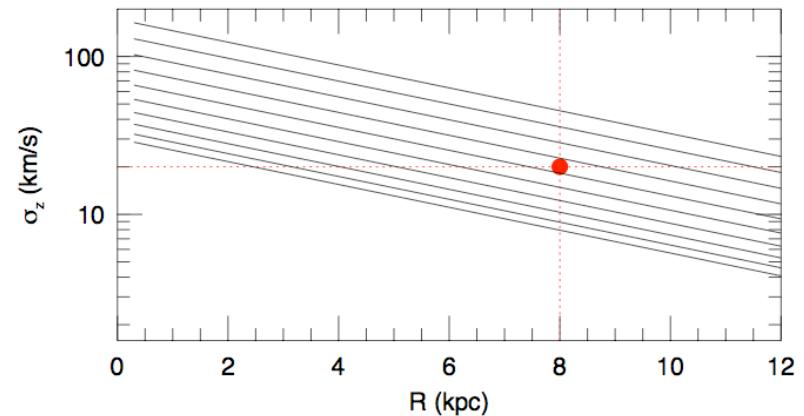
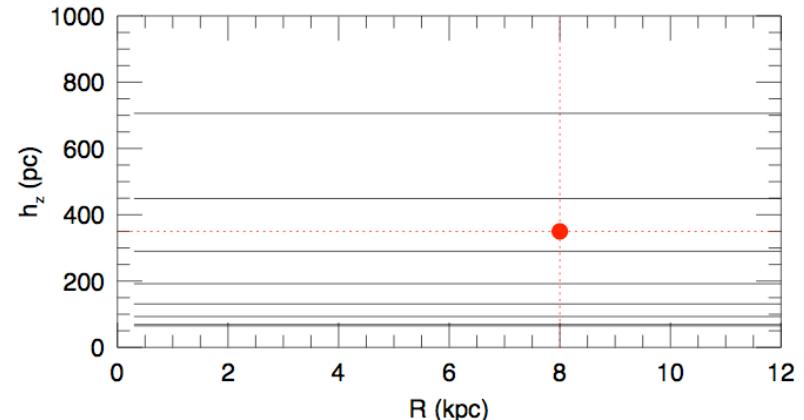
- Disk mass surface-density  $\Sigma$  and scale-length  $R$  independent of time

### ► Fixed parameters:

- $n = 3$

- $\tau = 0.05 \text{ Gyr}$

### ► Free parameters: none



\*\* Cheating? Recall Tamburro et al. 2009

# Disk heating: beyond the solar neighborhood

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- ▶ Other models:
  - ▶ So far we have held  $n$  and  $\tau$  fixed, or held  $n$  fixed and set  $\tau = t_{\text{dyn}}$ . The latter looked promising.
  - ▶ It is straightforward to find relationships between  $n$  and  $\tau$  such that the final conditions are met for any age population, e.g.,
    - ▶  $h_z(R_\odot, t_0) = 350 \text{ pc}$
    - ▶  $\sigma_z(R_\odot, t_0) = 20 \text{ km/s}$
    - ▶  $t_0 = 11 \text{ Gyr}$  (what might be better for old, thin disk?)even assuming the initial  $\sigma_z$  and  $h_z$  are independent of radius.
  - ▶ In this class of models, keeping either  $n$  or  $\tau$  fixed forces the other parameter to change with radius.
  - ▶ In all reasonable cases, this yields disks with nearly constant scale-height with radius
  - ▶ In the case where  $n$  is fixed,  $\tau(R)$  is close to  $t_{\text{dyn}}$ .



# Disk heating: beyond the solar neighborhood

Here're examples for fixed  $n$ :

