

# Astronomy 330

Lecture 6  
22 Sep 2010



# Outline

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- ▶ Review & conclude:
  - ▶ ISM detection techniques
  - ▶ Chemical evolution
- ▶ Stellar Luminosity Function
- ▶ The Milky Way as Galaxy:
  - ▶ Stellar Luminosity Function
  - ▶ Size and structure: bars, truncation
  - ▶ Kinematics: disk rotation



# Review: ISM

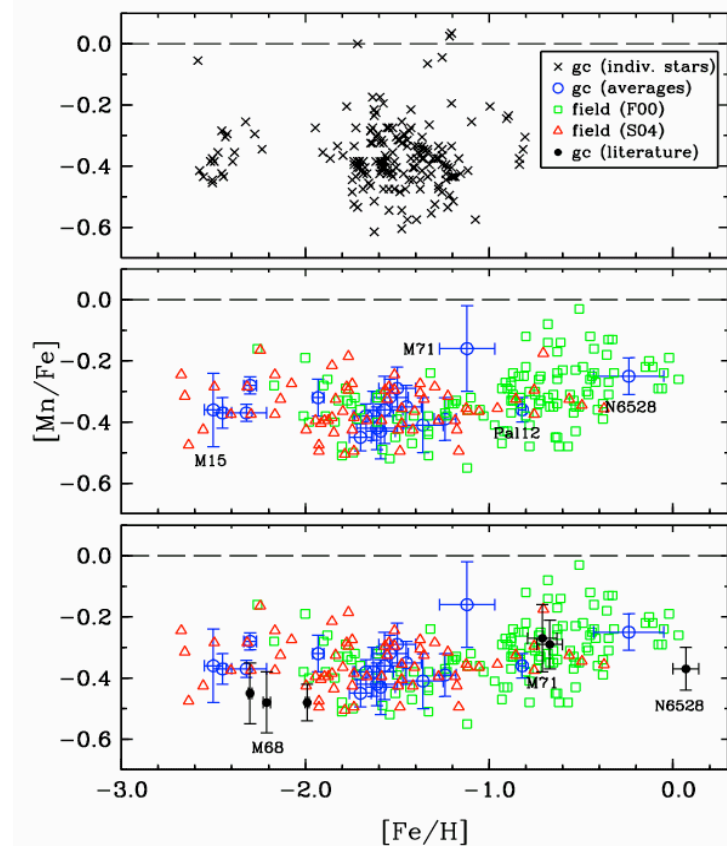
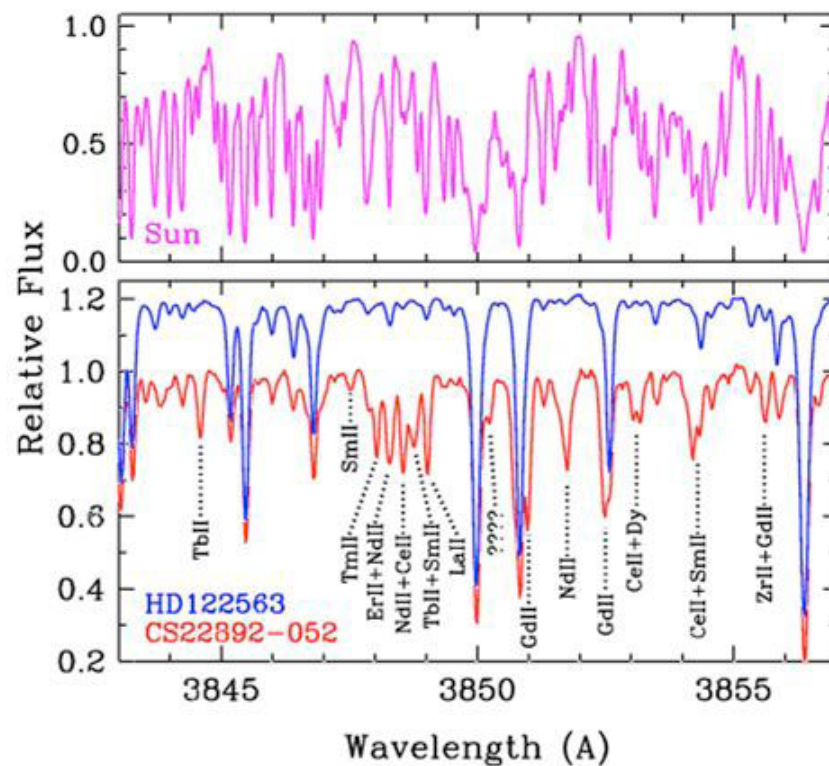
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- ▶ Gas content of disk galaxies
  - ▶ Phases: cold, cool, warm, hot
  - ▶ Filling-factors
  - ▶ Densities
  - ▶ Detection methods:
    - ▶ CO (mm)
    - ▶ HI (21 cm)
    - ▶ HII (H $\alpha$ , [OII], etc.)
    - ▶ X-ray emission
  - ▶ Diagnostics: SFR,  $T_e$ ,  $n_e$ , shocks
- ▶ Origin of the diffuse hot gas in galaxies
  - ▶ Likely from SNe
  - ▶ Hot gas is correlated with star formation/spiral arms in disk galaxies



# Review: Chemical Evolution

- ▶ What is the correlation between these observed absorption lines and the star formation history of this stellar system?





# Recall: Disk Gradients

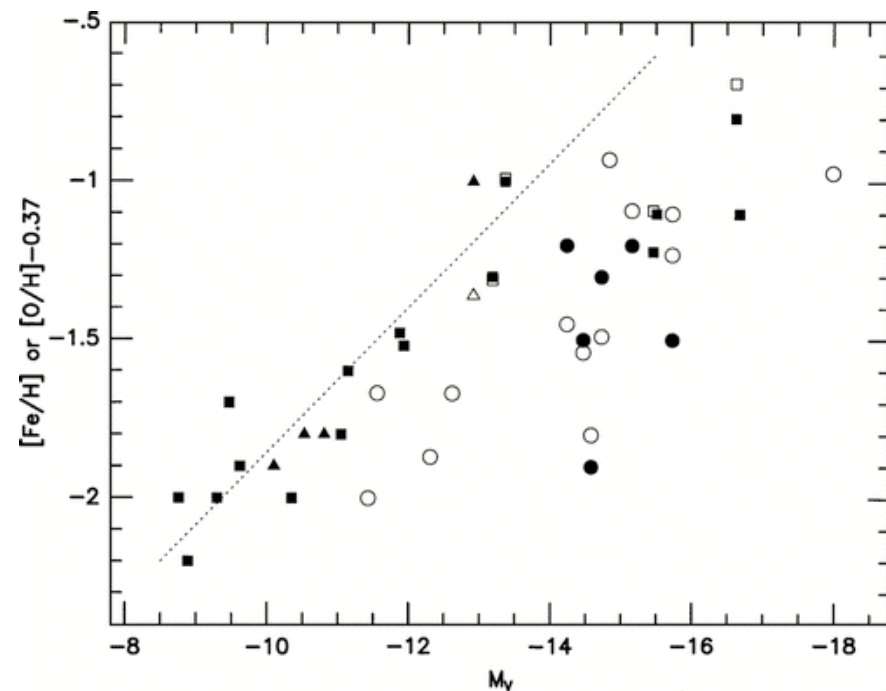
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- ▶ **General characteristics**
  - ▶  $12 + \log(\text{O}/\text{H}) = 8.58 - 0.32 R/R_0$
  - ▶ Generally: -0.04 to -0.07 dex/kpc
  - ▶ Flatter in late-types, steep in barred galaxies
- ▶ **Why are there gradients?**
  - ▶ Radial dependence on SFR/SFH?
  - ▶ Radial gas flows?
  - ▶ Radial dependence on yield?
  - ▶ Radial dependence on infalling gas?



# Extragalactic Abundances: Dwarfs

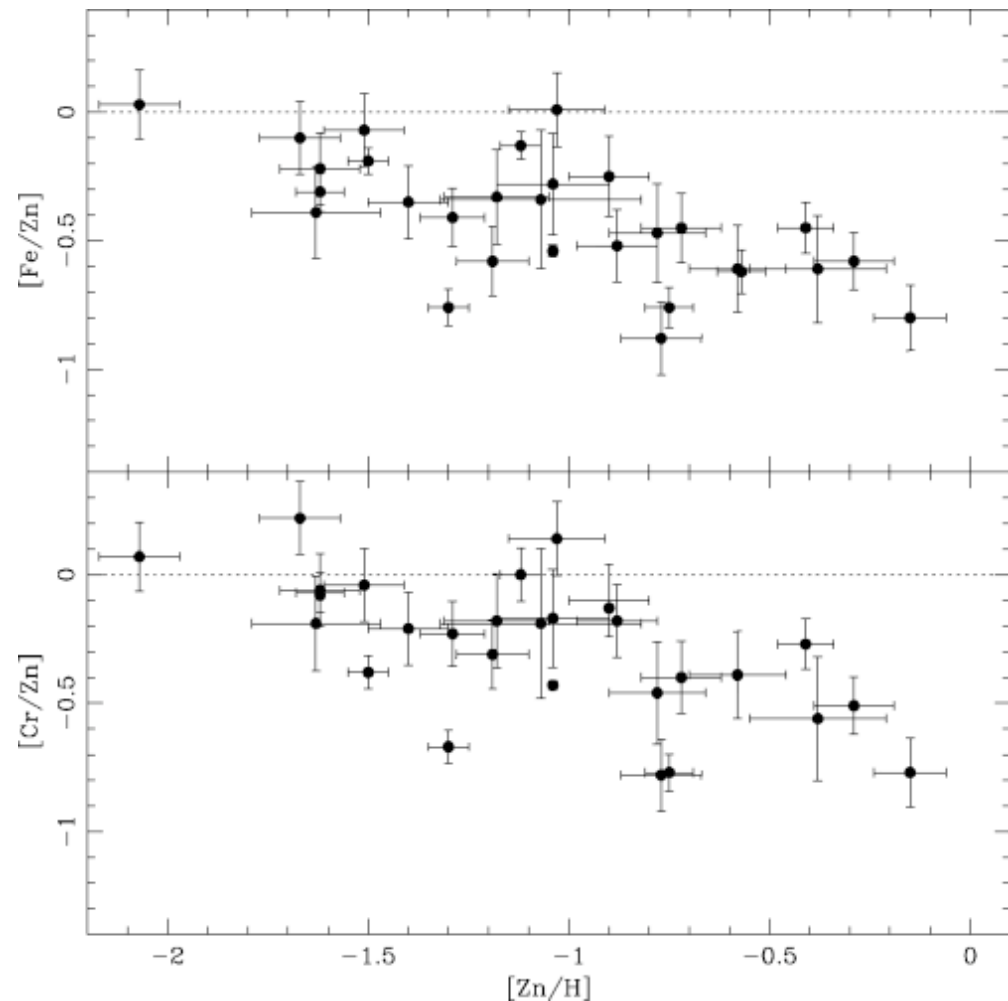
- ▶ LMC is 50-70% solar
  - ▶  $[O/H] = -0.3$  to  $-0.15$
- ▶ SMC  $\sim$  20-25% solar
  - ▶  $[O/H] = -0.7$  to  $-0.65$
- ▶ Some dwarfs extremely metal poor (1/10 solar)
- ▶ Why?



← Decreasing  
luminosity

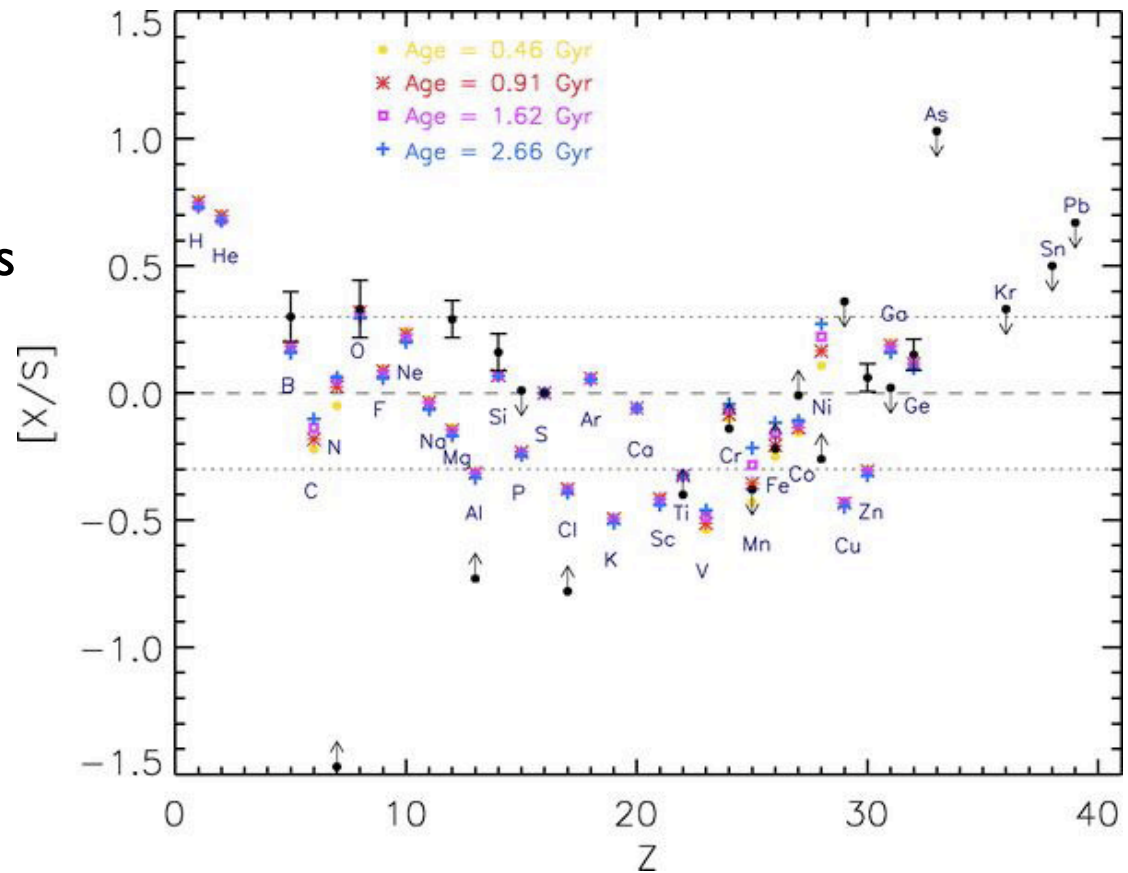
# QSO Absorption Lines

- ▶ Absorption line systems detected against background quasars
- ▶ Gas phase abundances can be measured via absorption lines
- ▶ Most metal-poor gas systems ever found
- ▶ Enrichment histories vary from solar



# QSO Absorption Lines

- ▶ Damped Ly- $\alpha$  systems have high column, high velocities  $\rightarrow$  correlated with galaxies
- ▶ Thought to be progenitors of today's massive galaxies
- ▶ Consistent with:
  - ▶ young ages
  - ▶ 1/3 solar
  - ▶ Enrichment dominated by massive stars
    - ▶ few Type-Ia SNe



Fenner, Prochaska, & Gibson 2004 ApJ

# Chemical Evolution of Galaxies

## ▶ Simple models

- ▶  $M_g(t)$  = gas mass
- ▶  $M_r(t)$  = remnant mass
- ▶  $M_s$  = mass in stars
- ▶  $M_h(t)$  = mass in heavy elements
- ▶  $Z(t) = M_h/M_g$  = metallicity
- ▶  $\Delta M$  = change in mass
- ▶  $p$  = fractional yield of heavy elements



$$\begin{aligned}\Delta M_h &= p \Delta M_s - Z \Delta M_s \\ &= (p - Z) \Delta M_s \\ \Delta Z &= \Delta (M_h/M_g) \\ &= [p \Delta M_s - Z(\Delta M_s + \Delta M_g)]/M_g\end{aligned}$$

See S&G 4.3.2

## ▶ In a closed box $\Delta M_s + \Delta M_g = 0$ .....

- ▶  $Z(t) = p \ln [M_g(t)/M_g(0)]$
- ▶ Implies gas-rich things should have lower  $Z$
- ▶ Also:  $M_s(<Z(t)) = M_g(0)[1 - e^{-Z(t)/p}] \rightarrow$

- ▶ We should see lots of really low metallicity G stars
- ▶ Something like 50% of G dwarfs should have  $z < 0.25Z_\odot$ !
- ▶ But we don't: closer to 25% for Fe and <1% for O
- ▶ ➔ so-called G-dwarf problem

# The G-Dwarf Problem

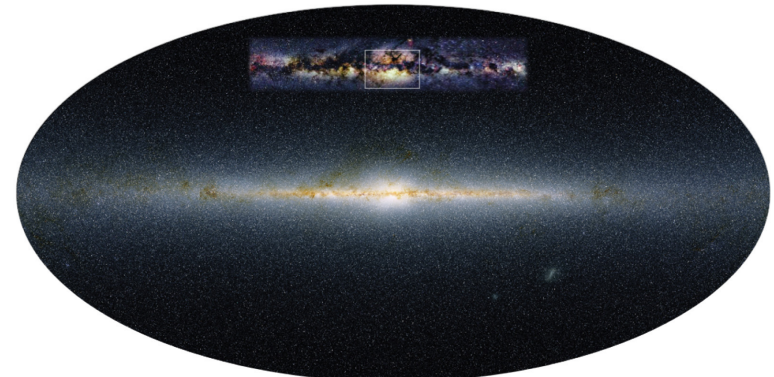
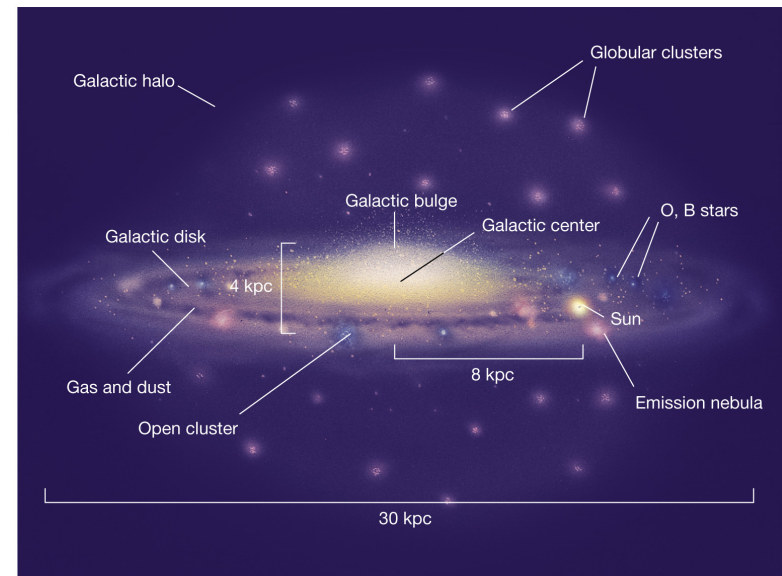
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- ▶ How does the absence of low-metallicity G-dwarfs in the solar neighborhood relate to a few other conundrums mentioned so far:
  - ▶ The mysterious absence of detected Pop III stars?
  - ▶ The puzzling fact that most of the baryons do not appear to be in galaxies, but in a hot ( $10^6$  K gas) in the IGM?
  - ▶ And the baryonic IGM is metal-enriched?



# Modeling the Milky Way Galaxy (MWG)

- ▶ What is the stellar distribution?
- ▶ How big is the Milky Way?
  - ▶ Does (where does) the disk have an outer truncation?
- ▶ Does it have a bar?
- ▶ How do the stars move in the galaxy?
  - ▶ Galactic rotation and Oort's constants





# Star Counts

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## ► Formalism

►  $N(M,S) = \int \Phi(M,S) D(r) r^2 dr$

- $N$  = # of field stars of a given absolute magnitude ( $M$ ) and spectral type ( $S$ ) in the galaxy
- $\Phi$  = stellar luminosity function (# pc<sup>-3</sup> for some spectral type)
- $D(r)$  = density distribution
  - may also depend on  $M, S$ :  $D(r, M, S)$
  - Alternatively,  $\Phi$  may also depend on  $r$

## ► The simplest thing we can actually observe:

- $A(m)$  = # of stars of some apparent magnitude,  $m$ .
- $A(m) = \int \Phi(M) D(r) \Omega r^2 dr$ 
  - $\Omega$  = solid angle of survey

## ► If we have colors, we might get a crude $A(m, S)$

- but without distances or some luminosity indicator, we can't break the dwarf-giant degeneracy (e.g., K V vs K III).



# Star Counts: Infinite Euclidean Universe

- ▶  $A(m)$  represents the differential counts, i.e., number of stars per apparent magnitude interval
- ▶ Knowing the geometry (locally Euclidean), the count slope ( $dA/dm$ ) tells us about the spatial distribution of sources.
- ▶ For a *uniform* space-distribution of sources it is straightforward to show

- ▶  $d(\log A)/dm = 0.6m + \text{constant}$

- ▶ This leads to Olbers' paradox:

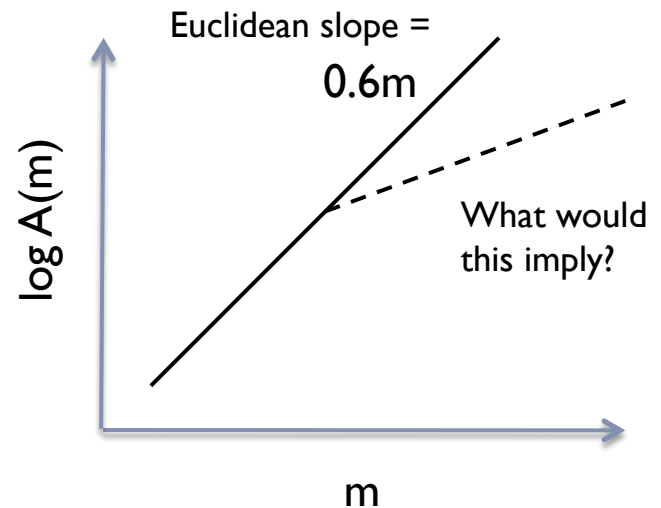
- ▶  $I(m) = I_0 \exp(-0.4m)$

- ▶  $L(m) = I(m)A(m)$

- ▶  $L_{\text{tot}} = \int I(m)A(m) dm = \infty$

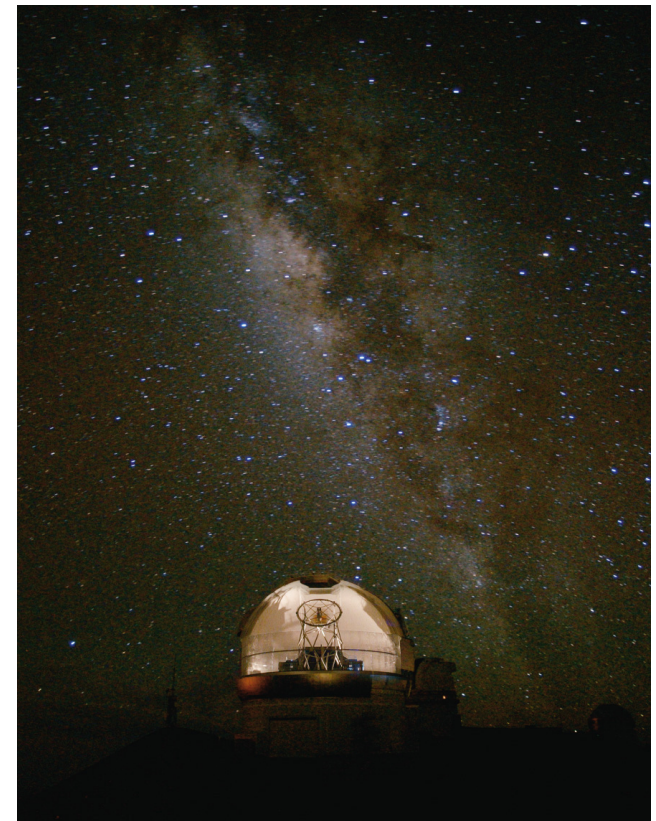
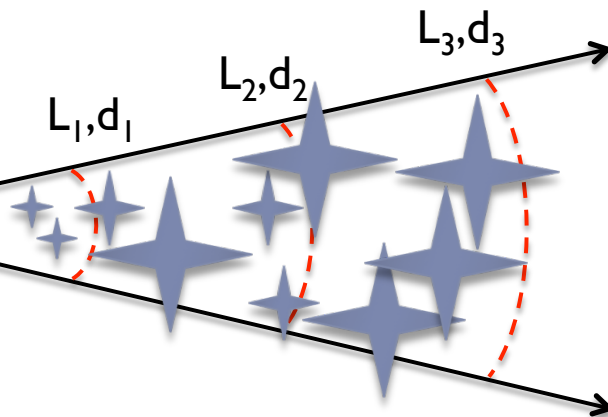
- ▶ The distribution of stars in the galaxy must be spatially finite

- ▶ *What about the universe of galaxies?*



# The Malmquist Bias & the Night Sky

- ▶ What stars do you see when you look up at the night-time sky?
- ▶ Does this make sense given what you know about the HR diagram
- ▶ Malmquist bias:
  - ▶ You can see brighter objects farther away to a fixed  $m$
  - ▶ Volume increases as  $d^3$



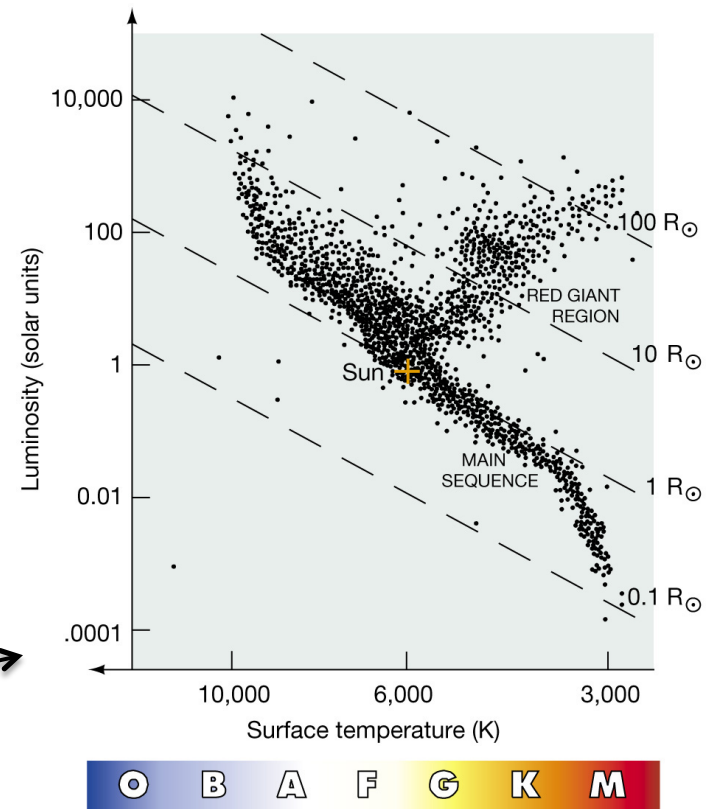
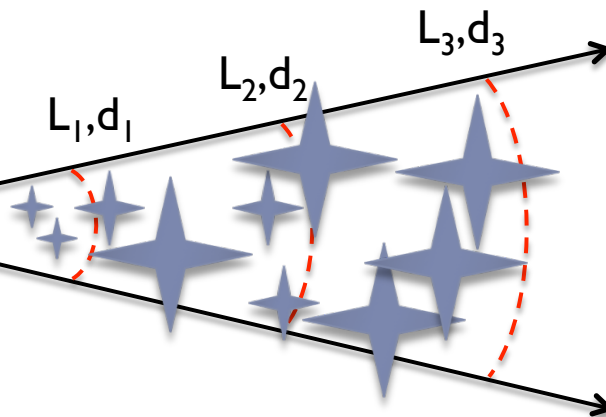
For a uniform space-density, the observer is biased toward finding intrinsically luminous objects.

young

old

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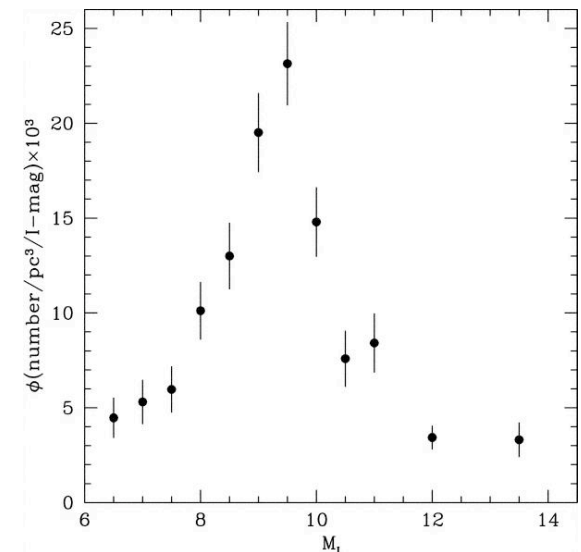
For a uniform space-density, the observer is biased toward finding intrinsically luminous objects.

young

old

# Star Counts & The Malmquist Bias

- ▶ What's the mean magnitude of stars with apparent magnitude,  $m$ ?
  - ▶  $M(m) = \int M \Phi(M) D(r) r^2 dr / \int \Phi(M) D(r) r^2 dr$
  - ▶ Recall  $A(m) = \int \Phi(M) D(r) \Omega r^2 dr$
- ▶ Assume the stellar luminosity function (LF) is Gaussian for a given spectral type:
  - ▶  $\Phi(M, S) = \Phi_0 / (2\pi)^{1/2} \sigma \exp[-(M - M_0)^2 / 2 \sigma^2]$
  - ▶  $M_0$  = mean magnitude
  - ▶  $\Phi_0$  = # pc<sup>-3</sup> for some spectral type
  - ▶  $\sigma$  is the distribution width



Zheng et al. (2004, ApJ, 601 500):  
MW disk M-dwarfs, *I*-band, *HST*

# Star Counts & The Malmquist Bias

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- ▶ Push through the integral for  $M(m)$  and move things around a bit....

- ▶  $M(m) = M_0 - [\sigma^2/A(m,S)] [dA(m,S)/dm]$

- ▶ Or:

$$M(m) - M_0 = -\sigma^2 d \ln A / dm$$

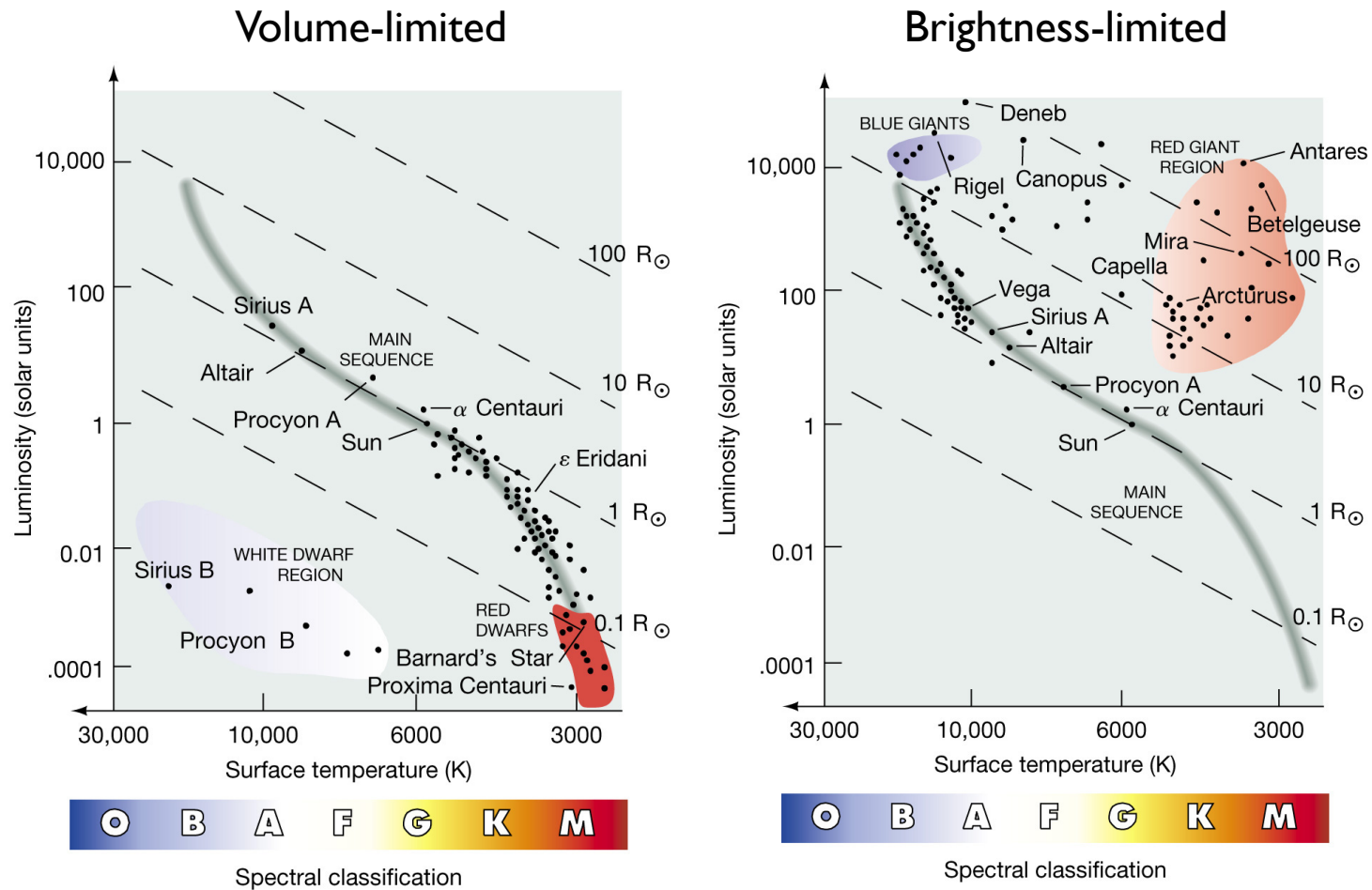
*This is for the specific case of a Gaussian LF, but it can be generalized.*

- ▶ If there are more stars at faint magnitudes, then the stars at some  $m$  are more luminous than the average for all stars in a given volume
  - ▶ This will come back to bite us with a vengeance when considering distant galaxy counts

A note on logarithmic derivatives:  
 $d \ln x = dx / x$   
This is nice because it normalizes the gradient to the amplitude of the signal, i.e., dimensionless.  
Therefore often used in Astronomy



# Space Densities: Local Neighborhood





# Stellar Luminosity Function

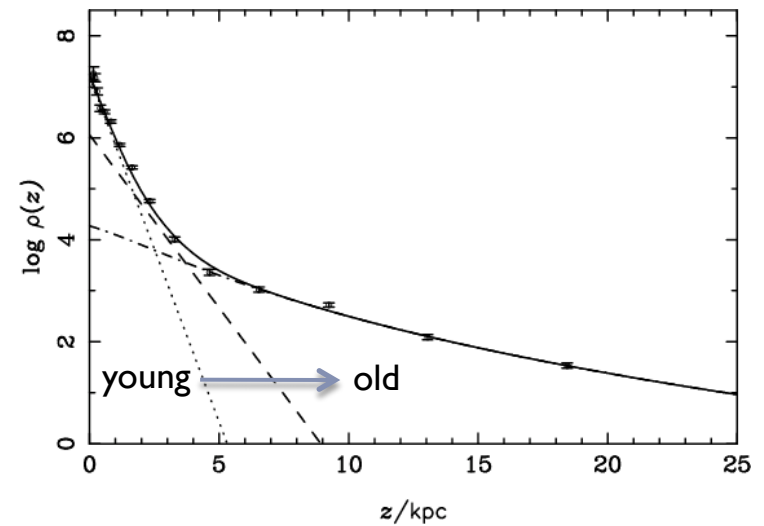
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- ▶ Measure for a distance(volume)-limited sample
- ▶ Bahcall & Soneira (1980) used:
  - ▶  $\Phi(M) = [n_* 10^{\beta(M-M_*)}] / [1 + 10^{-(\alpha - \beta)\delta(M-M_*)}]^{1/\delta}$ 
    - ▶  $n_* = 4.03 \times 10^{-3}$
    - ▶  $M_* = 1.28$
    - ▶  $\alpha = 0.74, \beta = 0.04, 1/\delta = 3.40$
- ▶ See also Figure 2.4 in S&G.
- ▶ Basic results
  - ▶  $10^5$  times more G stars than O stars
  - ▶ Nearby stars tend to be
    - ▶ low-luminosity and apparently faint
  - ▶ Average  $M/L = 0.67 (M/L)_{\odot}$



# Star Counts: The Disk

- ▶ Star counts (z direction)
  - ▶  $n(z)$  proportional to  $\exp(-z/z_0(m))$ ,
    - ▶  $z_0(m)$  is the scale height (and, yes, it does vary with magnitude)
  - ▶ More importantly,  $z_0$  varies with spectral type:
    - ▶ young : old  $\rightarrow$  small : large
    - ▶ **WHY?**
  - ▶ Reid & Majewski (1993)
    - ▶ Thin disk with  $z_0 = 325$  pc – Pop I
    - ▶ Thick disk with  $z_0 = 1200$  pc – Pop II
- ▶ The Disk
  - ▶  $I(R) = I(0)\exp[-R/h_R]$
  - ▶ tough to measure in our own galaxy, but measurable in other disks pretty easily.
- ▶ Disk is really a double exponential:
  - ▶  $I(R,z) = I(0,0)\exp(-z/z_0 - R/h_R)$



Du et al. 2003 A&A 407 541,  
stellar density perpendicular to  
the plane

# Star Counts: The Halo

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- ▶ Halo stars

- ▶ Halo stars are faint, need an easy to find tracer

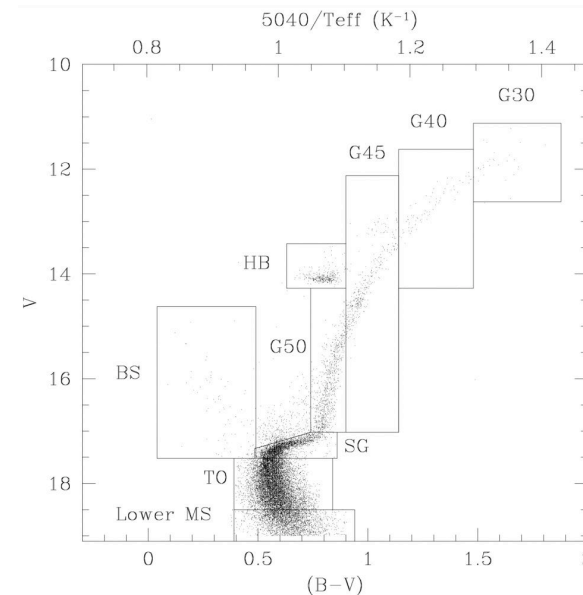
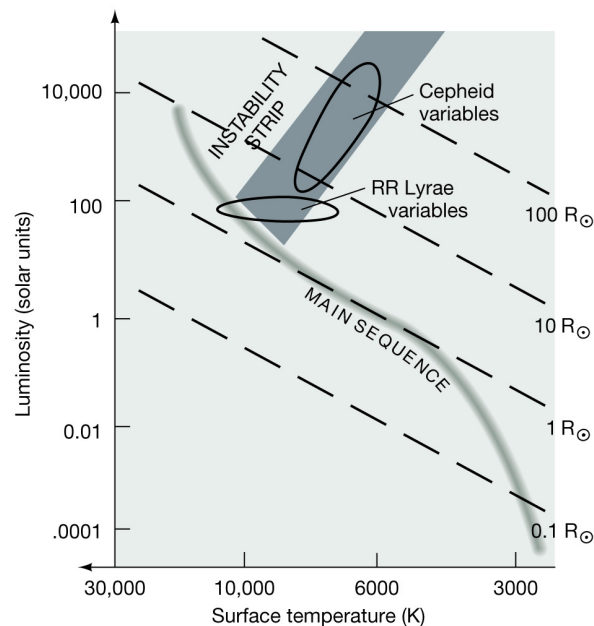
## RR Lyrae stars

- ▶ Stellar density falls off as  $r^{-3}$
  - ▶ Looks like the distribution of globular clusters, which you also get from RR Lyrae stars
- ▶ We will come back to this density fall-off when we consider the rotation curve.



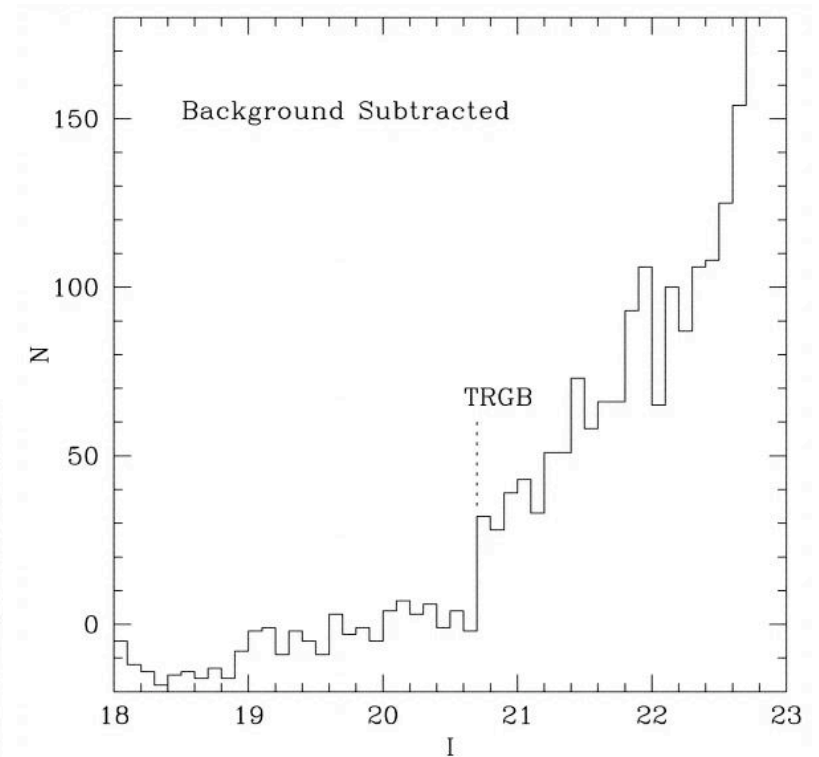
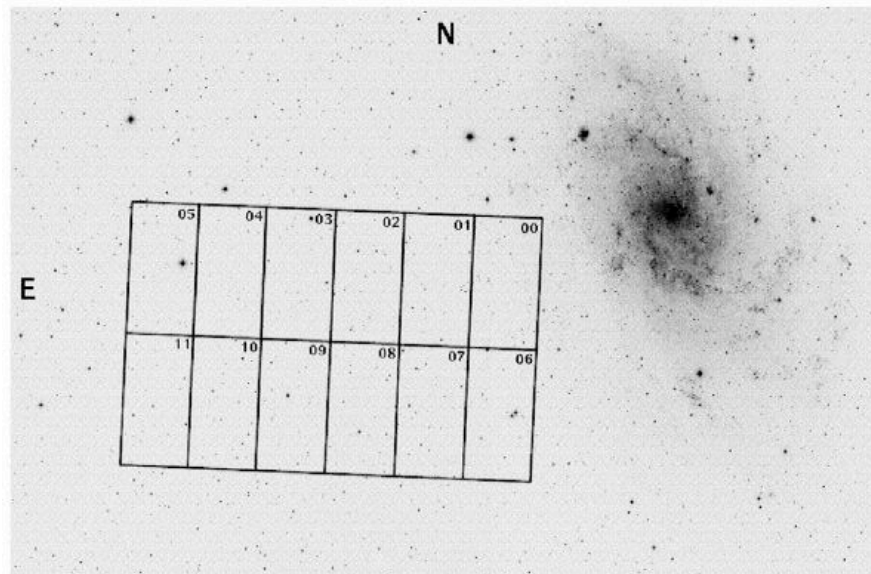
# Recall: RR Lyrae Stars

- ▶ HB stars in “the instability strip”
  - ▶ Solar mass
  - ▶ Opacity driven pulsations yield variability which is correlated with  $M$
  - ▶  $M = -2.3 \pm 0.2 \log(P) - 0.88 \pm 0.06$  (with some additional variation due to metallicity)
  - ▶ Old, low mass stars (hence good tracers of the halo)
- ▶ Higher mass (farther up the instability strip you’ll find Cepheids)



# M33 LF

- ▶ Outer fields of M33
  - ▶ (Brooks et al. 2004, AJ, 128, 237)



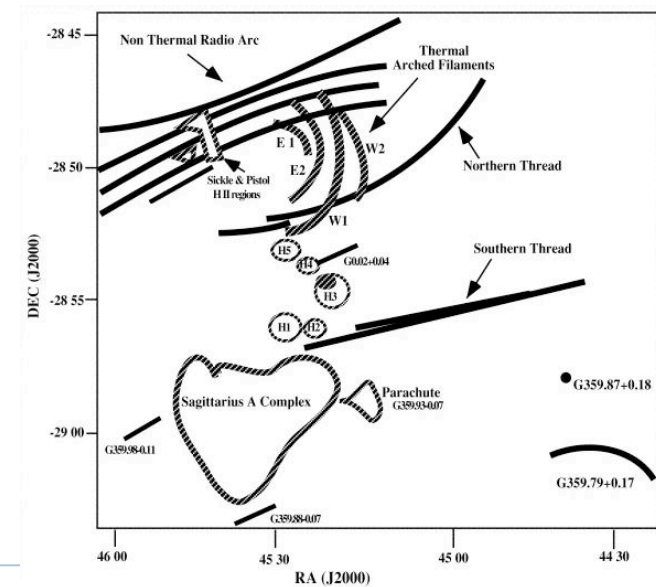
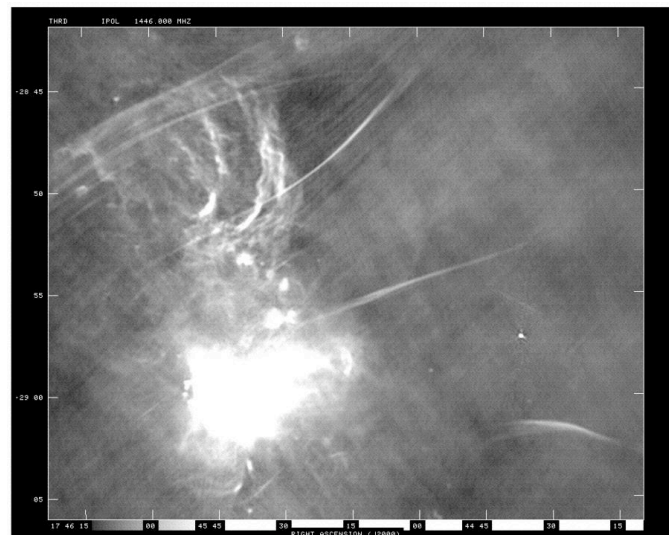
Counts proportional to luminosity function of *all* stars in M33 halo, corrected for contamination and completeness. TRGB at  $I = 20.7$  gives distance modulus.

# Galactic Center

- ▶ We'll talk about the center again when we discuss AGNs
- ▶ The optical view:



- ▶ The VLA 1.4 Ghz view:



# Galactic Center: Distance

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- ▶ Use RR Lyraes + other stellar tracers
  - ▶ Use the globular cluster population, OH/IR stars in the bulge
  - ▶ Get mean distances → 8.5 kpc
- ▶ Proper motion studies of Sgr A\*
  - ▶ Look for maser emission
  - ▶ Follow maser proper motion + observed velocity
    - distance (7.5 kpc)



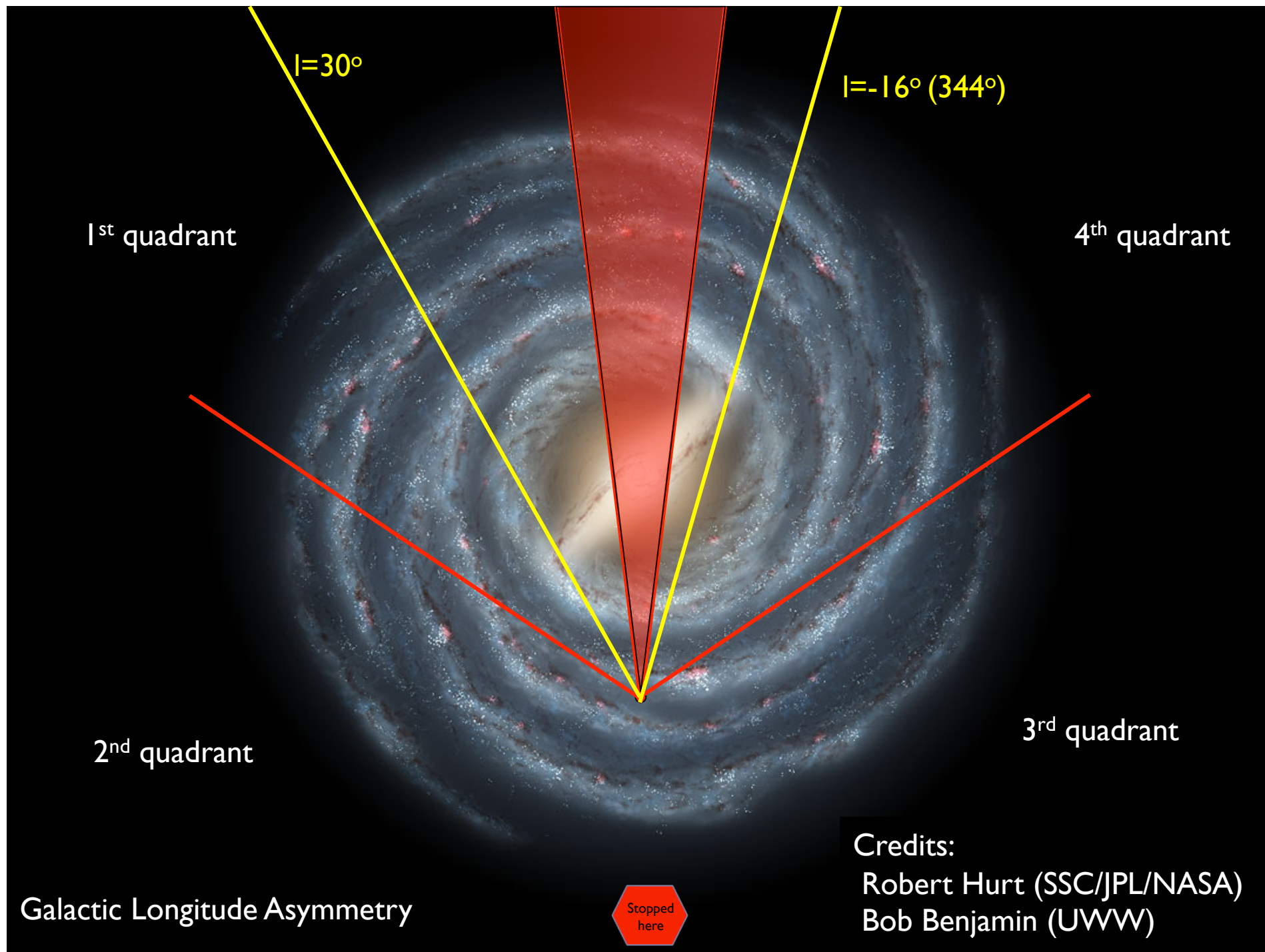


# Galactic Bar

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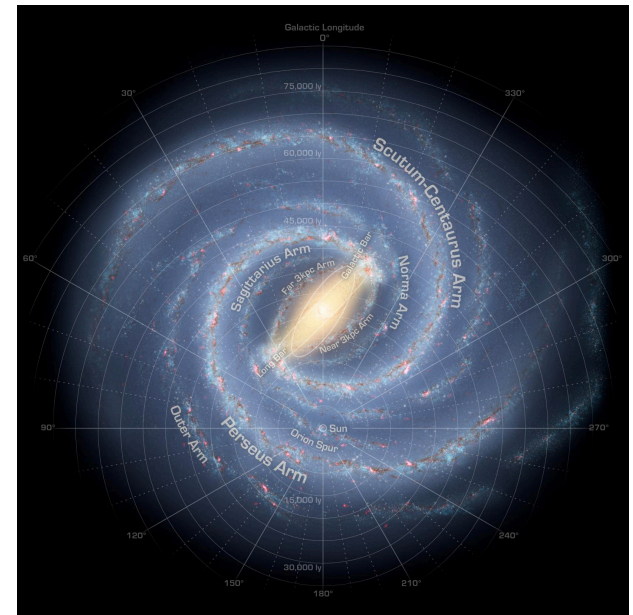
- ▶ Lots of other disk galaxies have a central bar (elongated structure). Does the Milky Way?
- ▶ Photometry – what does the stellar distribution in the center of the Galaxy look like?
  - ▶ Bar-like distribution:  $N = N_0 \exp(-0.5r^2)$ , where  $r^2 = (x^2+y^2)/R^2 + z^2/z_0^2$
  - ▶ Observe  $A(m)$  as a function of Galactic coordinates  $(l,b)$
  - ▶ Use  $N$  as an estimate of your source distribution:
    - ▶ counts  $A(m,l,b)$  appear bar-like
  - ▶ Sevenster (1990s) found overabundance of OH/IR stars in 1<sup>st</sup> quadrant. Asymmetry is also seen in RR Lyrae distribution.
- ▶ Gas kinematics:  $V_c(r) = (4\pi G \rho / 3)^{1/2} r$ 
  - ➔ we should see a straight-line trend of  $V_c(r)$  with  $r$  through the center (we don't).
- ▶ Stellar kinematics – again use a population of easily identifiable stars whose velocity you can measure (e.g. OH/IR stars).
  - ▶ Similar result to gas.





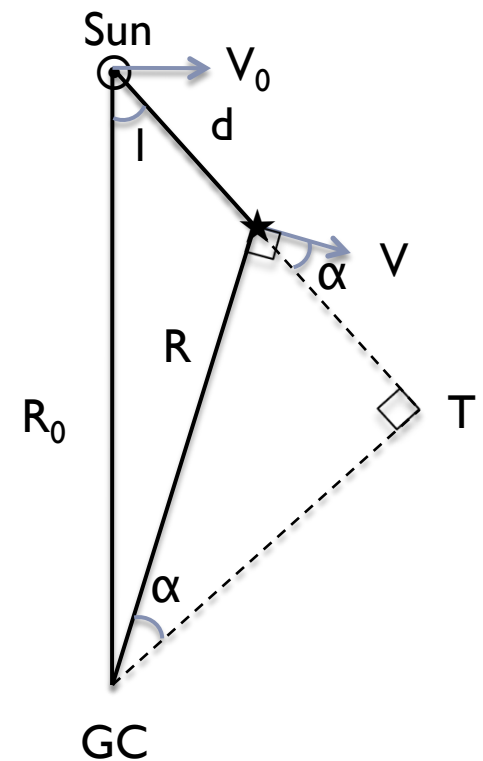
# Galactic Rotation: A Simple Picture

- ▶ Imagine two stars in the Galactic disk; the Sun at distance  $R_0$ , the other at a distance  $R$  from the center and a distance,  $d$ , from the Sun. The angle between the Galactic Center (GC) and the star is  $l$ , and the angle between the motion of the stars and the vector connecting the star and the Sun is  $\alpha$ . The Sun moves with velocity,  $V_0$ , and the other star moves with velocity,  $V$ .
- ▶ See Figure 2.19 in S&G.



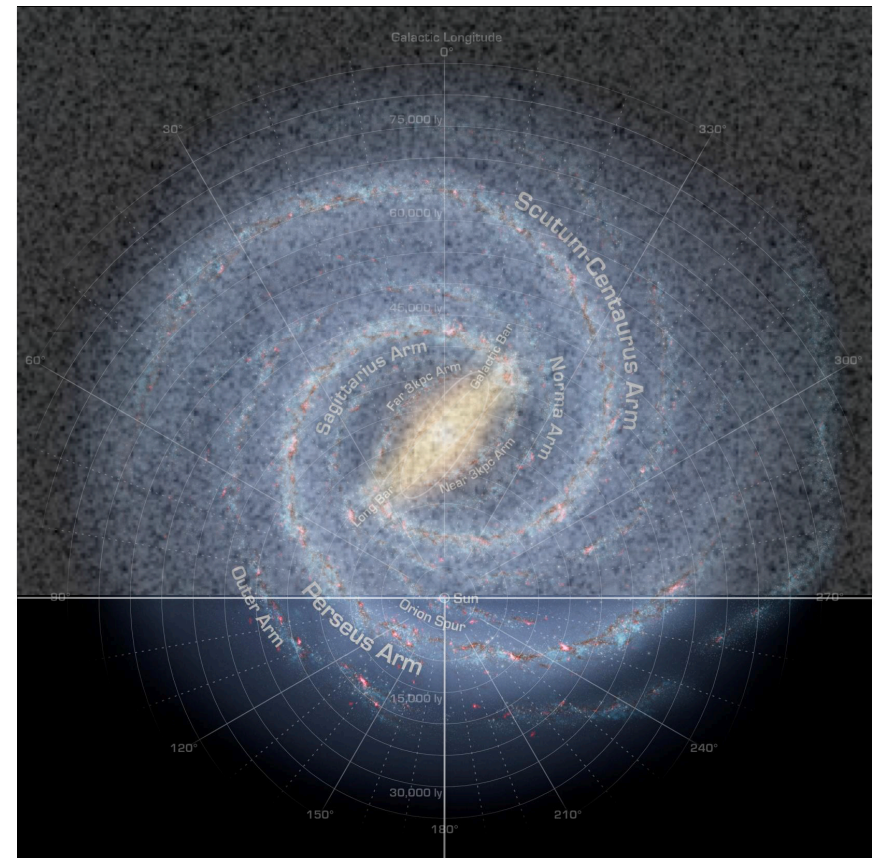
# Relative motion of stars

- ▶ Radial velocity of the star
  - ▶  $V_r = V \cos \alpha - V_0 \sin l$
  - ▶ now use law of sines to get...
  - ▶  $V_r = (\omega_* - \omega_0) R_0 \sin l$ ,
    - ▶  $\omega$  is the angular velocity defined as  $V/R$ .
    - ▶  $l$  is the Galactic longitude
- ▶ Transverse velocity of the star
  - ▶  $V_T = (\omega_* - \omega_0) R_0 \cos l - \omega_* d$



# Longitudinal dependence

- ▶  $90^\circ \leq l \leq 180^\circ$ 
  - ▶ larger  $d$
  - ▶  $R > R_0$
  - ▶  $\omega_*^* < \omega_0$ 
    - ▶ this means increasingly negative radial velocities
- ▶  $180^\circ \leq l \leq 270^\circ$ 
  - ▶  $V_R$  is positive and increases with  $d$

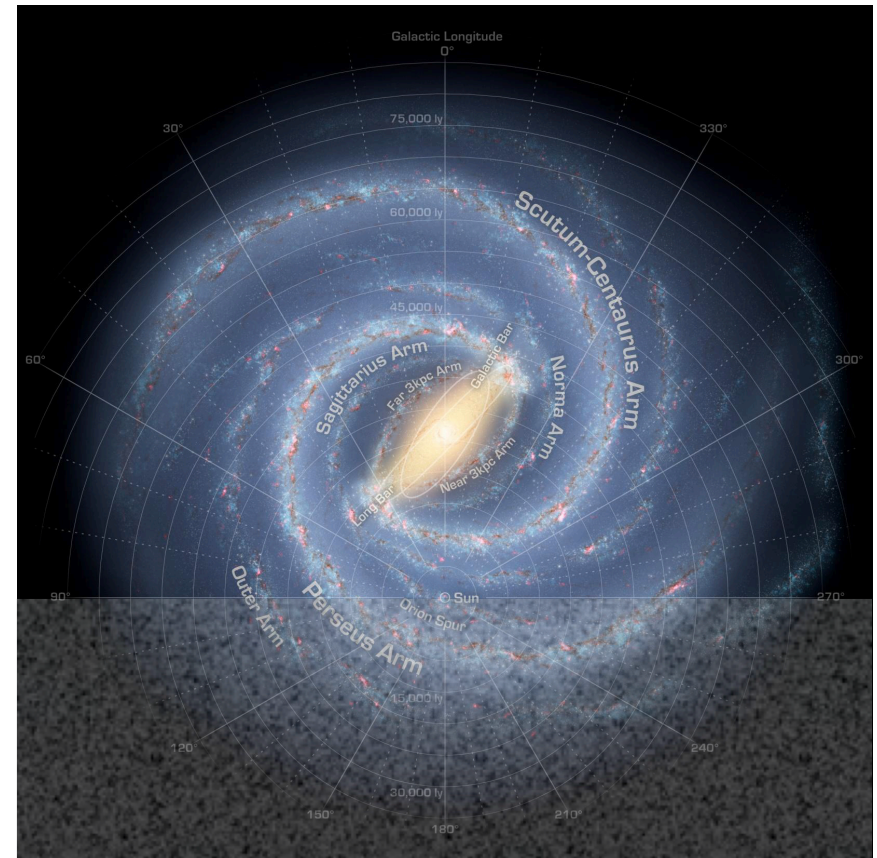


$90^\circ \leq l \leq 180^\circ$

$180^\circ \leq l \leq 270^\circ$

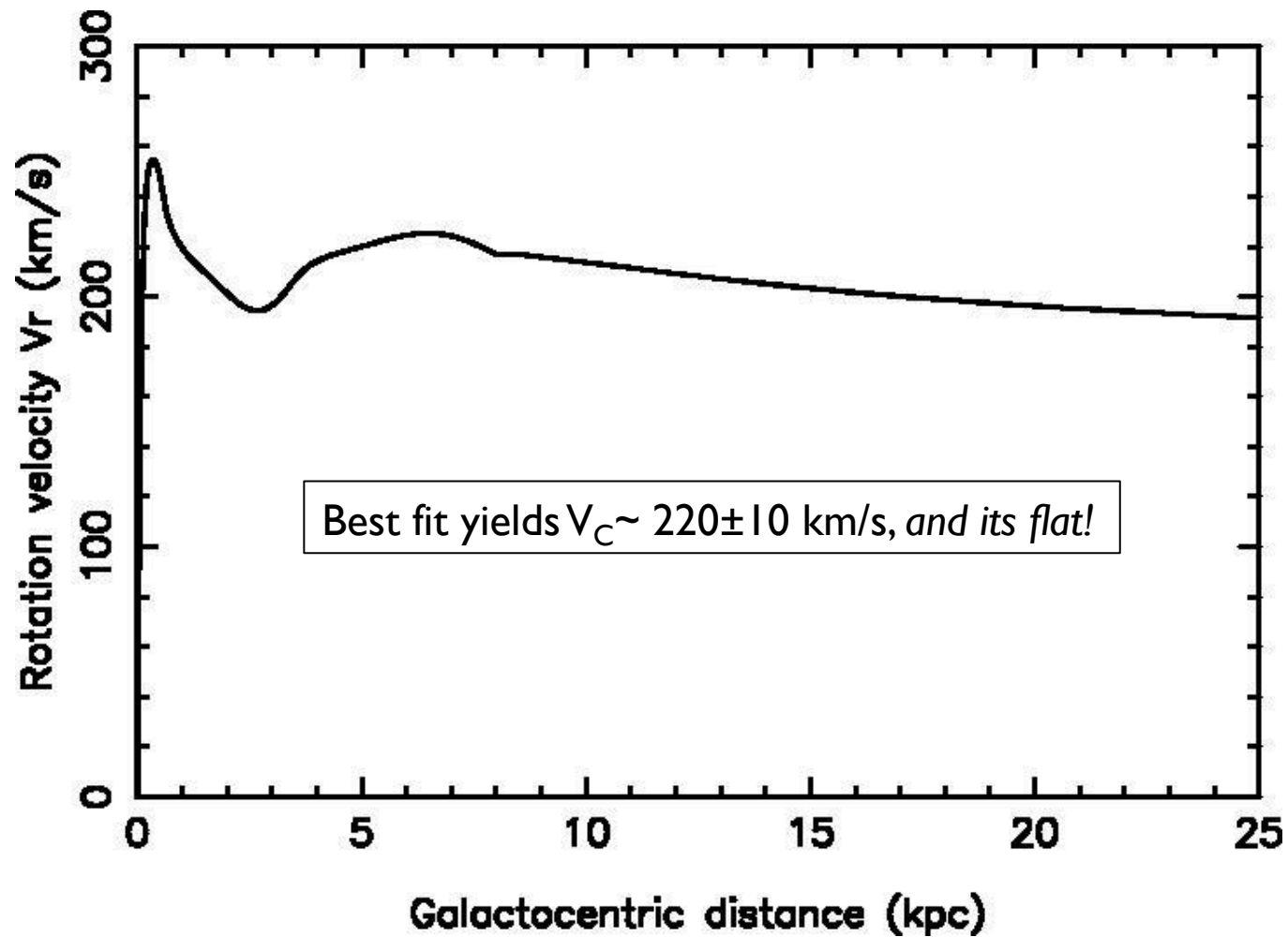


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# Galactic Rotation Curve

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# Oort's Constant A: Disk Shear

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- ▶ Assume  $d$  is small
  - ▶ this is accurate enough for the solar neighborhood
- ▶ Expand  $(\omega_* - \omega_0) = (d\omega/dR)_{R_0}(R - R_0)$
- ▶ Do some algebra....
  - ▶  $V_R = [(dV/dR)_{R_0} - (V_0/R_0)] (R - R_0) \sin l$
- ▶ If  $d \ll R_0$ ,
  - ▶  $(R_0 - R) \sim d \cos(l)$
  - ▶  $V_R = A d \sin(2l)$
- ▶ where  $A = 1/2[(V_0/R_0) - (dV/dR)_{R_0}]$ 
  - ▶ This is the 1<sup>st</sup> Oort constant, and it measures the shear (deviation from rigid rotation) in the Galactic disk.



# Oort's Constant B: Local Vorticity

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- ▶ Do similar trick with the transverse velocity:
  - ▶  $V_T = d [A \cos(2l) + B]$ , and
  - ▶  $\mu_l = [A \cos(2l) + B] / 4.74$  = proper motion of nearby stars
- ▶  $B = -12.4 \pm 0.6$  km/s/kpc
  - ▶ A measure of angular-momentum gradient in disk
- ▶  $\omega_0 = V_0 / R_0 = A - B$
- ▶  $(dV/dR)_{R_0} = -(A + B)$
- ▶ Observations of local kinematics can constrain the global form of the Galactic rotation curve

